



SEARCH FOR NEW SOURCES OF CP VIOLATION IN CHARM BARYONIC DECAYS WITH THE LHCb EXPERIMENT

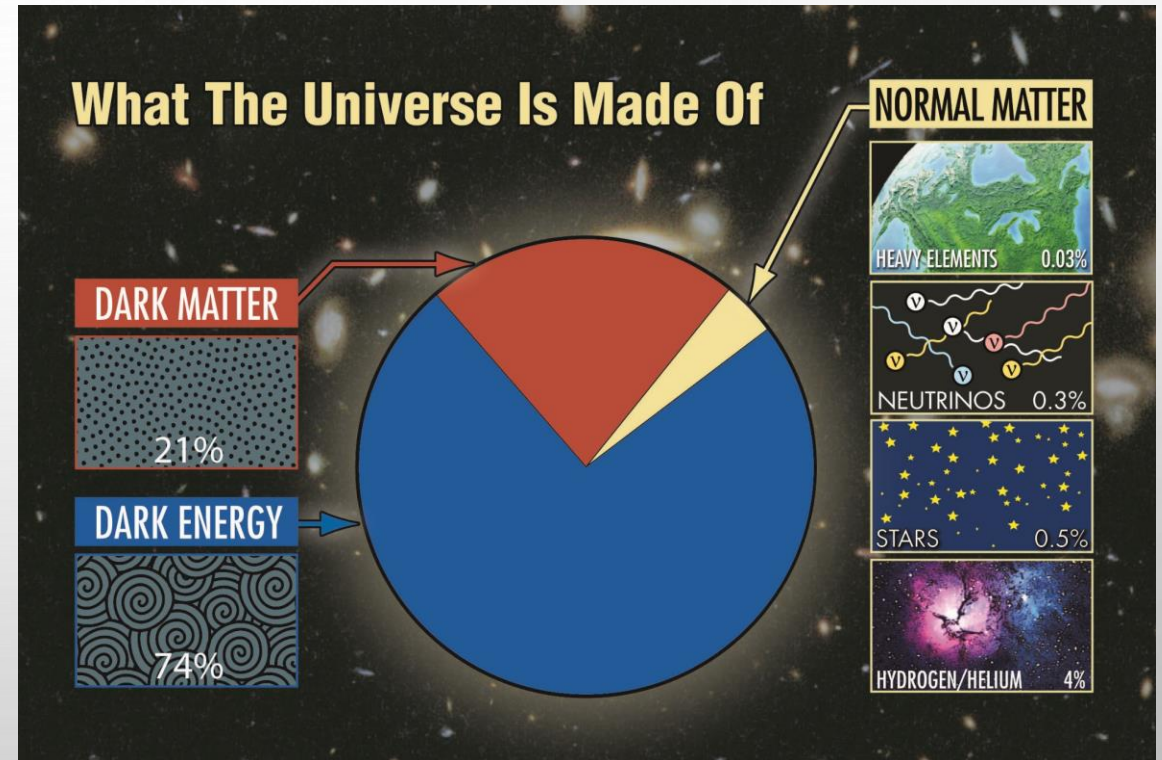
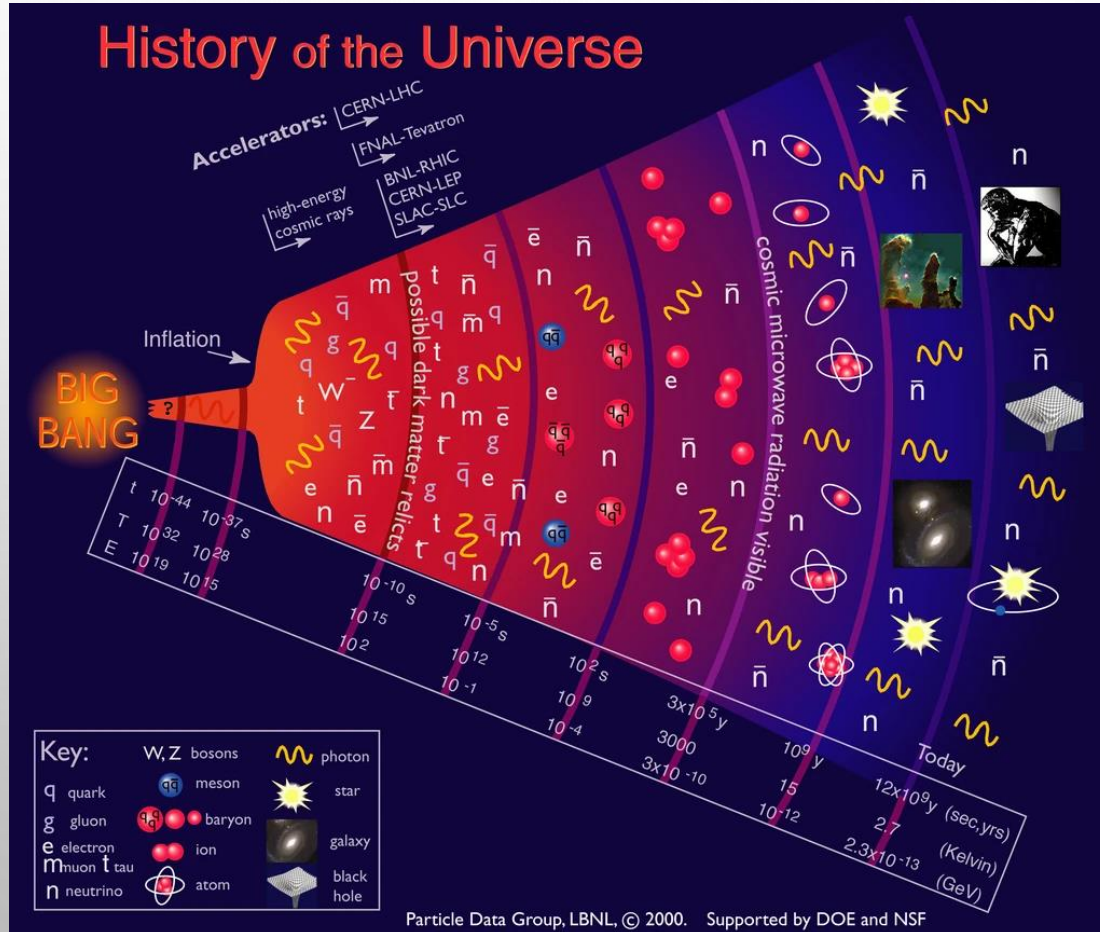
TOMASZ SZUMLAK

LHCb COLLABORATION

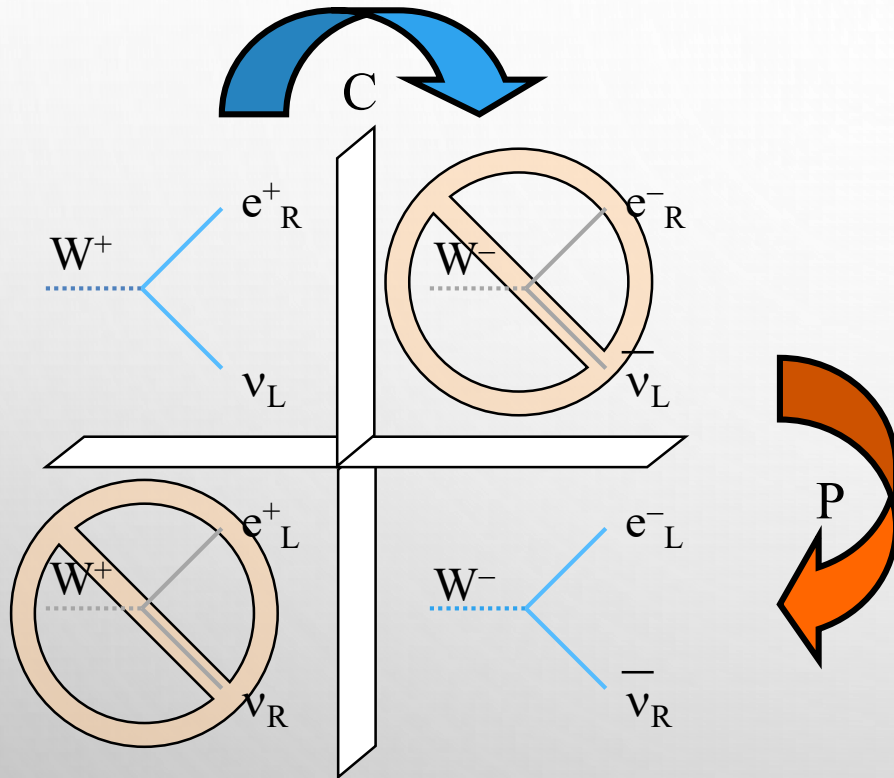
AGH-UST

JAGIELLONIAN UNIVERSITY SEMINAR, 21/06/2021, KRAKÓW

WHY WE ARE HERE AT ALL?



WHAT'S THE MATTER WITH ANTI-MATTER...?



WEAK INTERACTIONS VIOLATE MAXIMALLY SPACE PARITY SYMMETRY.

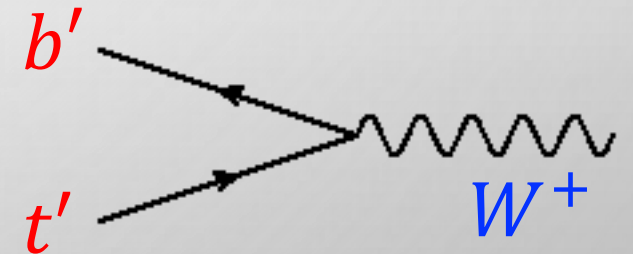
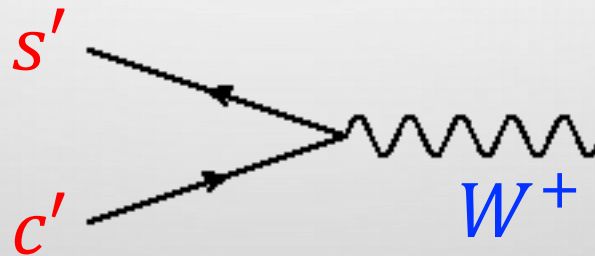
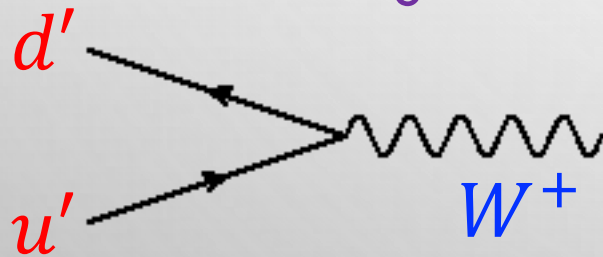
- WOLFGANG PAULI: “I CANNOT BELIEVE GOD IS A WEAK LEFT-HANDER.”

- $SU_L(2)$ symmetry for massless quarks

$$\mathcal{L}_W = \frac{g}{\sqrt{2}} u'_L \gamma_\mu W^\mu d'_L \quad \text{x3!}$$

- Flavour universality – interactions do not depend on the family.

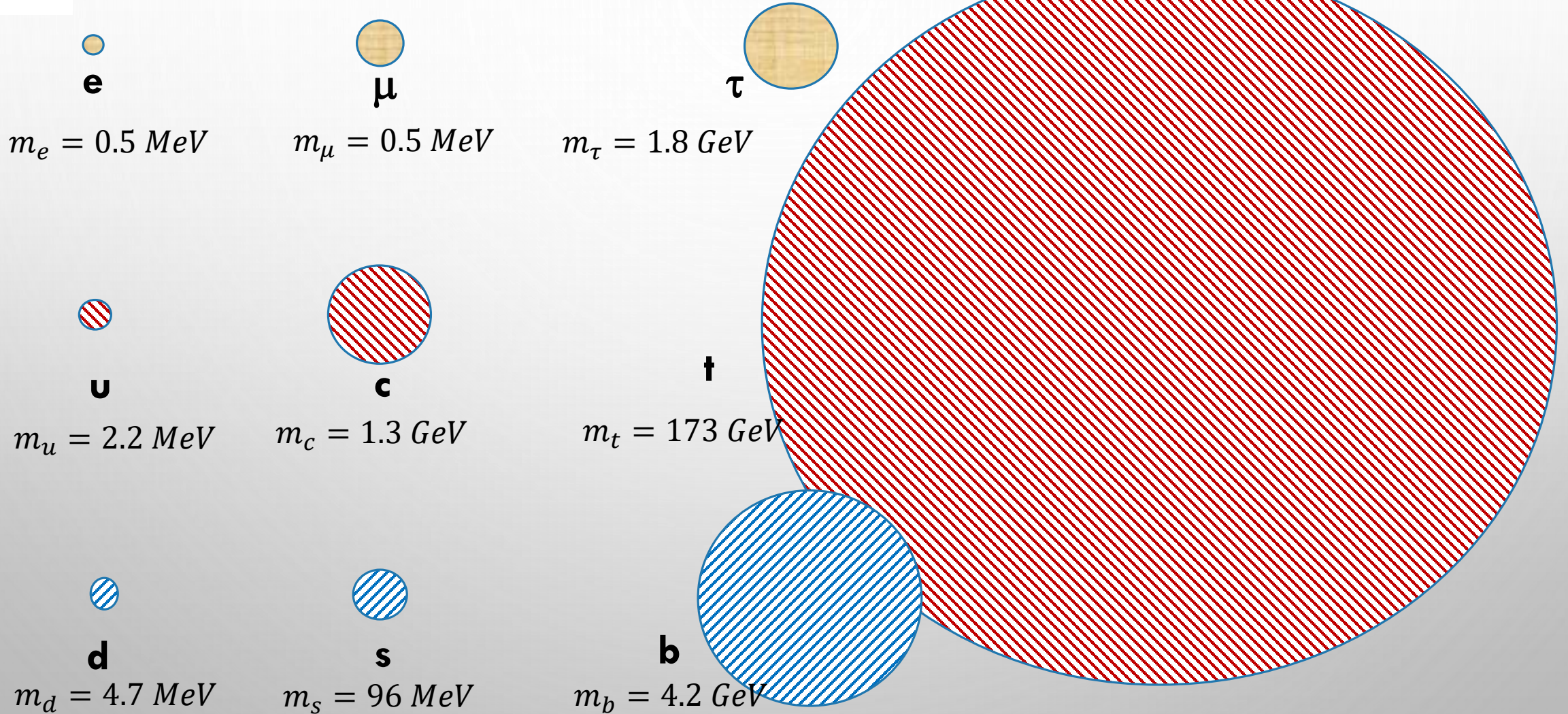
- Cannot distinguish d' from s'



- No CP violation possible!!

- Now we add the mass to the picture!

MASS HIERARCHY PROBLEM...



(Interaction base)

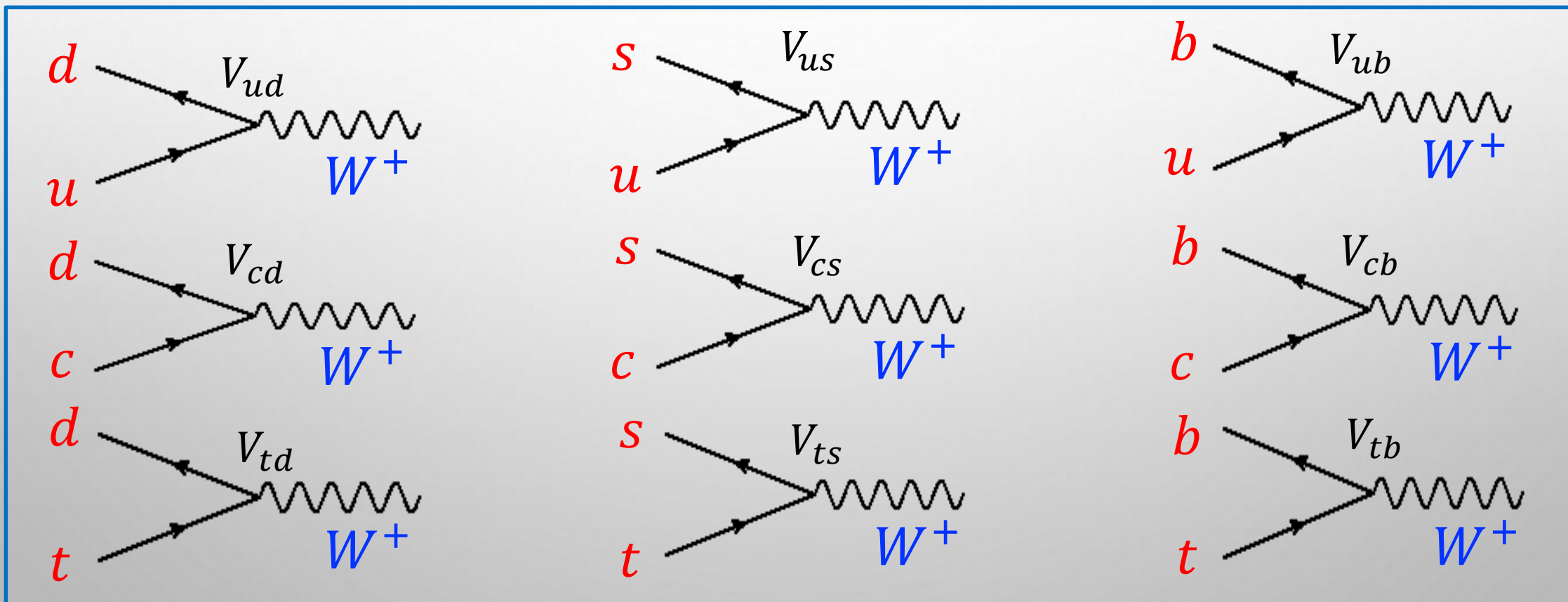
$$\mathcal{L}_W = \frac{g}{\sqrt{2}} u'_L \gamma_\mu W^\mu d'_L$$



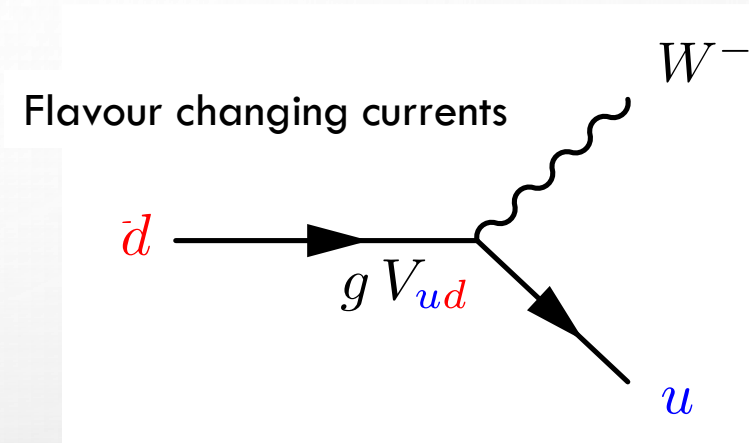
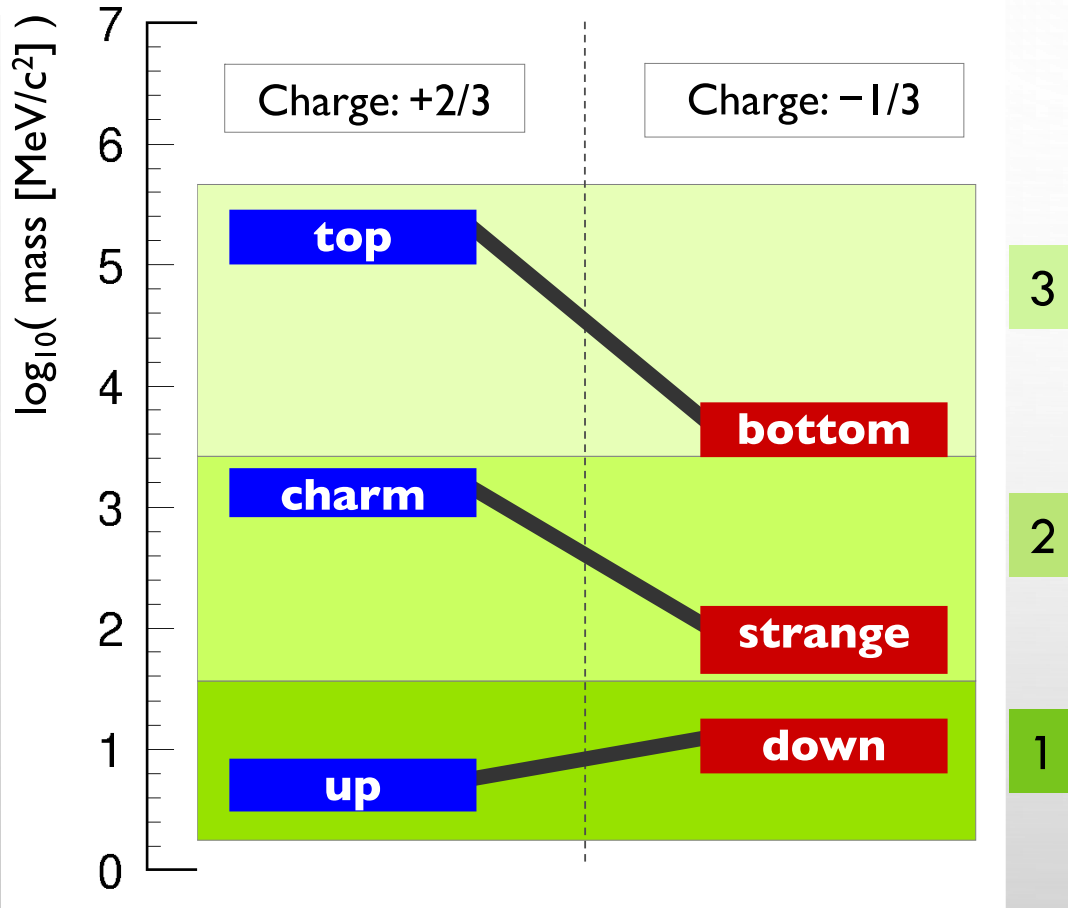
(Mass base)

$$\mathcal{L}_W = \frac{g}{\sqrt{2}} V_{CKM} u_L \gamma_\mu W^\mu d_L$$

Change of base: $u'_i = (V^u)_{ij} u_j$ and: $d'_i = (V^d)_{ij}^\dagger d_j$

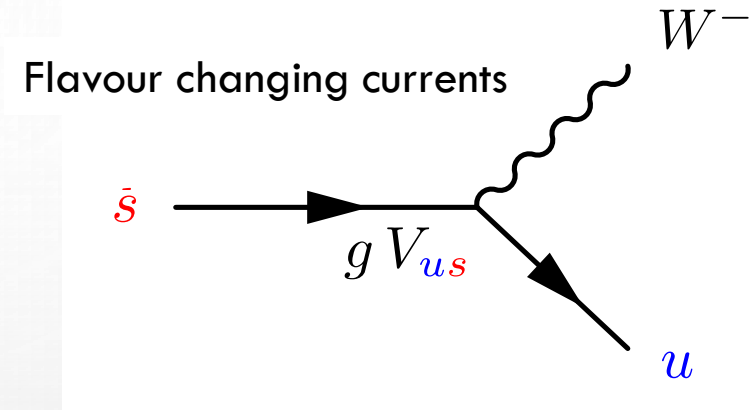
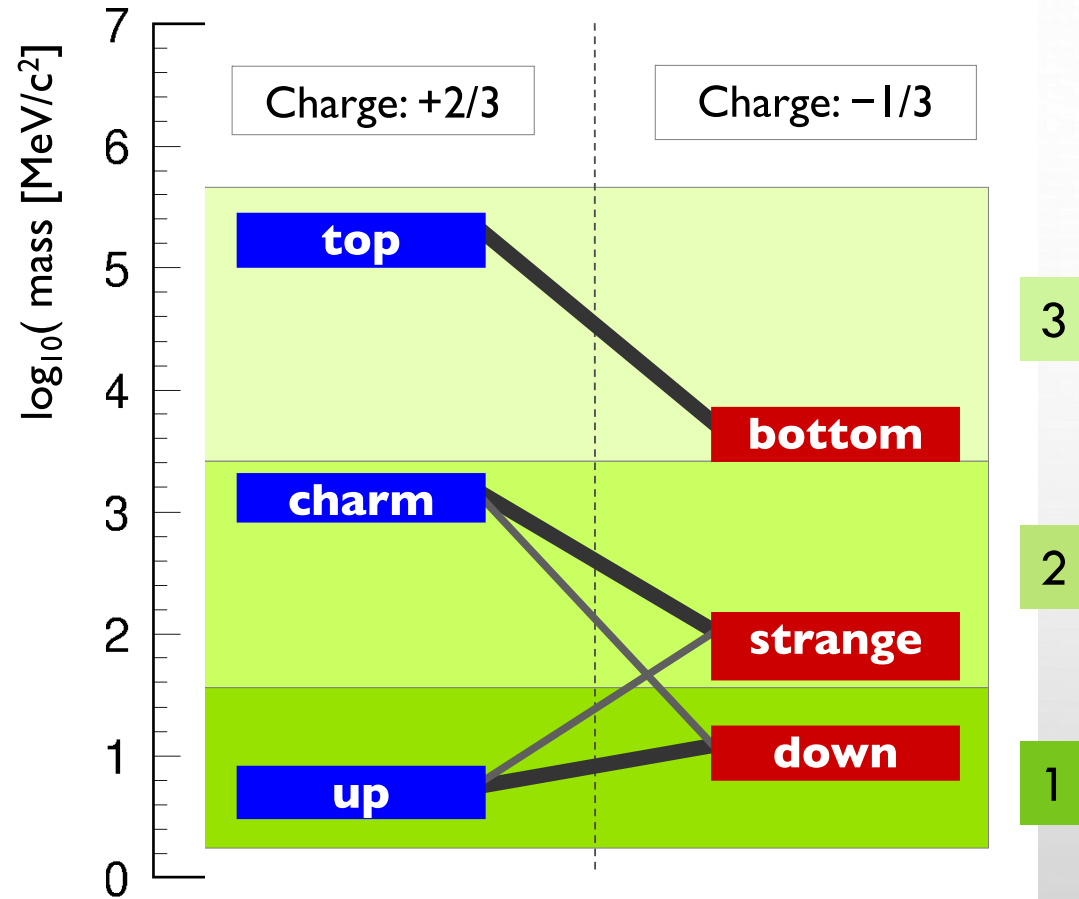


BUILDING CKM MATRIX



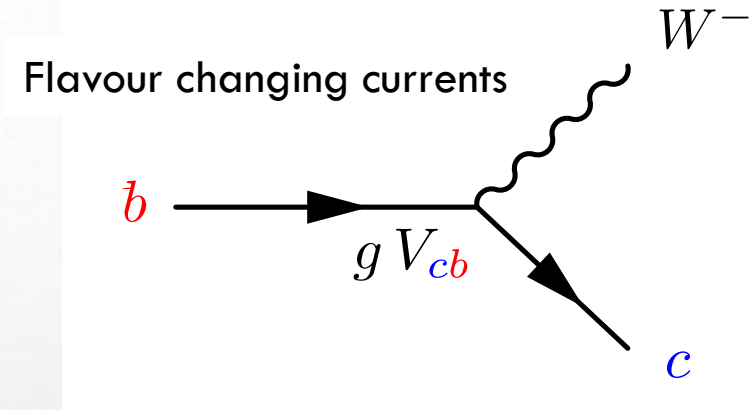
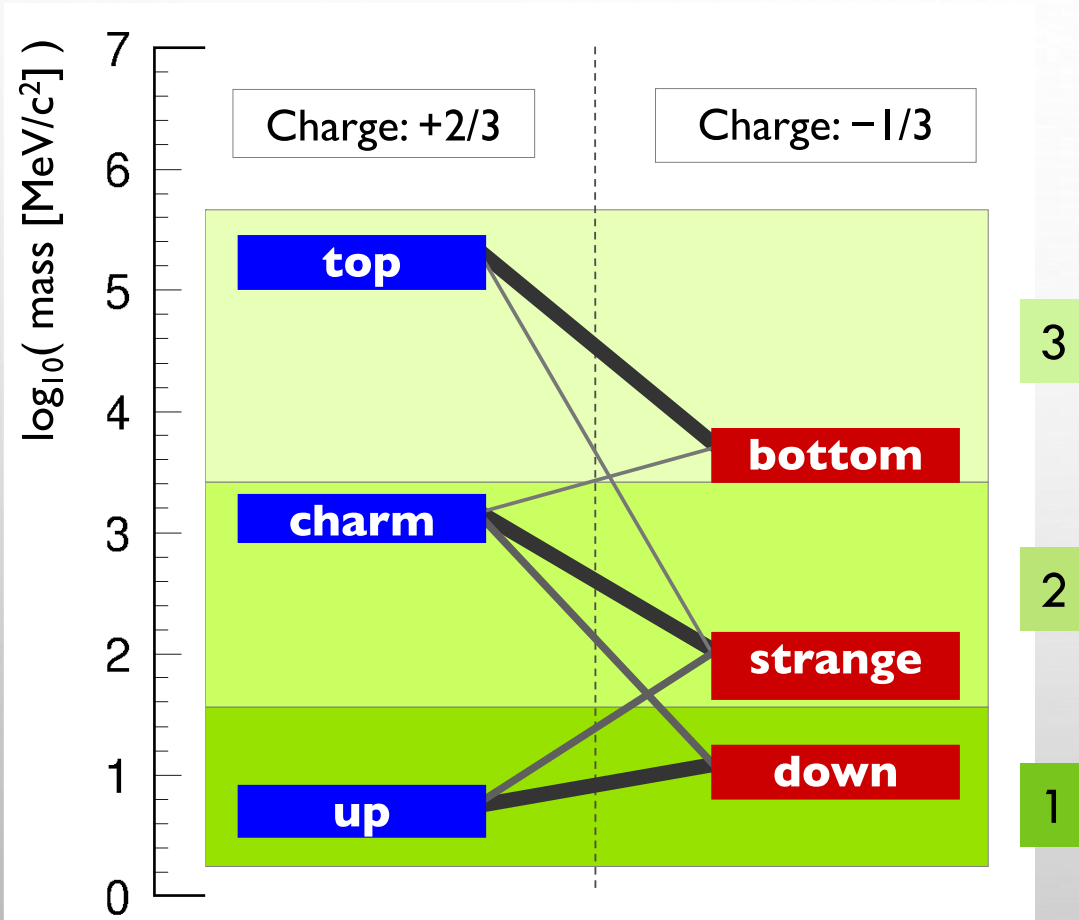
$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & & \\ & V_{cs} & \\ & & V_{tb} \end{pmatrix}$$

BUILDING CKM MATRIX



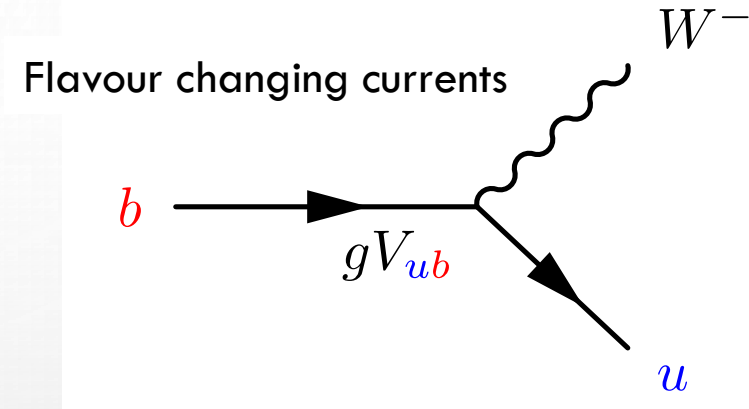
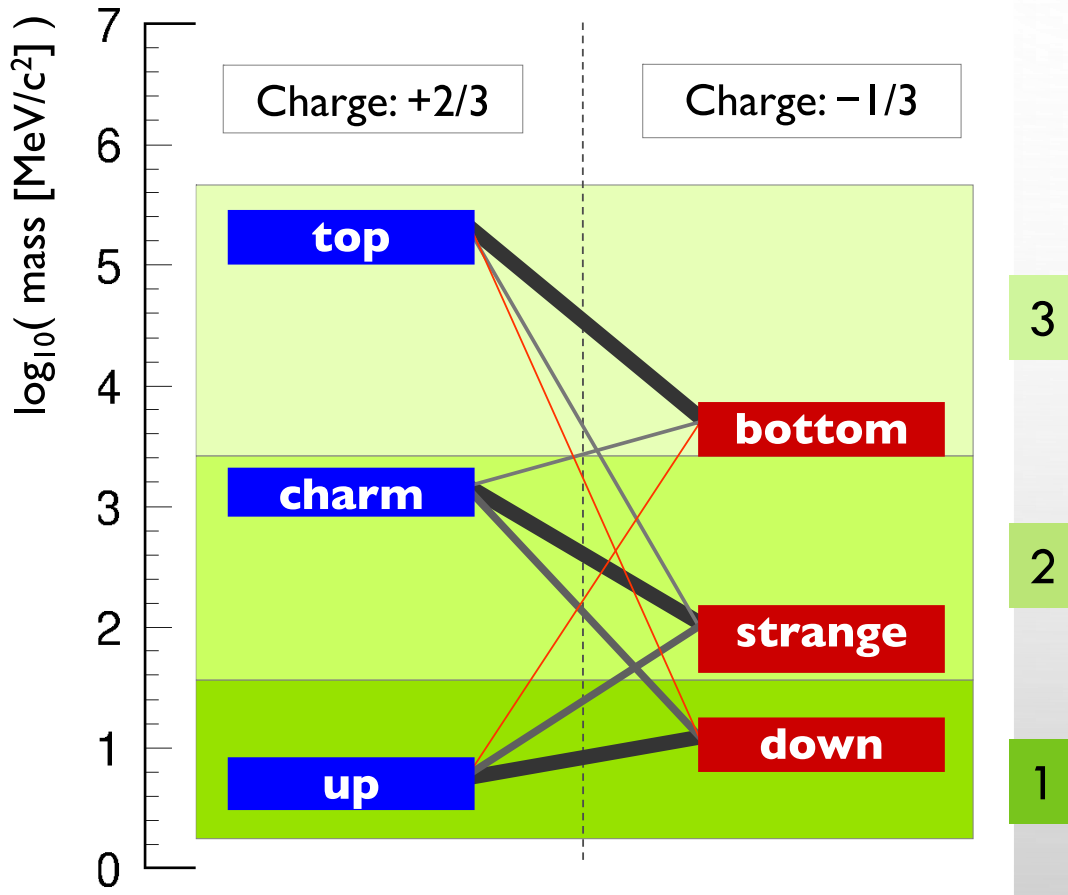
$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & \\ V_{cd} & V_{cs} & \\ & & V_{tb} \end{pmatrix}$$

BUILDING CKM MATRIX



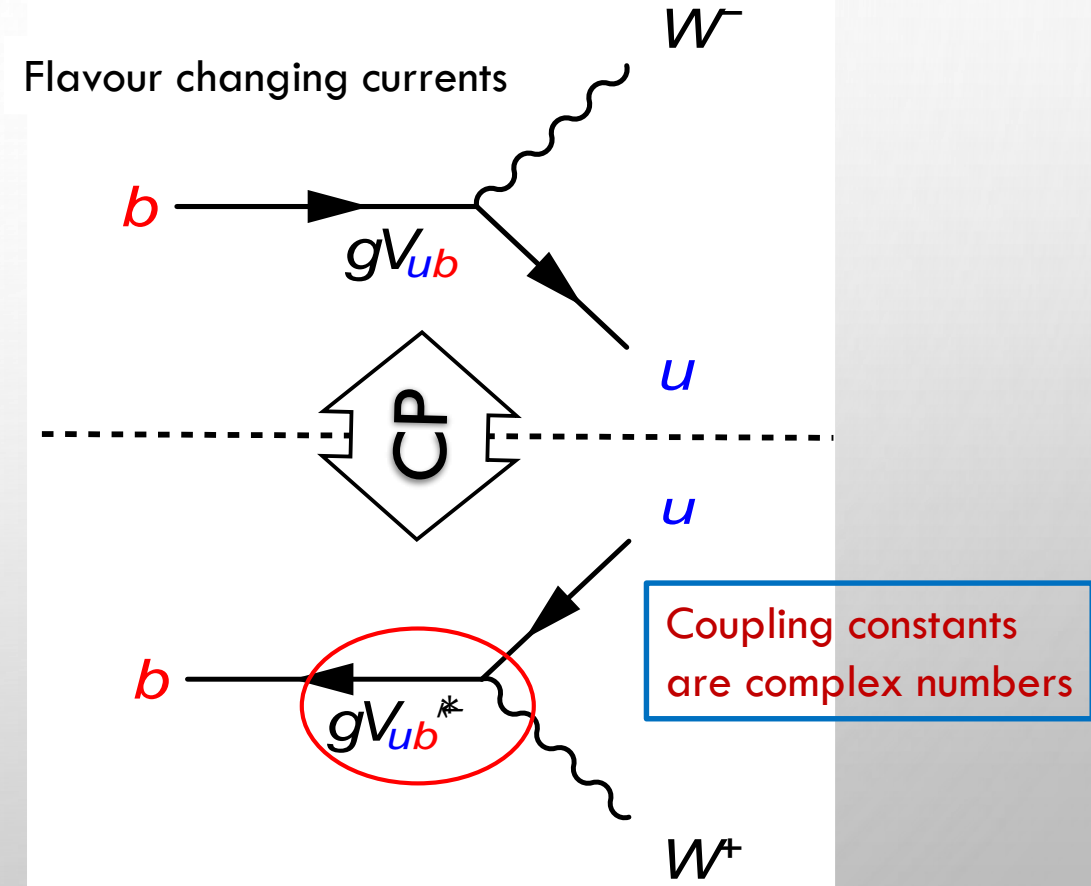
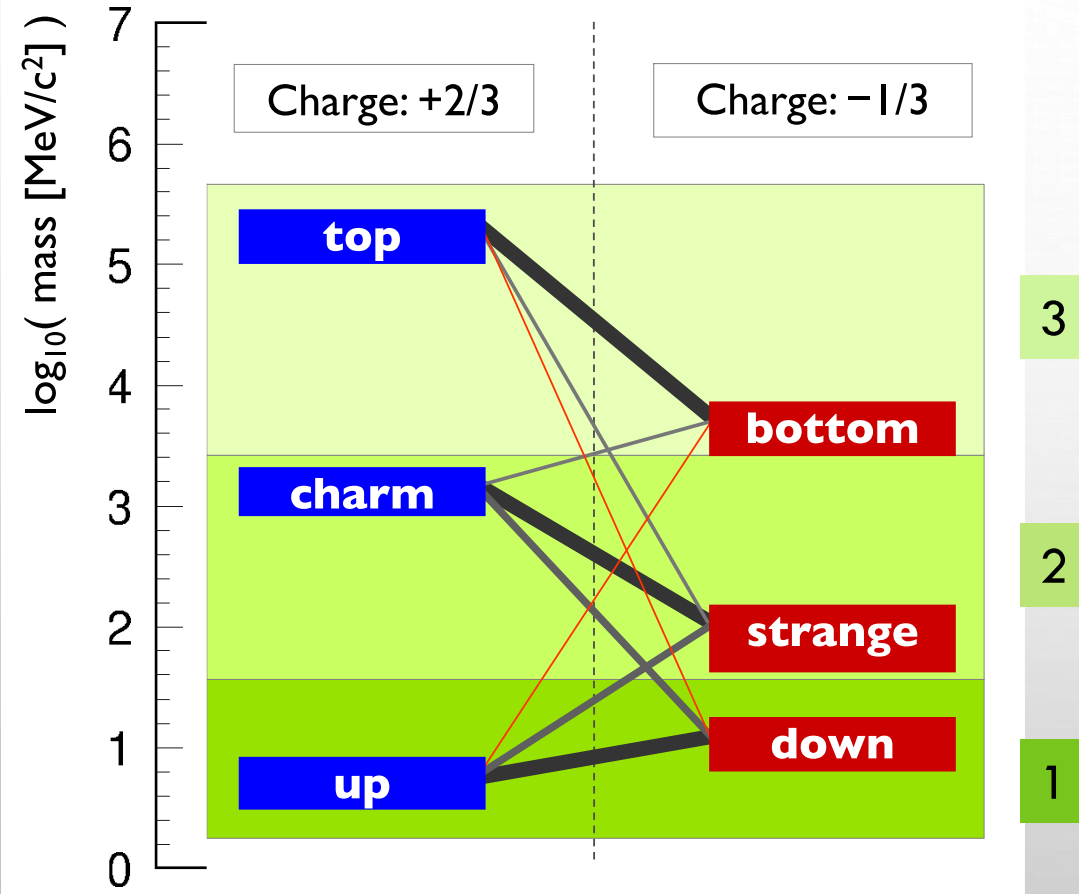
$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

BUILDING CKM MATRIX



$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

BUILDING CKM MATRIX



NEED FOR 3 GENERATIONS

$$V_{CKM}: \begin{matrix} & d & s & b \\ \begin{matrix} u \\ c \\ t \end{matrix} & \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \end{matrix}$$

- Wolfenstein parametrisation: $V_{CKM} =$

$$\begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

→ One complex phase

$$V_{CKM}: \begin{matrix} & d & s \\ \begin{matrix} u \\ c \end{matrix} & \begin{pmatrix} V_{ud} & V_{us} \\ V_{cd} & V_{cs} \end{pmatrix} \end{matrix}$$

$$V_{CKM} =$$

$$\begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda \\ -\lambda & 1 - \frac{1}{2}\lambda^2 \end{pmatrix}$$

→ No CP violation

- 3 generations with quark doublets are necessary at the least to broke the CP symmetry

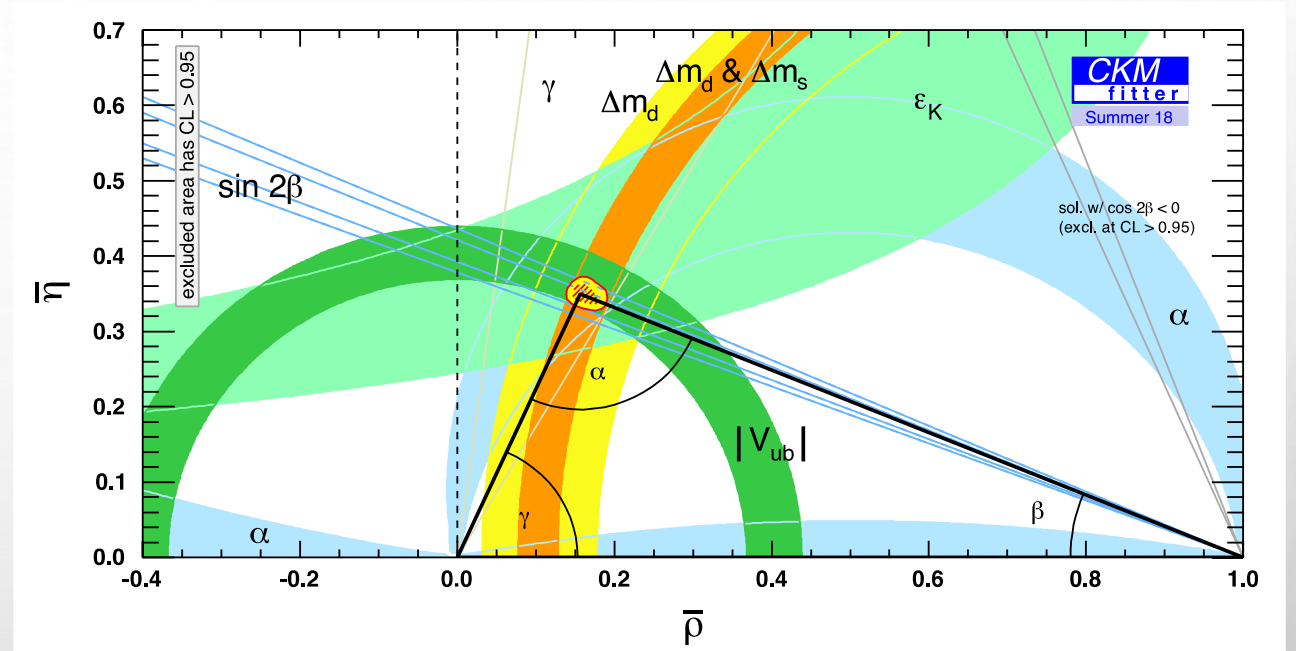
NEED FOR 3 GENERATIONS

$$V_{CKM}: \begin{matrix} & d & s & b \\ \begin{matrix} u \\ c \\ t \end{matrix} & \begin{pmatrix} V_{ud} \\ V_{cd} \\ V_{td} \end{pmatrix} & \begin{pmatrix} V_{us} \\ V_{cs} \\ V_{ts} \end{pmatrix} & \begin{pmatrix} V_{ub} \\ V_{cb} \\ V_{tb} \end{pmatrix} \end{matrix}$$

- Unitarity triangle view: $V_{CKM} =$

$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ -|V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & -|V_{ts}|e^{i\beta_s} & |V_{tb}| \end{pmatrix}$$

Unitarity: $V_{CKM}V_{CKM}^\dagger = 1$



CP violation:

→ Surface $\neq 0$

→ Non-zero CP-phases.

CPV IS UNIVERSAL IN THE SM

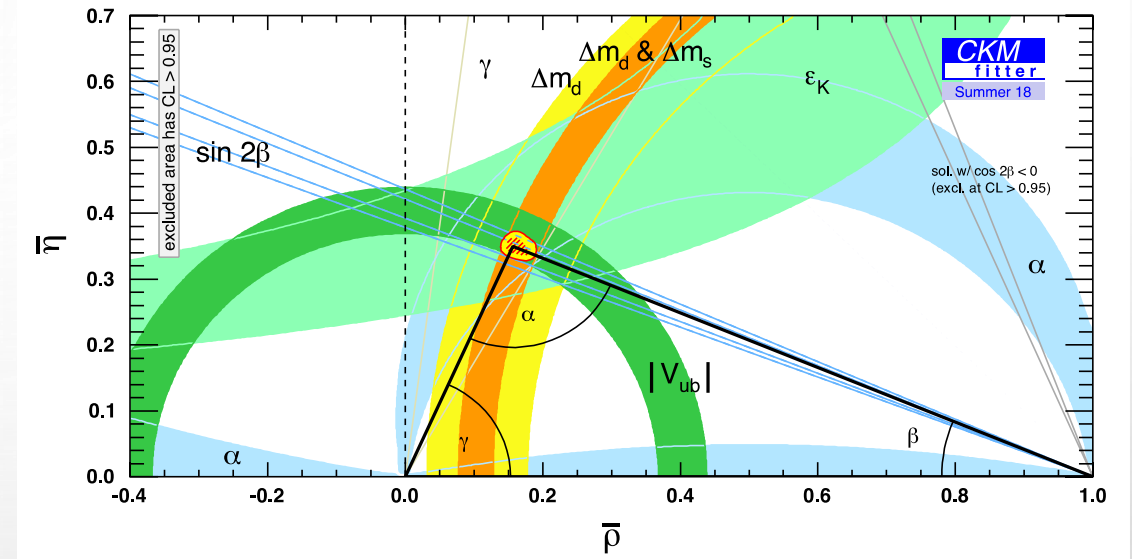
- CPV CANNOT DEPEND ON REPRESENTATION.
 - AREA OF THE UNITARITY TRIANGLE
 - JARLSKOG INVARIANT: $J = 3 \times 10^{-5}$
- 3 quark generations with different masses!!

- $m_u \neq m_c$; $m_c \neq m_t$; $m_t \neq m_u$
- $m_d \neq m_s$; $m_s \neq m_b$; $m_b \neq m_d$

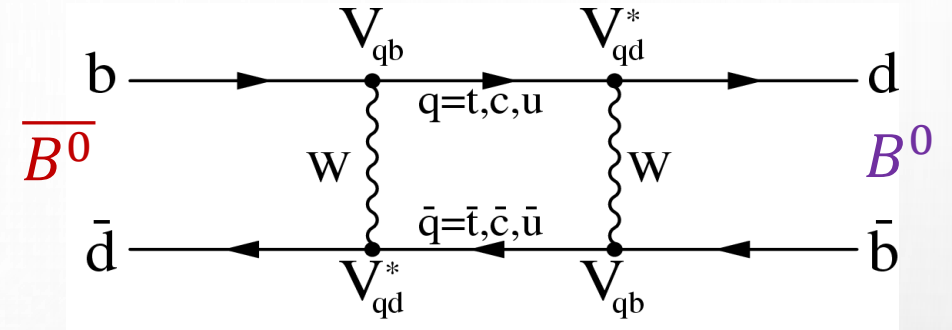
- Jarlskog (1987) CPV in the SM

$$\begin{aligned}
 - \det[M_u M_u^\dagger, M_d M_d^\dagger] &= 2 \cdot J \cdot (m_t^2 - m_c^2)(m_c^2 - m_u^2)(m_u^2 - m_t^2) \\
 &\quad \times (m_b^2 - m_s^2)(m_s^2 - m_d^2)(m_d^2 - m_b^2)
 \end{aligned}$$

$$M_{ij} = Y_{ij} v / \sqrt{2}$$



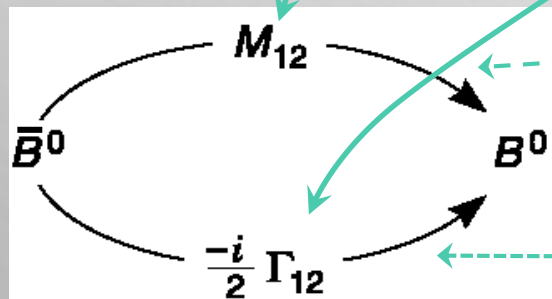
- Quantum interference $\overline{B^0}$ i B^0



- TIME EVOLUTION OF B^0 | $\overline{B^0}$ SYSTEM DESCRIBED BY EFFECTIVE HAMILTONIAN

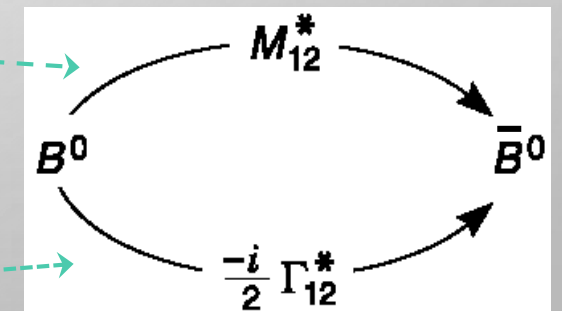
$$i \frac{\partial}{\partial t} \psi = H \psi \quad \rightarrow \quad \psi(t) = a(t) |B^0\rangle + b(t) |\overline{B^0}\rangle \quad \equiv \quad \begin{pmatrix} a(t) \\ b(t) \end{pmatrix}$$

$$H = \underbrace{\begin{pmatrix} M & M_{12} \\ M_{12}^* & M \end{pmatrix}}_{\text{Hermitian mass matrix}} - \frac{i}{2} \underbrace{\begin{pmatrix} \Gamma & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma \end{pmatrix}}_{\text{Hermitian decay matrix}}$$



$M_{12} B^0 \leftrightarrow \overline{B^0}$ off-shell particle exchange (short range processes)

$\Gamma_{12} B^0 \leftrightarrow f \leftrightarrow \overline{B^0}$ on-shell particle exchange (long range processes) $f = \pi^+ \pi^-$



$$i \frac{\partial}{\partial t} \psi(t) = \begin{pmatrix} M - \frac{i}{2} \Gamma & M_{12} - \frac{i}{2} \Gamma_{12} \\ M_{12}^* - \frac{i}{2} \Gamma_{12}^* & M - \frac{i}{2} \Gamma \end{pmatrix} \psi(t)$$

$$\Rightarrow \psi(t) = \alpha |B_H(t)\rangle + \beta |B_L(t)\rangle$$

e-vectors:

$$|B_H(t)\rangle = |B_H\rangle e^{-i\omega_+ t}$$

$$|B_L(t)\rangle = |B_L\rangle e^{-i\omega_- t}$$

B_H, B_L : e-states of mass

$$|B_H\rangle = p |B^0\rangle + q |\overline{B^0}\rangle$$

$$|B_L\rangle = p |B^0\rangle - q |\overline{B^0}\rangle$$

$B^0, \overline{B^0}$: e-states of flavour

$$\omega_{\pm} = m_{\pm} - \frac{i}{2} \Gamma_{\pm} \quad \begin{cases} m_{\pm} = M \pm \frac{1}{2} \Delta m & \text{masses} \\ \Gamma_{\pm} = \Gamma \pm \frac{1}{2} \Delta \Gamma & \text{lifetimes} \end{cases}$$

$$\Delta m = 2 \Re \sqrt{\left(M_{12} - \frac{i}{2} \Gamma_{12}\right) \left(M_{12}^* - \frac{i}{2} \Gamma_{12}^*\right)}$$

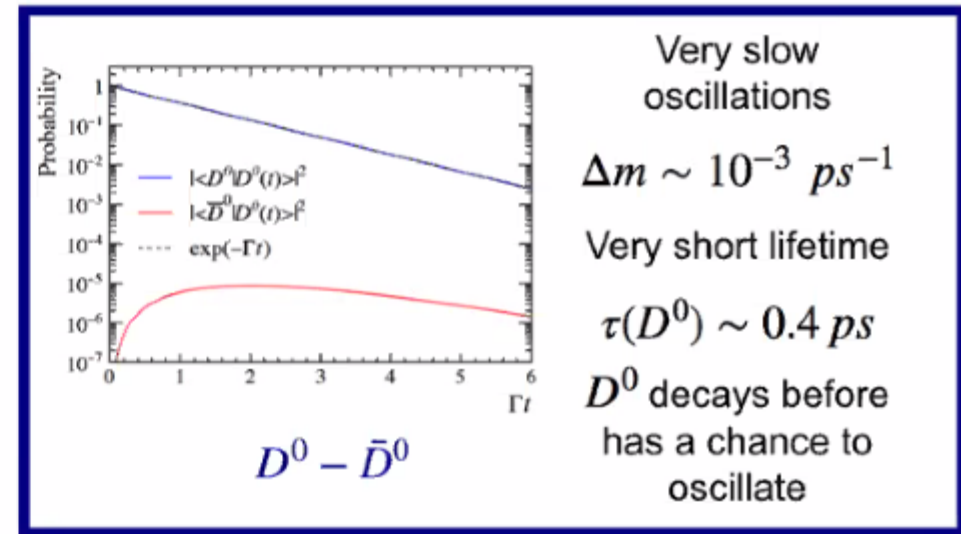
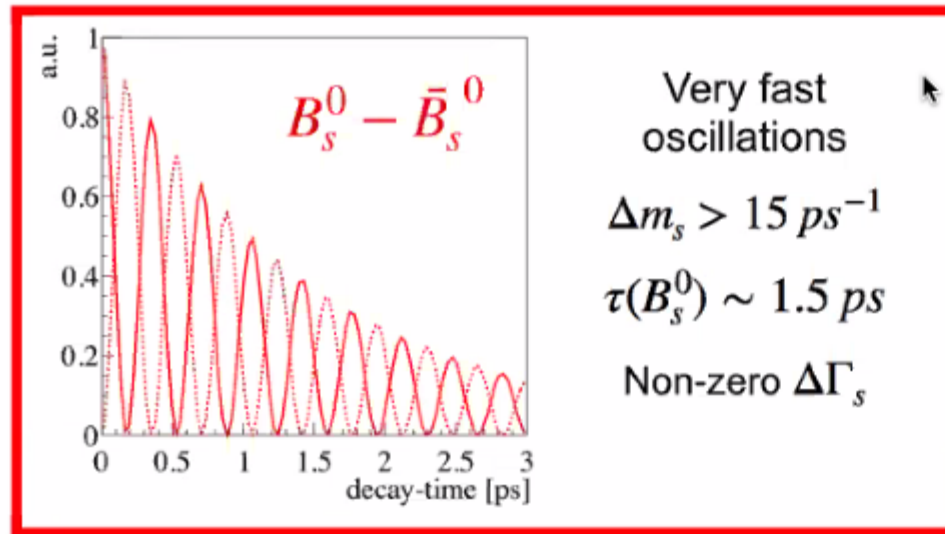
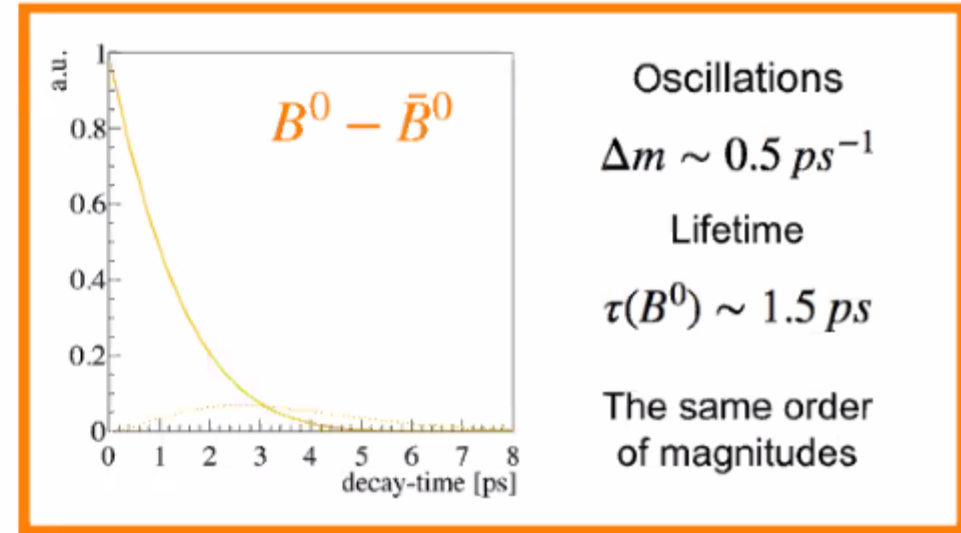
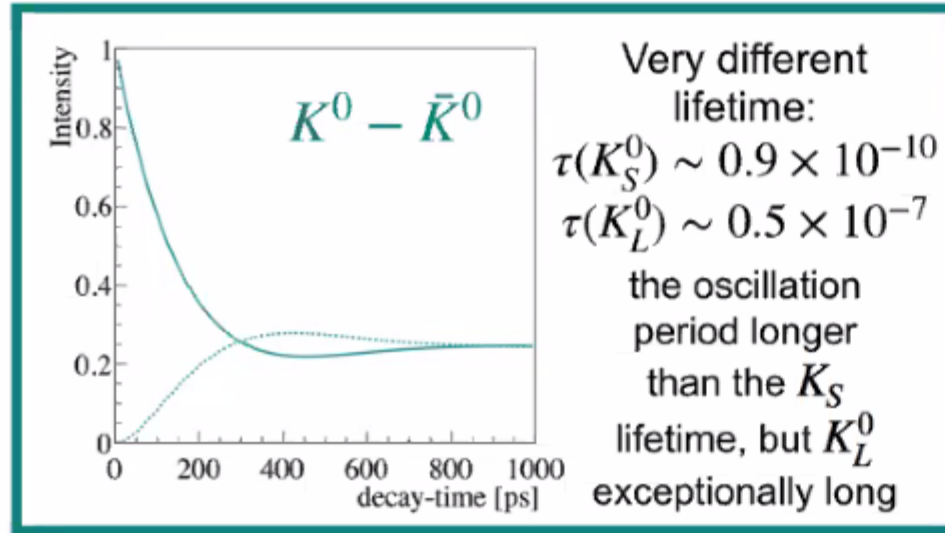
$$\Delta \Gamma = 4 \Im \sqrt{\left(M_{12} - \frac{i}{2} \Gamma_{12}\right) \left(M_{12}^* - \frac{i}{2} \Gamma_{12}^*\right)}$$

Eigen problem solution:

$$q/p = - \sqrt{\left(M_{12}^* - \frac{i}{2} \Gamma_{12}^*\right) / \left(M_{12} - \frac{i}{2} \Gamma_{12}\right)}$$

$$\begin{aligned} B^0 &: \Delta \Gamma \approx 0, |q/p| = 1 \\ B_S^0 &: \Delta \Gamma / \Delta m \ll 1, |q/p| = 1 \\ K^0 &: \Delta \Gamma / \Delta m \simeq 1, |q/p| - 1 \simeq 10^{-3} \end{aligned}$$

THE SAME PHYSICS, DIFFERENT CONSTANTS...



MIXING AND CPV - SUMMARY

$$x = \frac{M_H - M_L}{\Gamma} = \frac{\Delta m}{\Gamma} \quad y = \frac{\Gamma_H - \Gamma_L}{2\Gamma} = \frac{\Delta\Gamma}{2\Gamma}$$

Δm – determines mixing frequency, if x or y different from zero the mixing can occur

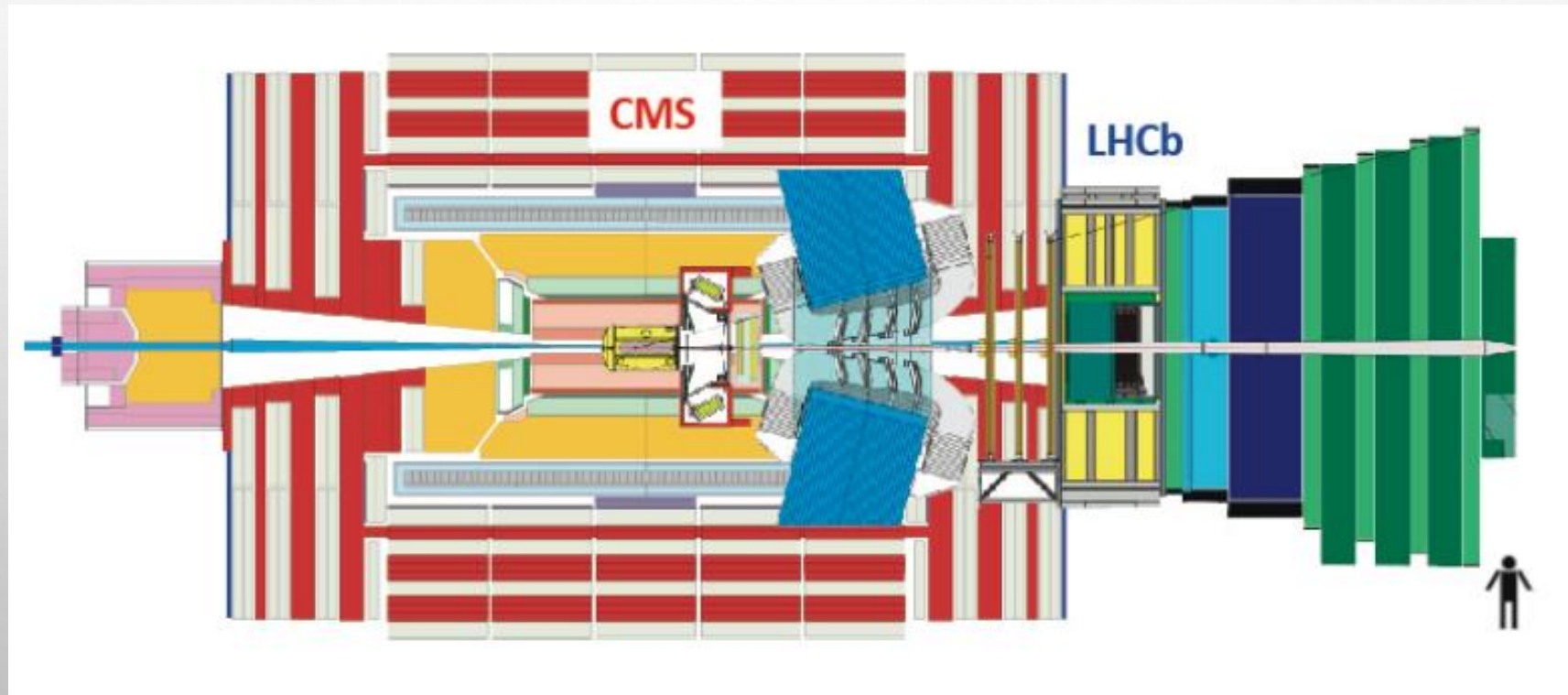
We also define the weak phase or CP violating phase:

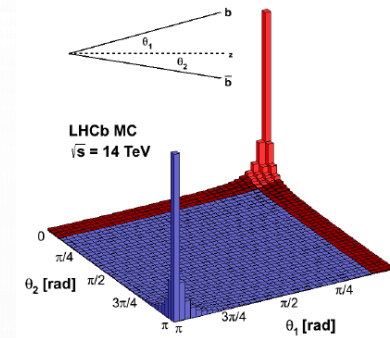
$$\phi = \arg(-M_{12} - \Gamma_{12})$$

If ϕ is different from zero and/or $\left|\frac{p}{q}\right| \neq 1$ we also can have CP violation on top of mixing

$$\Delta m_q = \frac{G_f^2}{6\pi^2} m_{B_q} M_W^2 f\left(\frac{m_t^2}{M_W^2}\right) \eta_{QCD} B_{B_q} f_{B_q}^2 |V_{tb}^* V_{tq}|^2$$

□ NON TYPICAL GEOMETRY, BUT A TYPICAL COMPOSITION...





❑ AFTER RUN 1 AND RUN 2 LHCb PROVED TO BE THE **GENERAL-PURPOSE FORWARD DETECTOR**

❑ A SINGLE ARM SPECTROMETER – NOT YOUR TYPICAL GEOMETRY FOR A COLLIDER BASED EXPERIMENT!

❑ FULLY INSTRUMENTED IN THE PSEUDO-RAPIDITY RANGE OF $(2 < \eta < 5)$

❑ CAN REGISTER UP TO 40% OF ALL HEAVY QUARKS WITH ONLY 4% OF THE SOLID ANGLE COVERAGE!

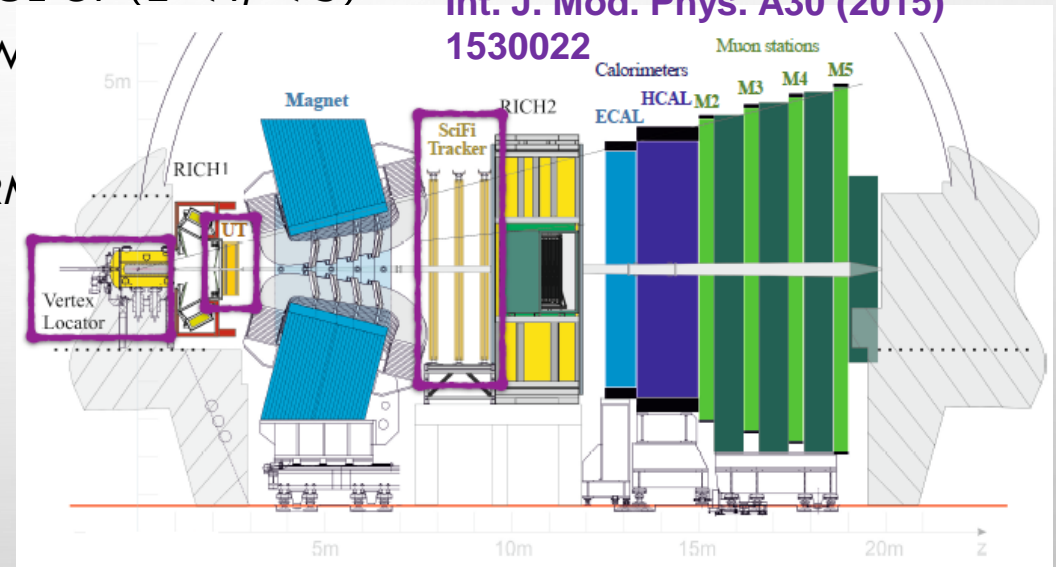
❑ VERY PRECISE MEASUREMENTS IN BEAUTY AND CHARM SECTOR AND NEW PHYSICS SEARCH

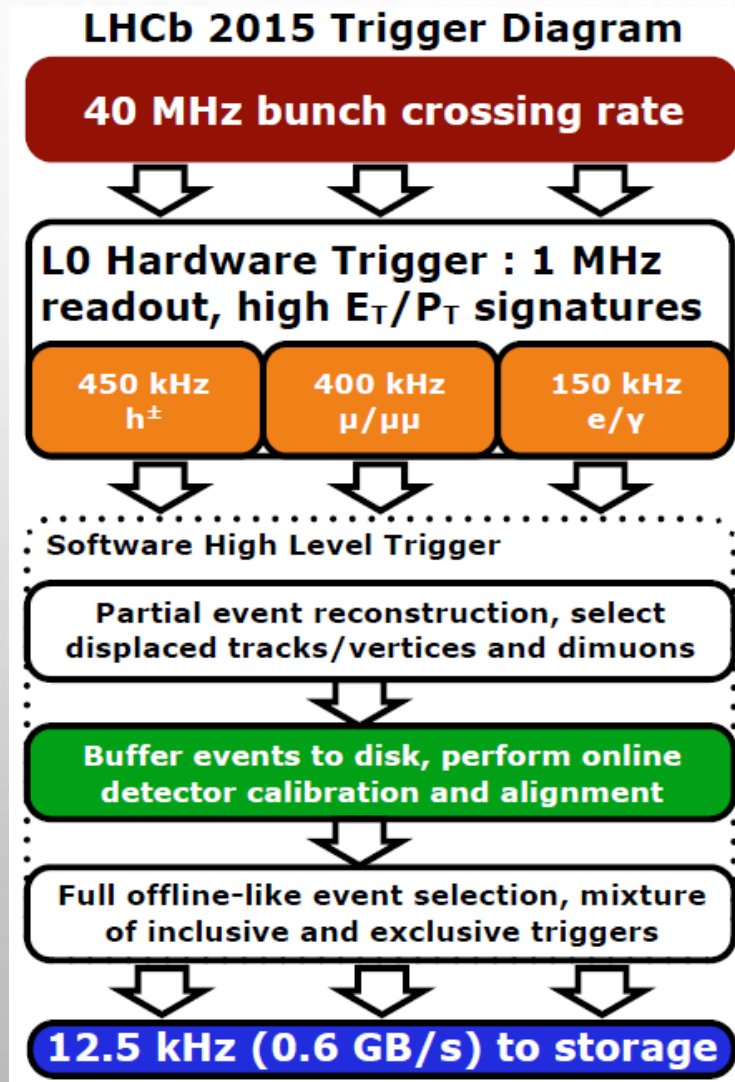
❑ EXCELLENT PERFORMANCE IN RUN 1 AND RUN 2:

- MOMENTUM RESOLUTION $\frac{\Delta p}{p} \sim 0.5\% @20 \text{ [GEV]}$
- IMPACT PARAMETER RESOLUTION $\sim 15 + \frac{29}{p_T} [\mu\text{m}]$
- TIME RESOLUTION $\sigma_t \sim 45 \text{ [FS]}$ FOR $B_s \rightarrow J/\psi\phi$

❑ IN TIME, THE PHYSICS PROGRAMME HAS BEEN EXTENDED TO COVER EXCLUSIVE PROCESSES, QCD STUDIES, ELECTRO-WEAK PHYSICS, DIRECT NP SEARCHES AND HEAVY ION PHYSICS

Int. J. Mod. Phys. A30 (2015)
1530022

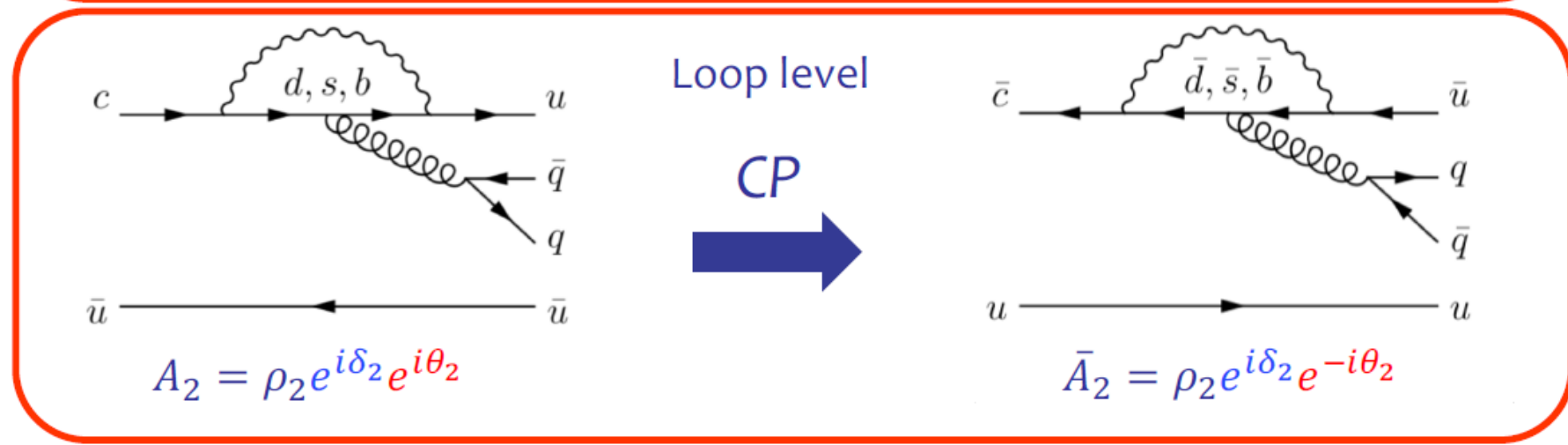
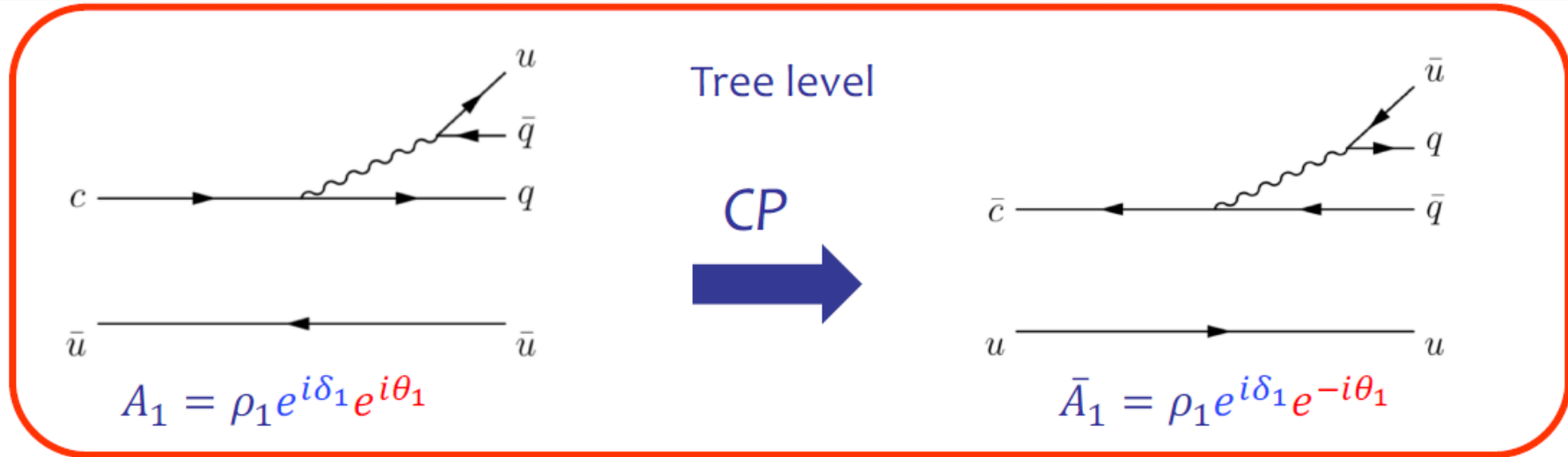




Trigger was continuously improved during Run 1-2 operation

- **Start of operation:**
Storage bandwidth 5 kHz wrt 2 kHz in the design (additional b/w for charm)
- **2012:** Deferred trigger.
Buffer 20% of bandwidth before HLT to disks (use interfill time)
- **Run 2 (2015-2018):** Split HLT.
 - Buffer all HLT1 output to disk.
 - Run calibration and alignment.
 - Offline-quality selections at the last stage of HLT.
 - Can run analyses on HLT2 output (Turbo stream)

FIRST CPV OBSERVATION IN CHARM SECTOR



$$|\bar{A}_1 + \bar{A}_2|^2 - |A_1 + A_2|^2 = 4\rho_1\rho_2 \sin(\theta_1 - \theta_2) \sin(\delta_1 - \delta_2)$$

CP asymmetry is defined as

$$A_{CP}(f) = \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow f)}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow f)} \quad \text{with } f = K^-K^+ \text{ and } f = \pi^-\pi^+$$

The flavour of the initial state (D^0 or \bar{D}^0) is tagged by the charge of the slow pion from $D^{*\pm} \rightarrow D^0\pi^+$ or muon from $B \rightarrow D^0(\rightarrow f)\mu^-X$

The raw asymmetry for tagged D^0 decays to a final state f is given by

$$A_{\text{raw}}(f) = \frac{N(D^0 \rightarrow f) - N(\bar{D}^0 \rightarrow f)}{N(D^0 \rightarrow f) + N(\bar{D}^0 \rightarrow f)}$$

$$\Delta A_{CP} \equiv A_{raw}(KK) - A_{raw}(\pi\pi) = A_{CP}(KK) - A_{CP}(\pi\pi)$$

$$\Delta A_{CP} \equiv A_{CP}(D^0 \rightarrow K^- K^+) - A_{CP}(D^0 \rightarrow \pi^- \pi^+) = (-15.4 \pm 2.9) \times 10^{-4}$$

5.3 standard deviations from zero

This is the first **observation** of CP violation in the decay of **charm** hadrons

DIRECTION BARYONS!!

- ❑ So far it seems that mesons are the champions of the CPV searches, but what about baryons? There are a lot of potential there.
- ❑ A lot of interest and hope related with Λ_b (Nature Physics 13 (2017) 391), indications for CPV with Run 1 data, but no confirmation with the larger sample
- ❑ Large samples of charm baryons collected during Run 2, first attempt to measure the ΔA_{CP}^{Baryon} with Λ_c^+

$$\Delta A_{CP}^{baryon} \equiv A_{CP}(\Lambda_c^+ \rightarrow pK^-K^+) - A_{CP}(\Lambda_c^+ \rightarrow p\pi^-\pi^+) = (0.30 \pm 0.91 \pm 0.61)\%$$

- ❑ No luck there..., how about another interesting state... Ξ_c^+ ?

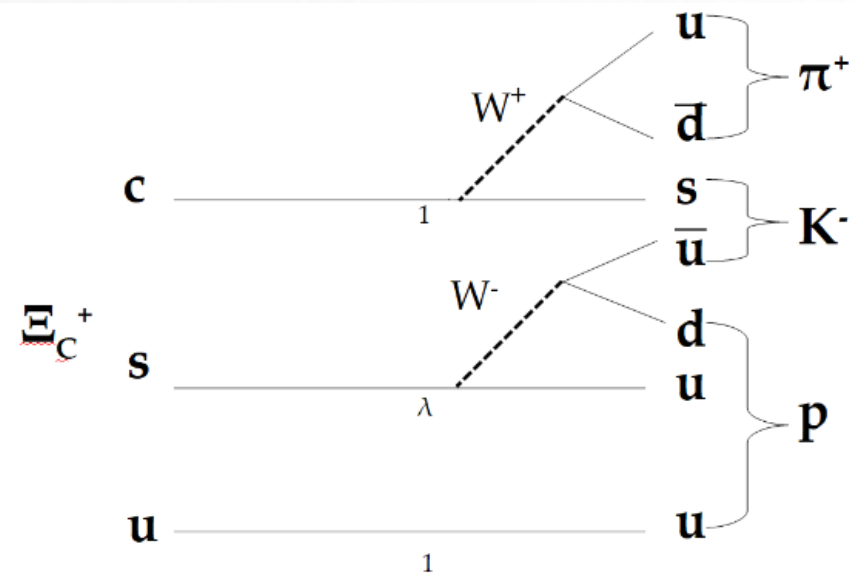
STUDIES OF PROMPT Ξ_C^+ DECAYS

- ❑ Run 1 data (2010 – 2012) of prompt $\Xi_C^+ \rightarrow pK^- \pi^+$ decays has been started by the Warsaw group, Krakow joined in 2018
- ❑ Two model independent techniques were used S_{CP} and KNN to measure the CP violation
- ❑ No luck so far: Paper-2019-026 ([The Eur. Phys. Journal C 80, 986 \(2020\)](#))
- ❑ We may face two problems here: either the CPV is very small (for $\Xi_C^+ \rightarrow pK^- \pi^+$ decays we expect the CPV at the level of $10^{-3} - 10^{-4}$), or our methods are not sensitive enough
- ❑ In Run 2 analysis we are testing, for the first time, KDE approach to enhance the binned S_{CP} method and to use the energy test also supported by KDE estimator
- ❑ Currently involved: Artur Ukleja (Warsaw NCBJ), Jakub Ryzka, TS (AGH)

STUDIES OF PROMPT Ξ_c^+ DECAYS

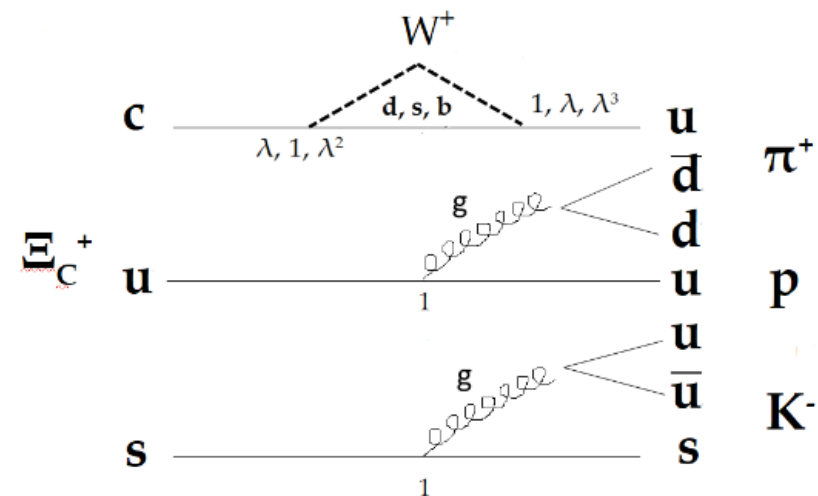
- Note! All that follows from this point forth is **LHCb PRELIMINARY!**
- The work was presented at Charm working group meeting and we are in process of writing the analysis note (which will turn into paper at some point)

STUDIES OF PROMPT Ξ_C^+ DECAYS – DIAGRAMS

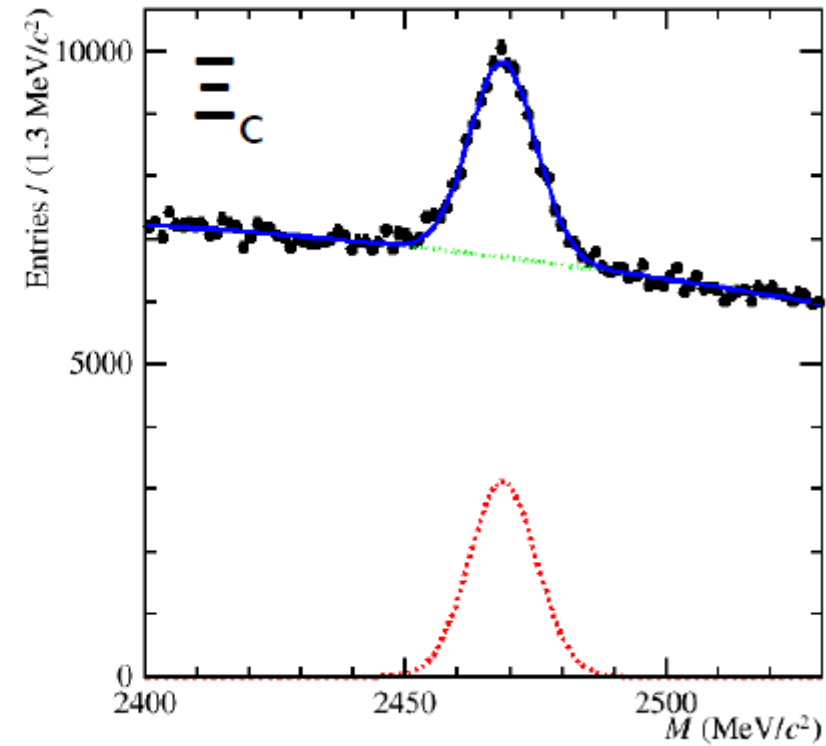
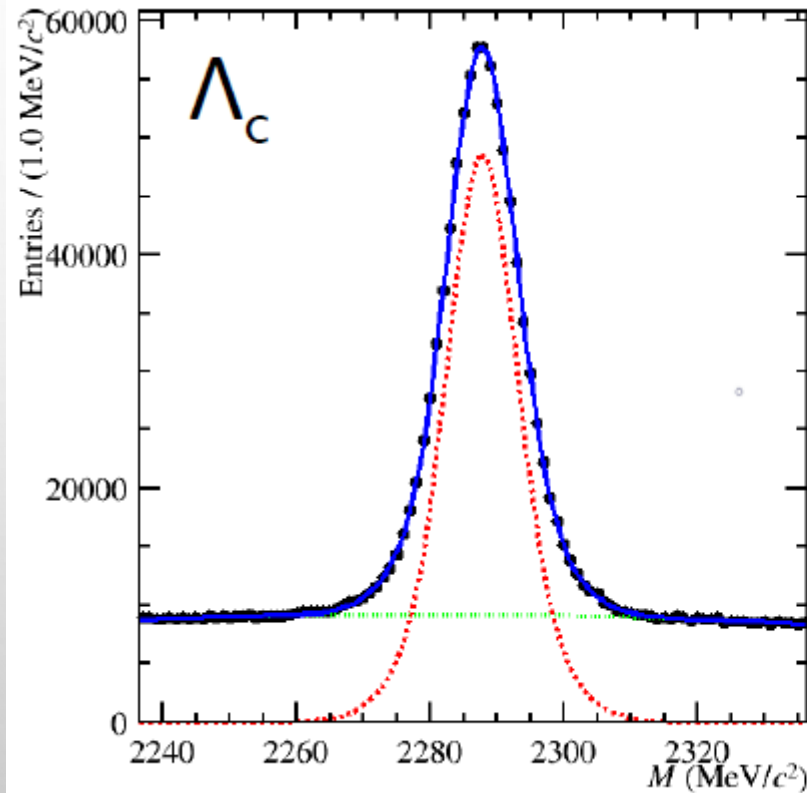


$$A_T \sim \lambda T$$

$$P \sim \lambda P_d + \lambda P_s + \lambda^5 P_b$$



$$FoM = \frac{S}{\sqrt{S+B}}$$

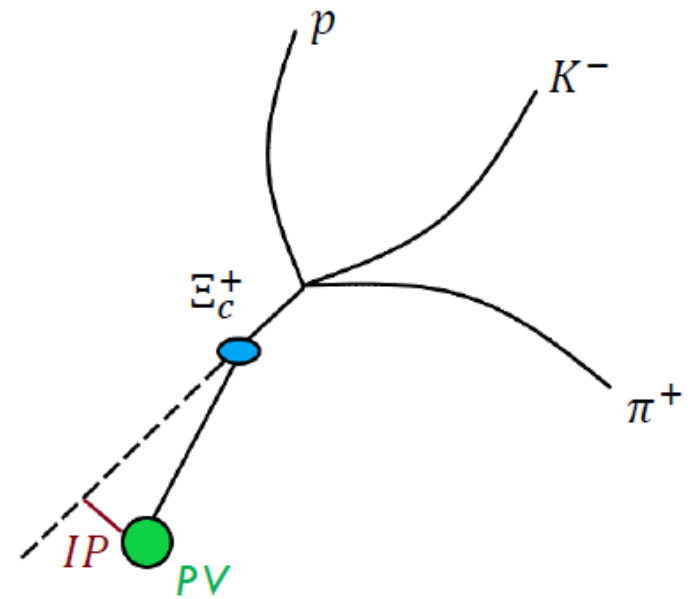


Signal: $f(x) = \text{sig1frac} \cdot G(x, \mu, \sigma_1) + (1 - \text{sig1frac}) \cdot G(x, \mu, \sigma_2)$

Background: $p_0 + p_1 x$

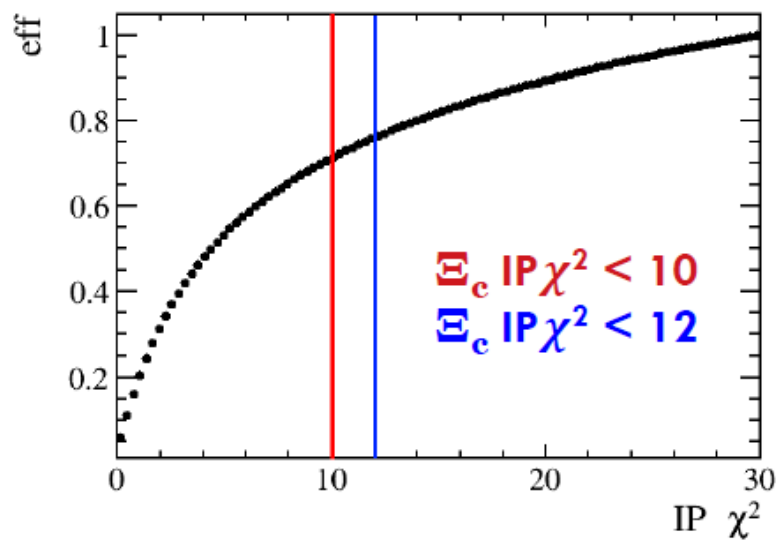
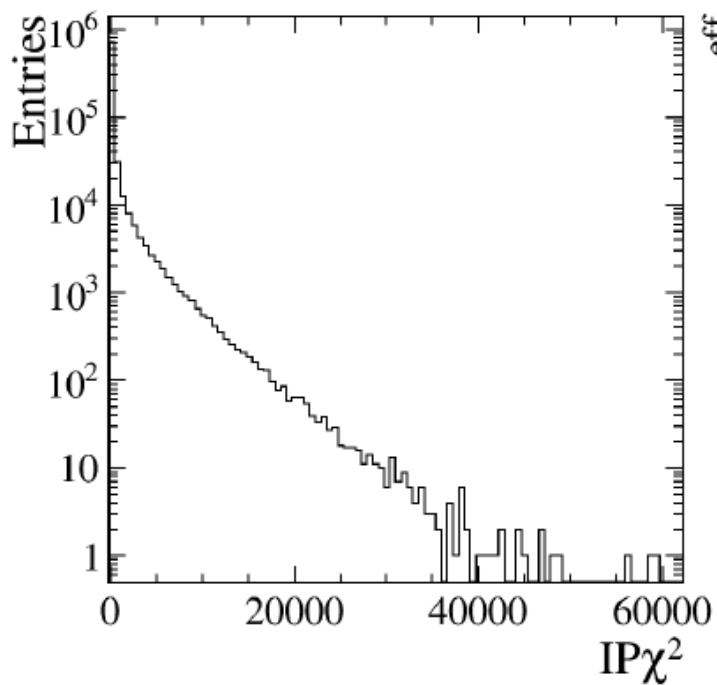
Cuts were implemented for the following variables:

- Proton/Kaon/Pion
 - PID
 - ProbNN
 - $IP\chi^2$
 - TRACK_GhostProb
 - momentum
- Charm baryon
 - Vertex $\chi^2/ndof$
 - $IP\chi^2$
 - Transverse momentum
 - DIRA
 - $FD\chi^2$
 - Pseudorapidity η

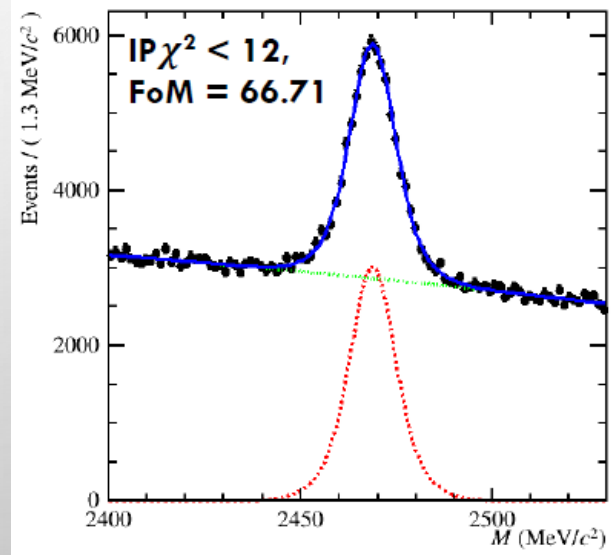
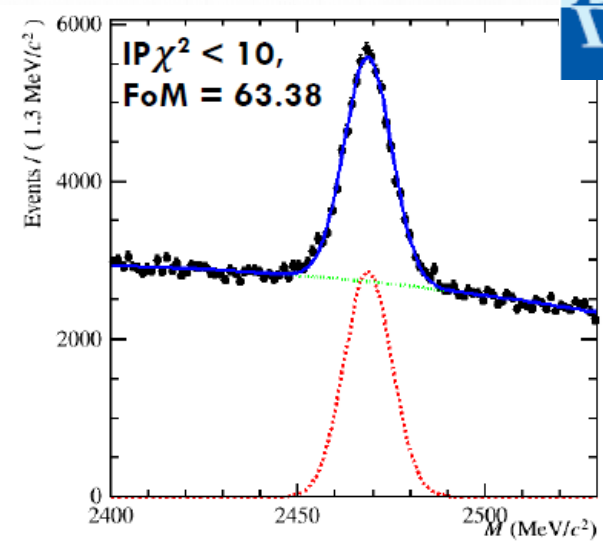


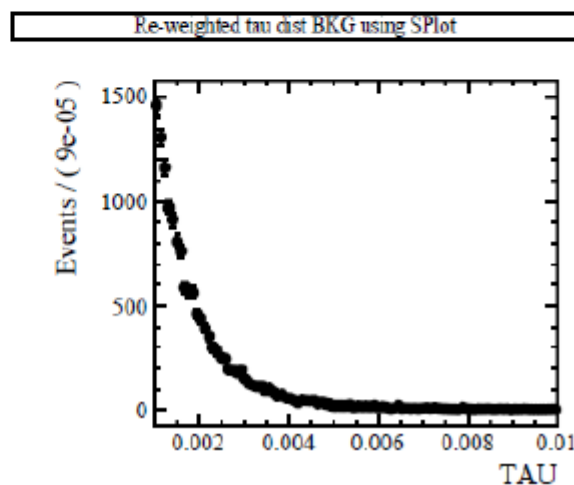
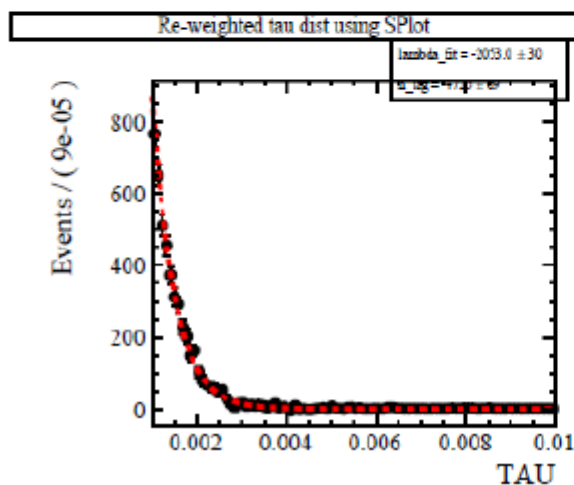
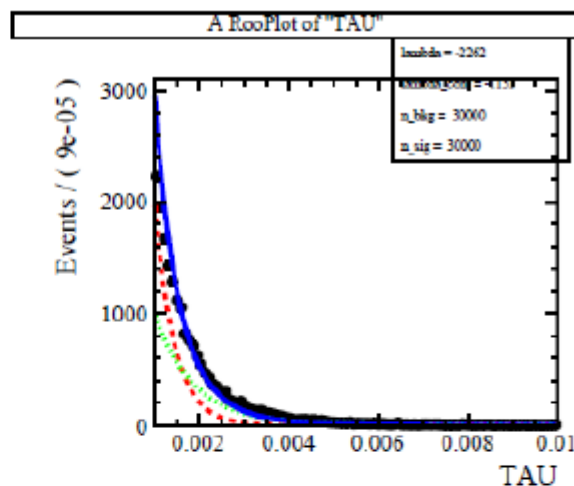
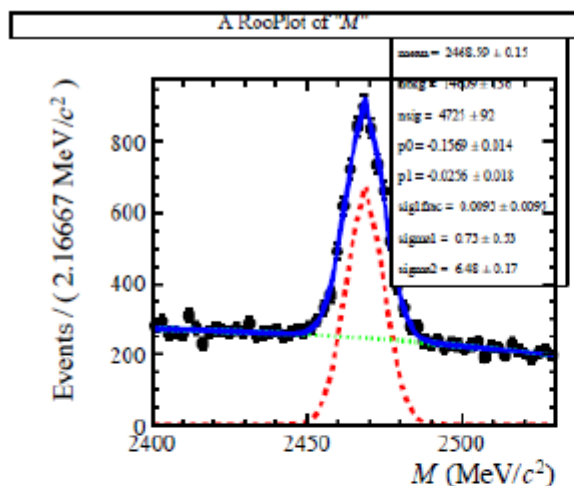
FINAL SELECTION ALGORITHM

Different cuts are considered: $IP\chi^2 < 10$, $IP\chi^2 < 12$



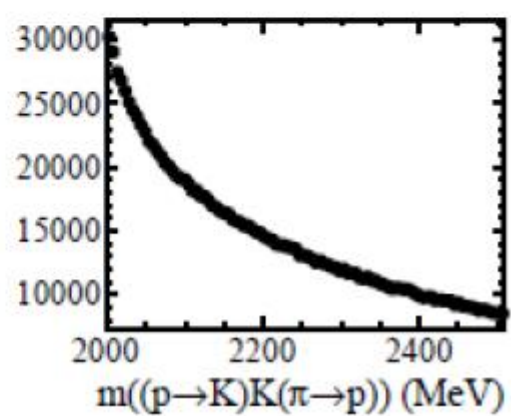
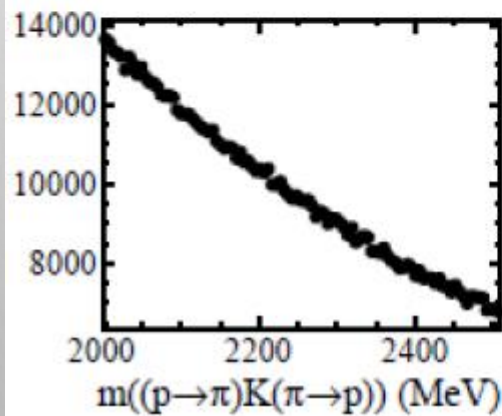
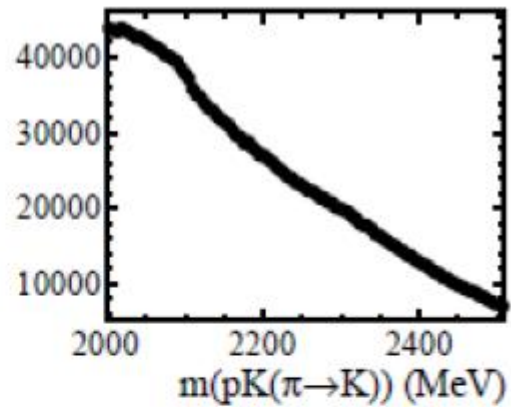
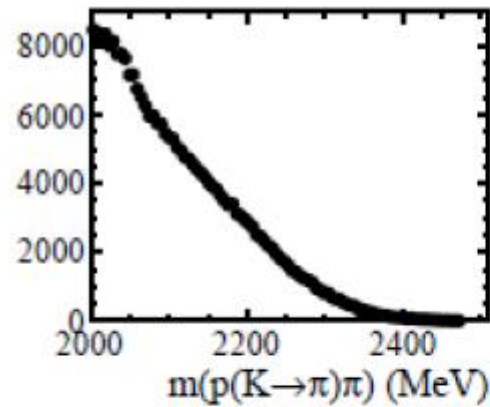
$$Eff = \frac{\#entries\ left\ after\ cut}{\#all\ entries}$$





- sPlot technique is also used to determine lifetime of Ξ_c
- $\tau = 0.487 \pm 0.007$ ps
- Contamination from other decays seems to be negligible

CROSS-CHECKS – WRONG MASS HYP

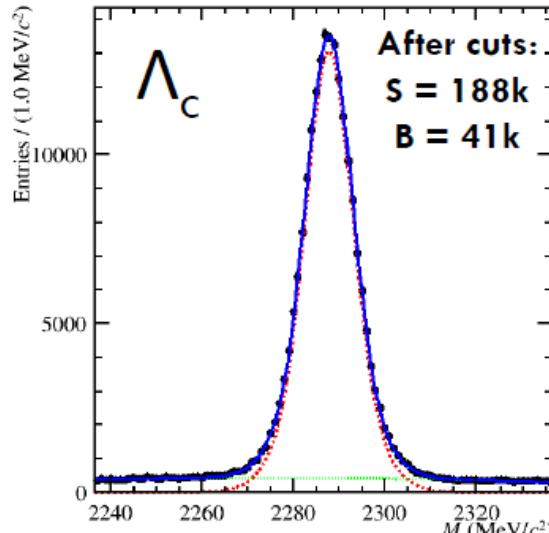
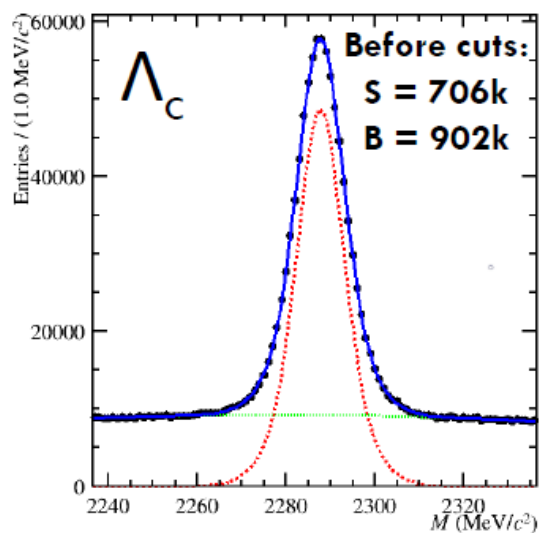
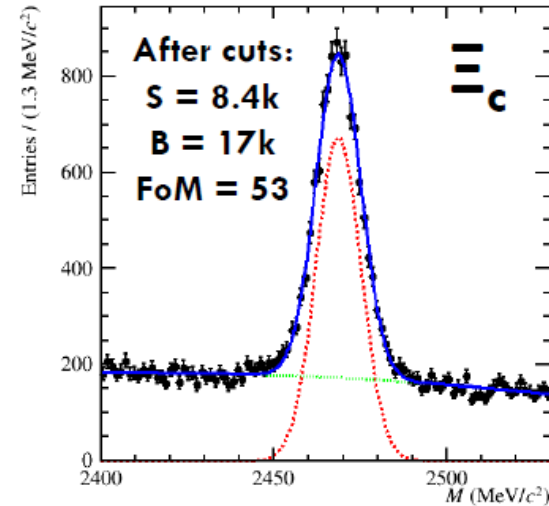
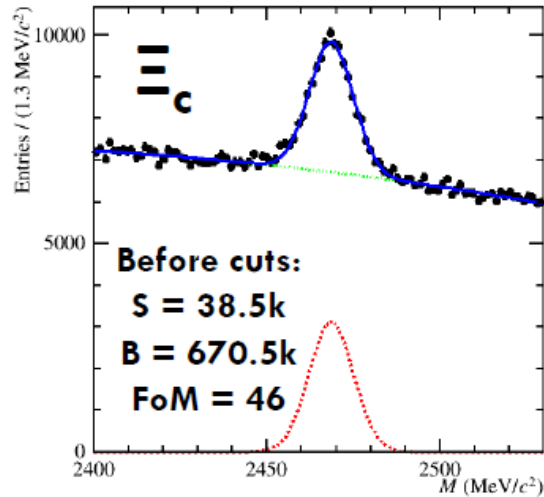


False particle identification is investigated as additional cross-check

- $K \rightarrow \pi$
- $\pi \rightarrow K$...
- 7 combinations
- $\sim 1\%$ of data
- 3 mass ranges for better visibility
 - (1200, 1800) MeV
 - (1800, 2000) MeV
 - (2000, 2500) MeV

No mass peaks from the other decays: D , D_s , Λ_b etc.

EVENT YIELDS – FINAL SELECTION

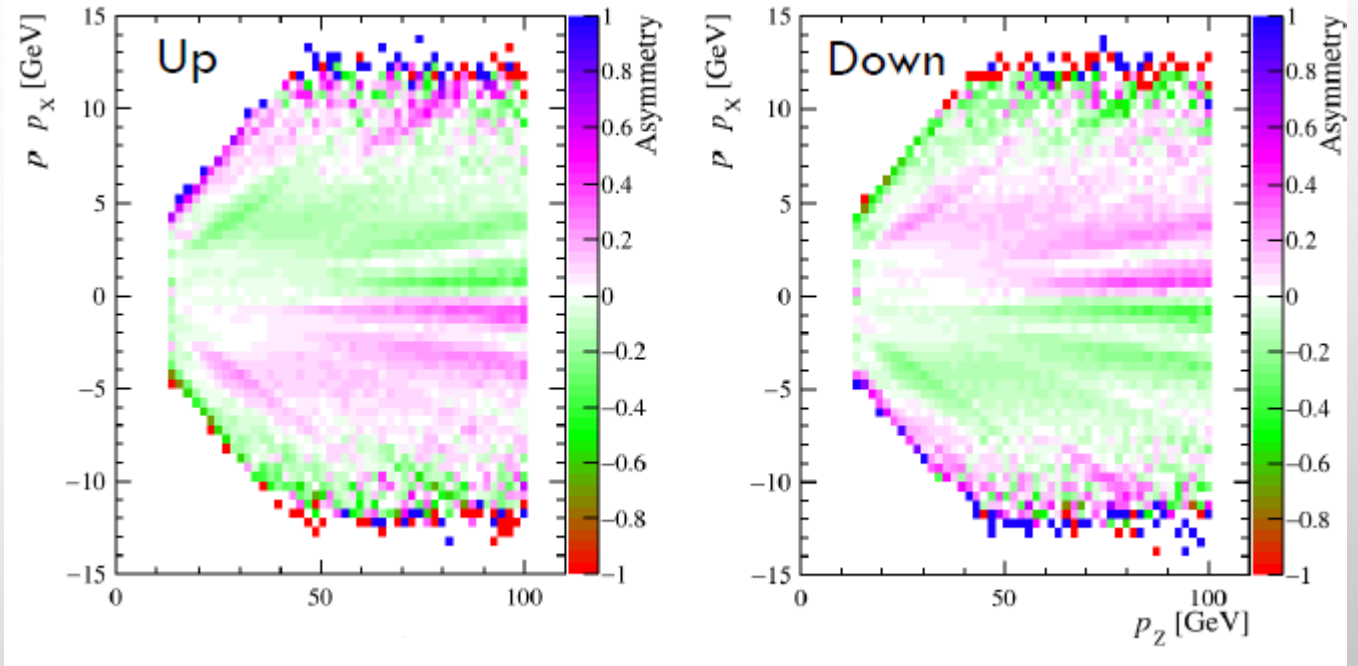


2018	Before offline cuts	After SC (including bkg)
Λ_c	~ 170 mln	~ 20 mln
Ξ_c	~10 mln	~ 4,5 mln

- ❑ Note, this is fully blinded analysis, only ~1% of the data sample used in tests and cut optimisation
- ❑ This is necessary to tune fiducial cuts that take into account the boundary detector effects
- ❑ Close to impossible to get it from MC or the control channel
- ❑ The control channel used for testing the biases in CPV estimation

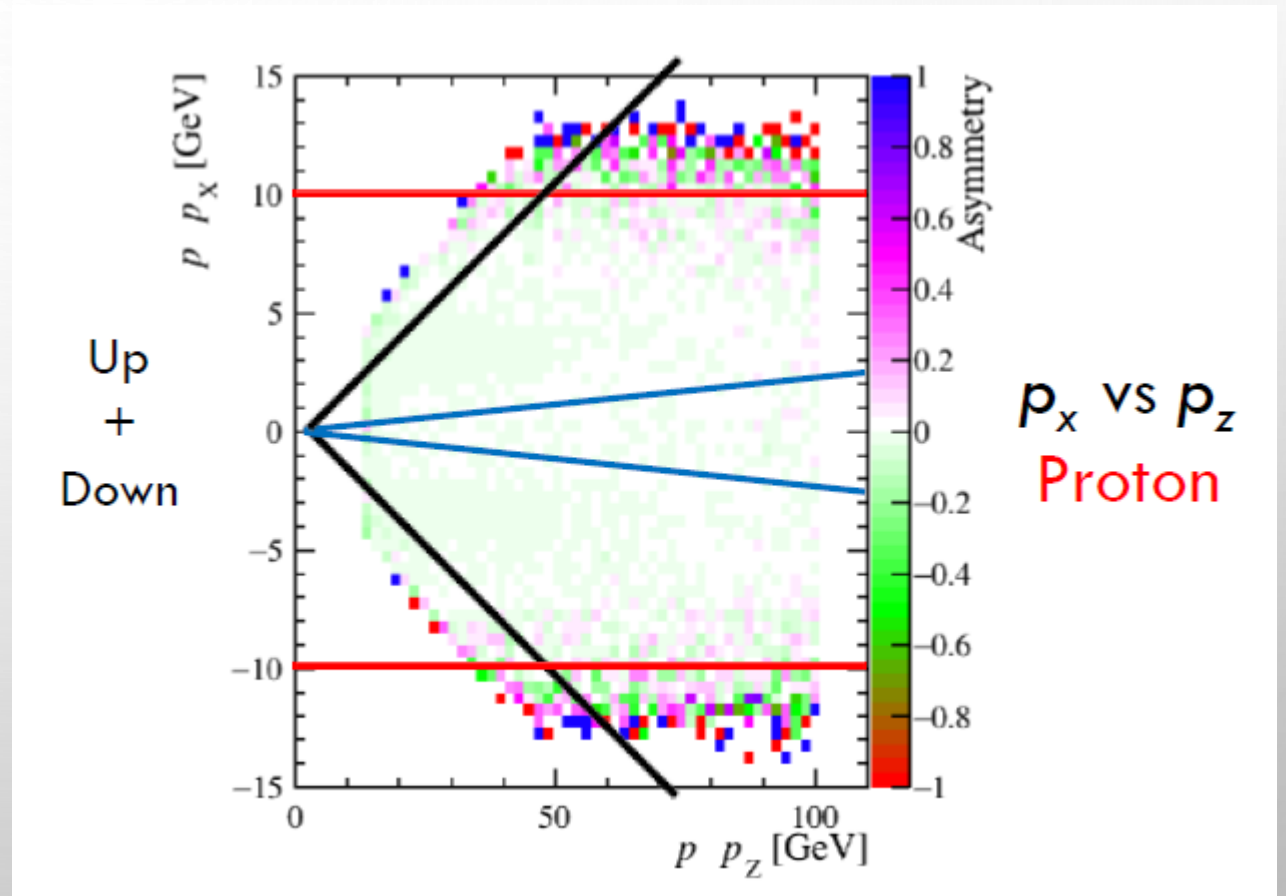
- Geometry of the detector can be not uniform
- Whole data sample
- Detection asymmetries expected in external regions and close to the beam axis
- Asymmetry in PX and PZ

$$Asymmetry = \frac{N_+ - N_-}{N_+ + N_-}$$

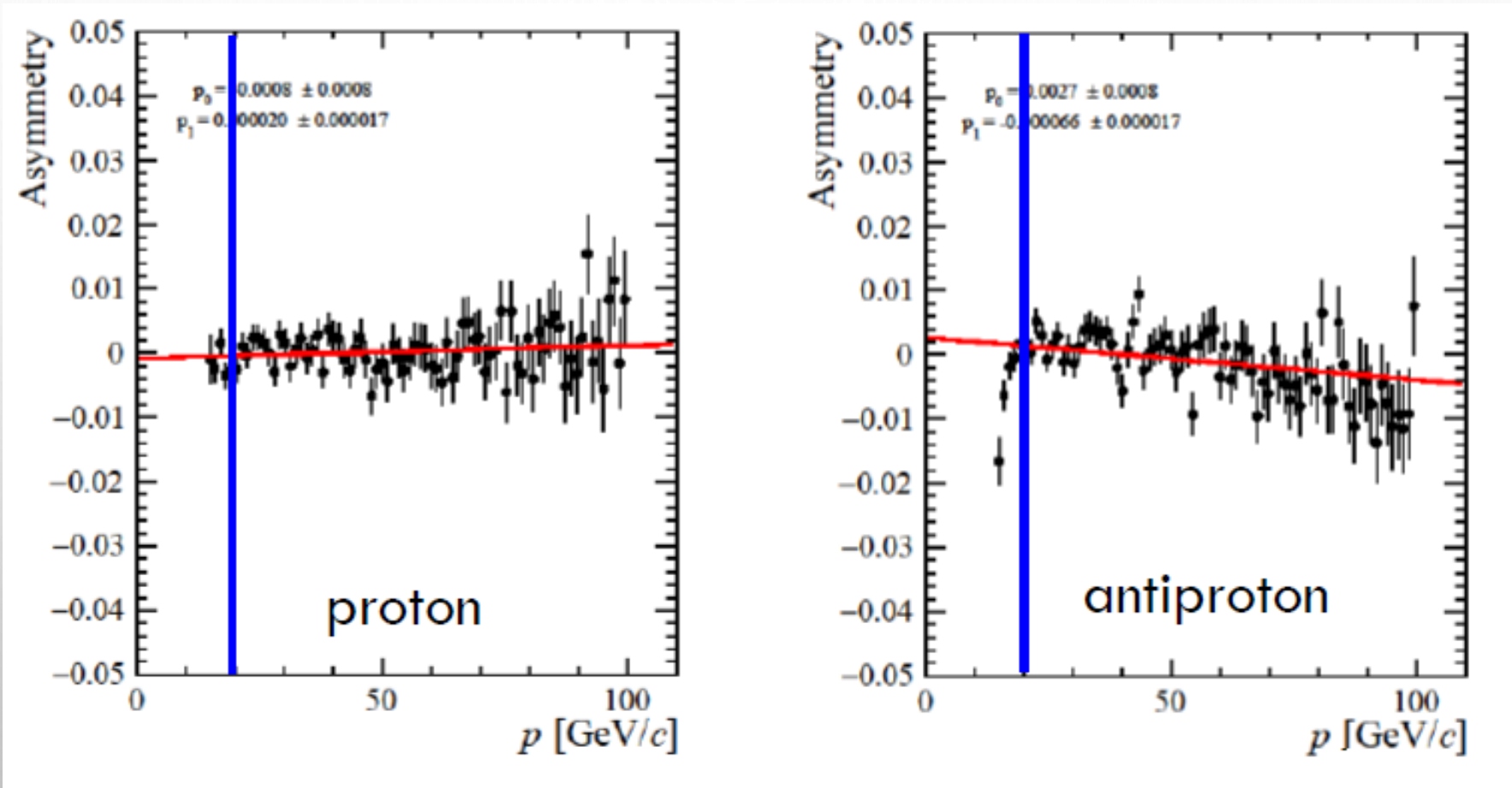


- Geometry of the detector can be not uniform
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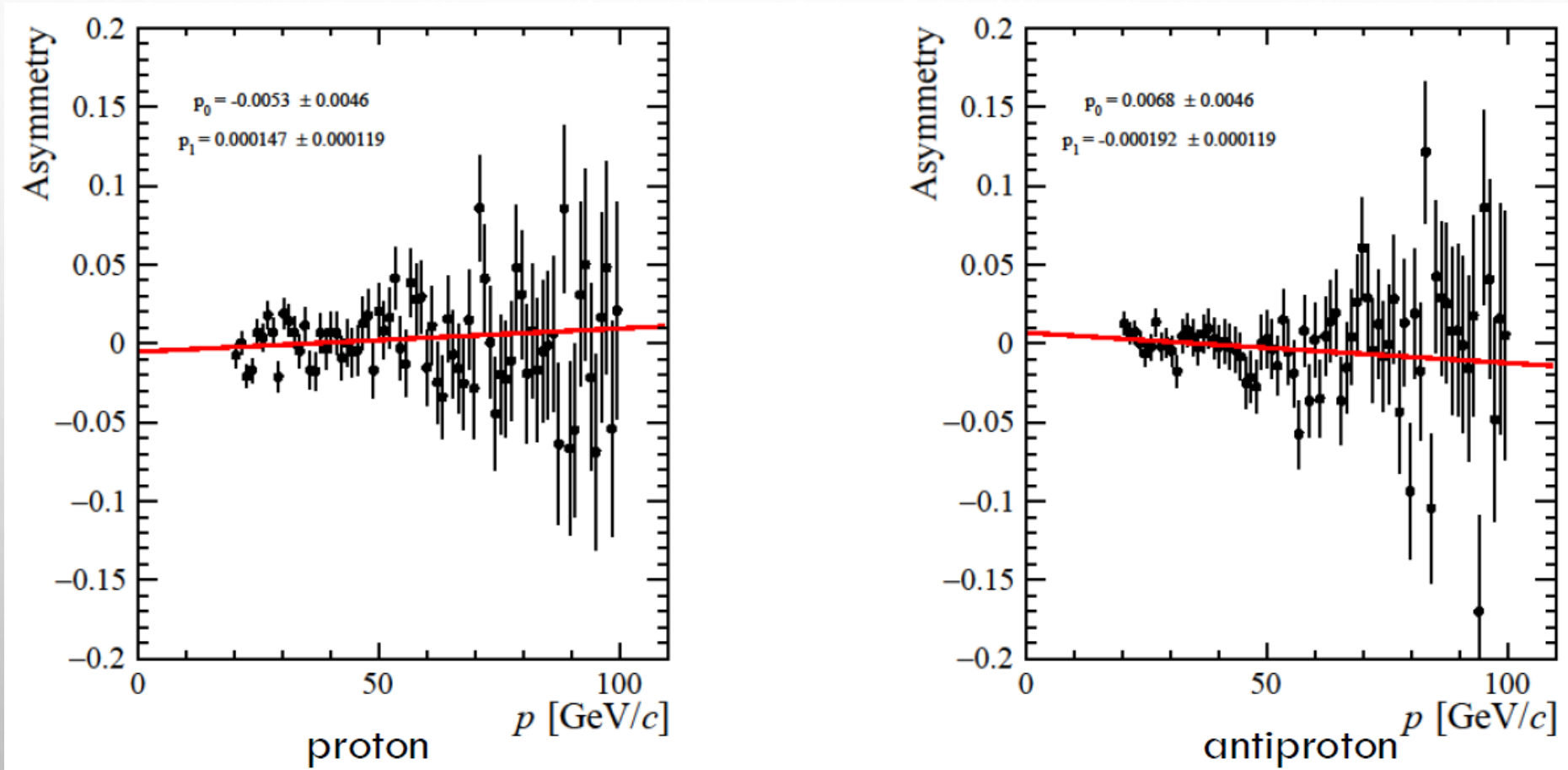
$$Asymmetry = \frac{N_+ - N_-}{N_+ + N_-}$$



EVENT YIELDS – TRACKING EFFECTS



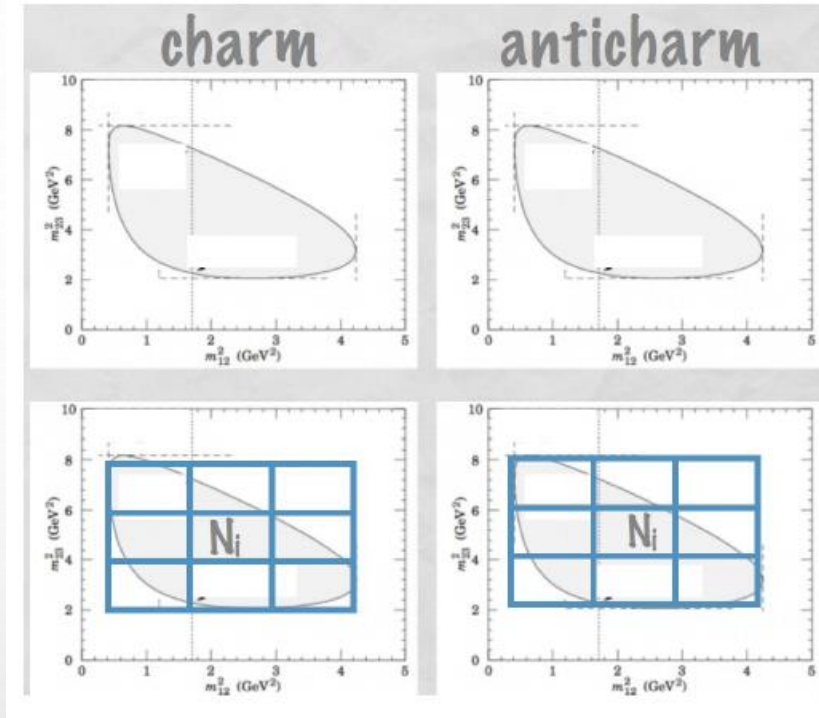
EVENT YIELDS – TRACKING EFFECTS



- This method is well-known and commonly used in many analyses:
- The method is based on dividing the phase space into n bins. For each bin, comparison between Dalitz plots for particles and antiparticles is performed.
- Significance of the difference between number of particles (N^+) and antiparticles (N^-) is computed, using the following expression:

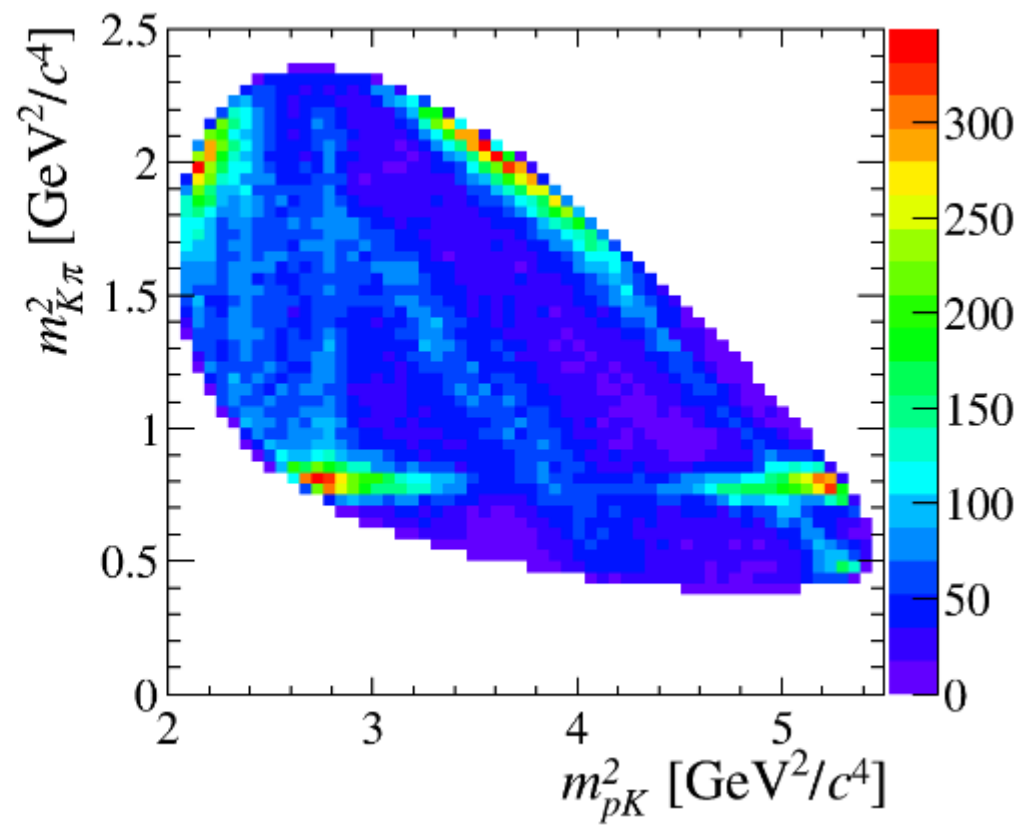
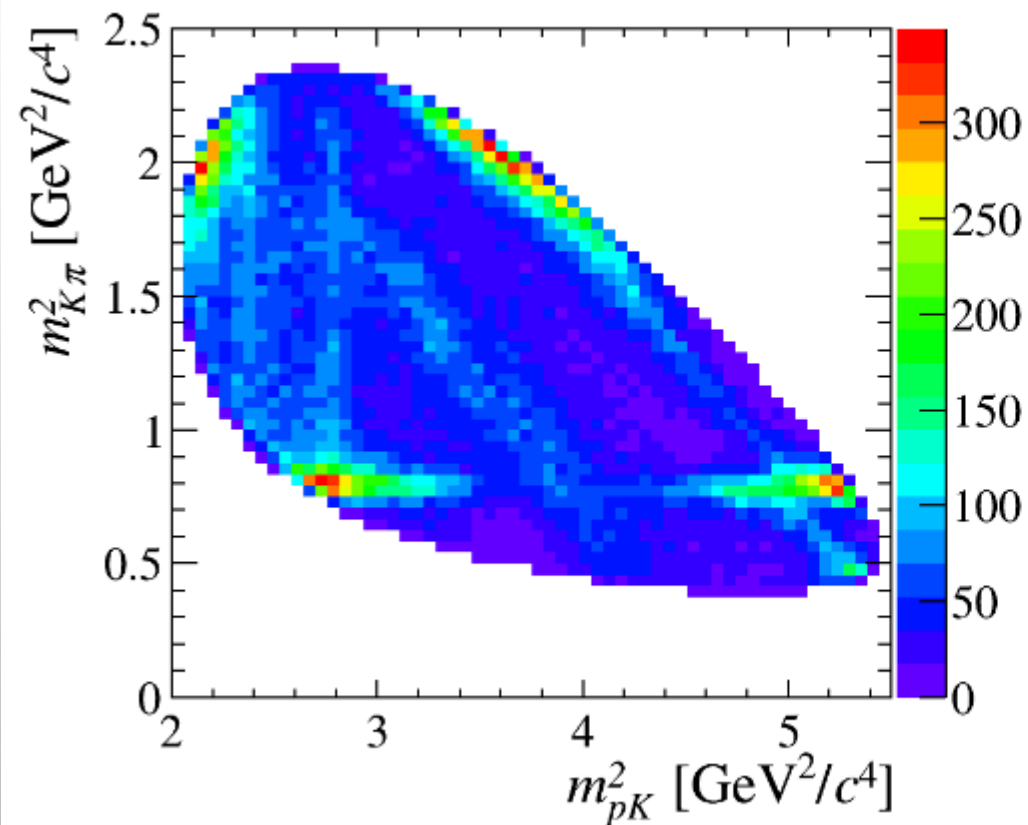
$$S_{CP}^i = \frac{N_i^+ - \alpha N_i^-}{\sqrt{\alpha(N_i^+ + N_i^-)}}$$

where $\alpha = N^+/N^-$ accounts for global asymmetries

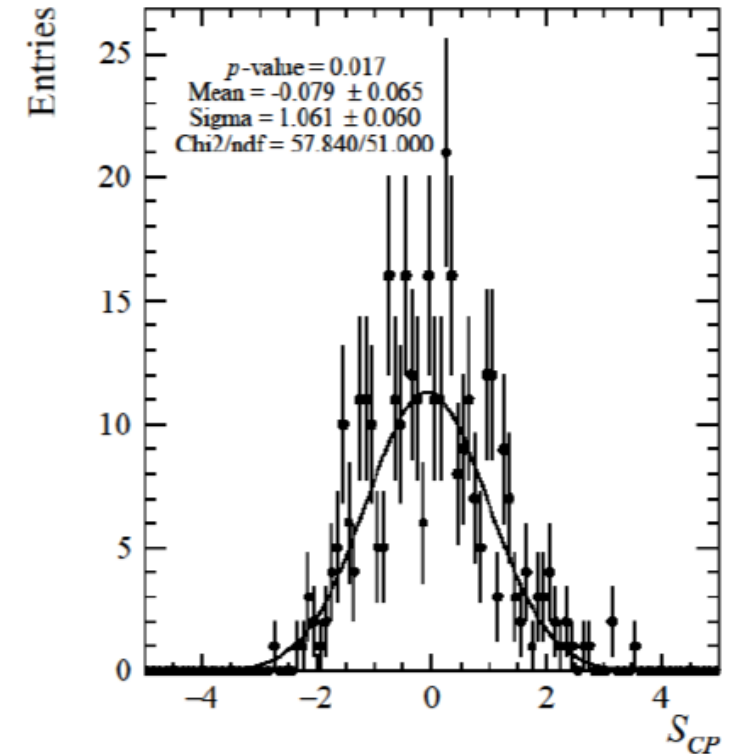
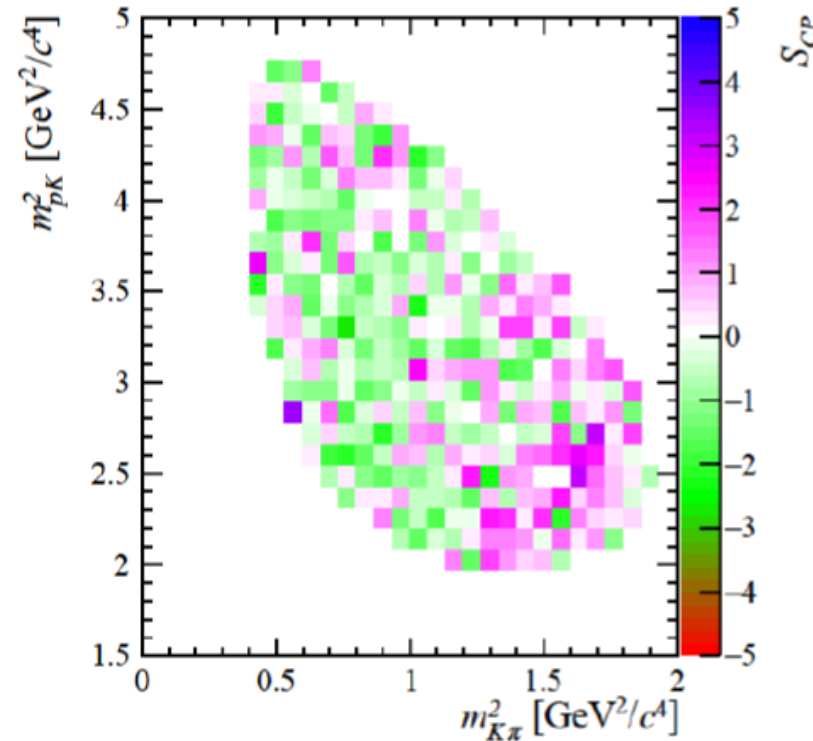


- Without local asymmetries S_{CP} is Gaussian distribution with $\mu = 0$ and $\sigma = 1$.
- Calculating a $\chi^2/ndf = \sum_i (S_{CP}^i)^2 / (nbins - 1)$
- Measuring **p-value**
- **p-value $\ll 1$ in case of CPV**

DALITZ PLOTS FOR 2018 (CONTROL CHANNEL)



- Example with 52 bins
- p -value = 1.7%
- If still there are any pollution asymmetry, it is below method sensitivity
- Result is in agreement with no observation of CPV – as expected 😊



- Kernel Density Estimation is a non-parametric way to estimate the probability density function f of a random variable.

$$f(\hat{x}) = \frac{1}{n} \sum_{i=1}^n \omega(x - x_i, h)$$

where:

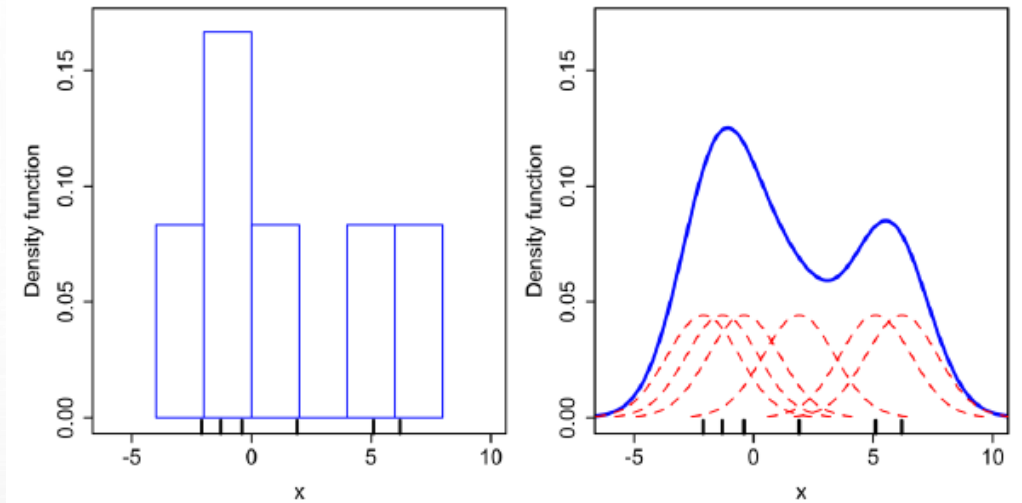
$$\omega(t, h) = \frac{1}{h} K\left(\frac{t}{h}\right)$$

is weighting function.

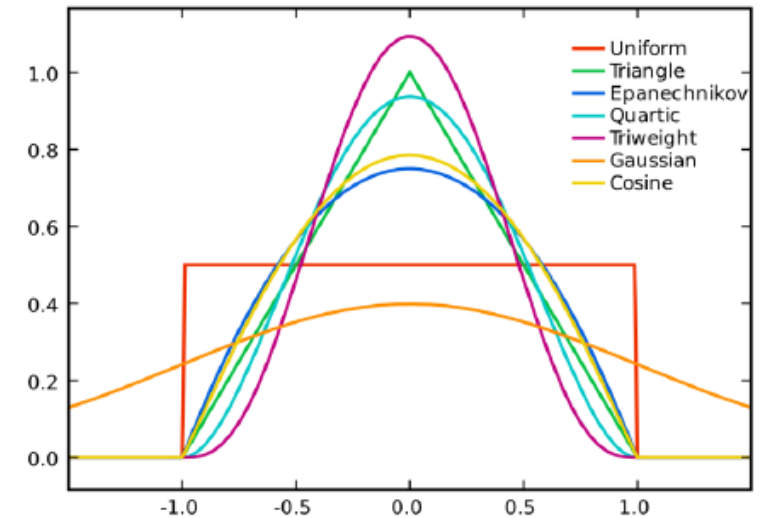
- K is the kernel, which determines the shape of the weighting function and h is the smoothing parameter.
- In this analysis I use **triangle kernel**:

$$\omega(t, h) = \begin{cases} \frac{1}{h} \left(1 - \frac{|t|}{h}\right) & \text{for } |t| < h \\ 0 & \text{otherwise} \end{cases}$$

KDE method was tested in $K^* \mu\mu$ decays [CERN-THESIS-2010-186]

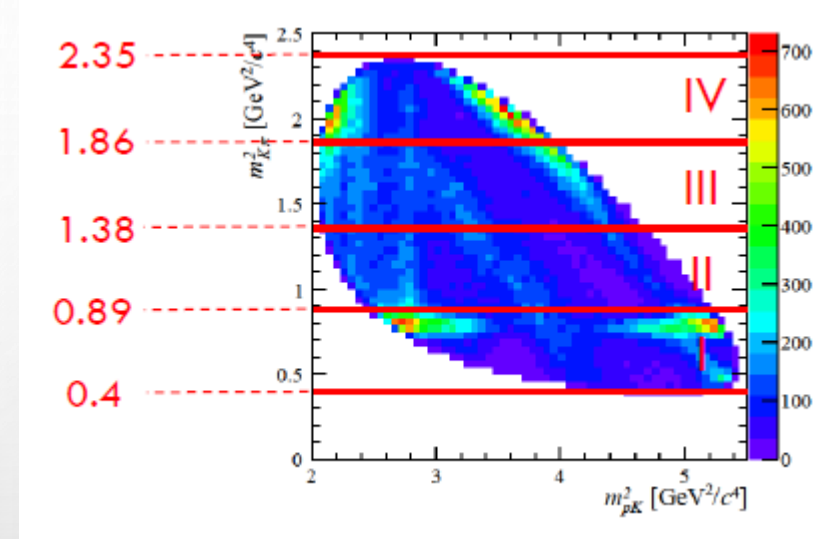
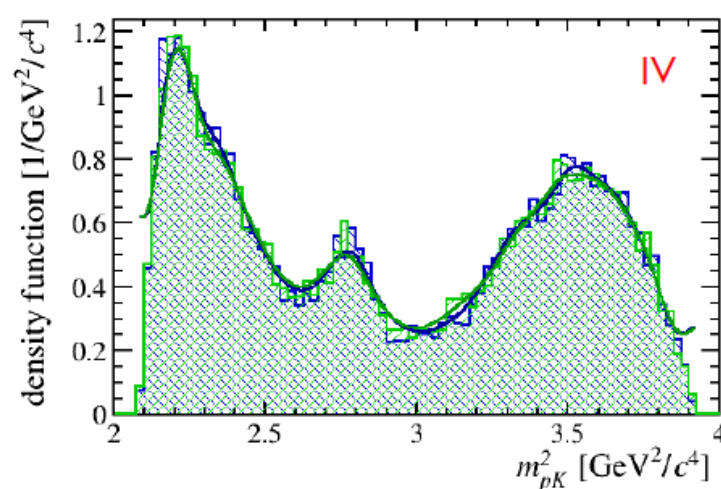
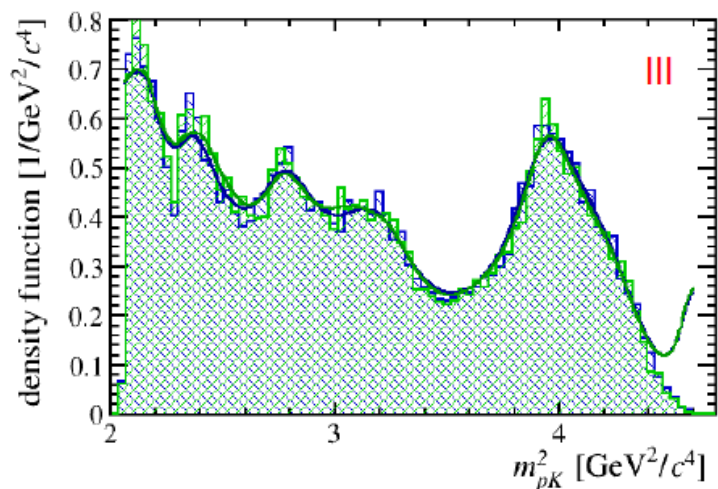
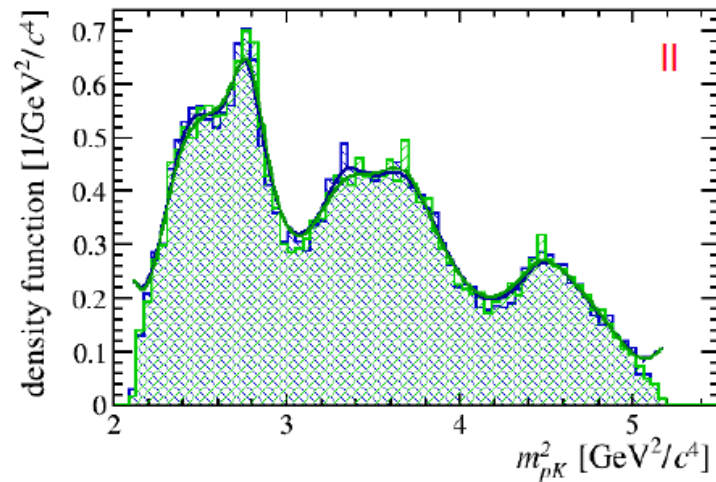
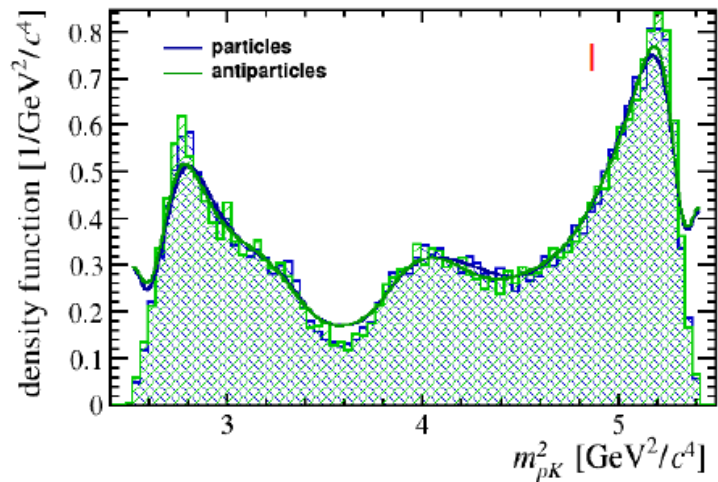


KDE example with Gaussian Kernel

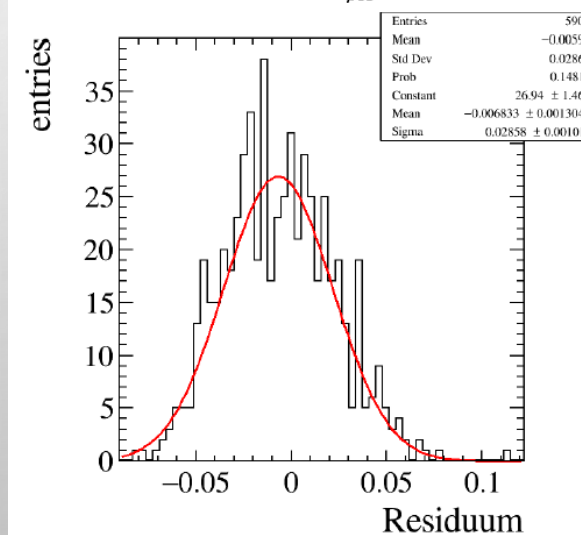
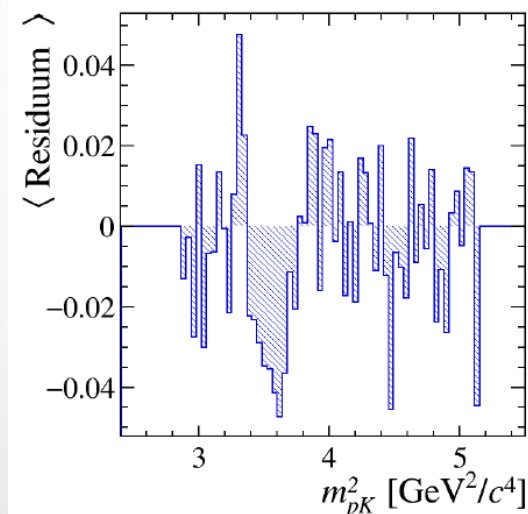
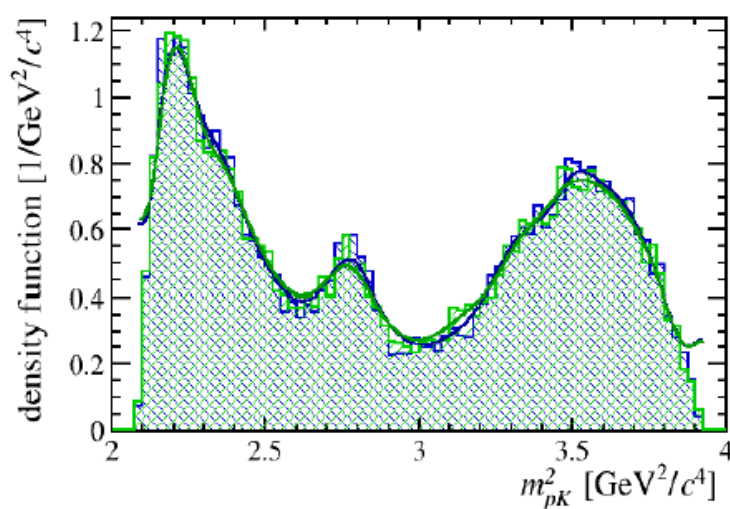
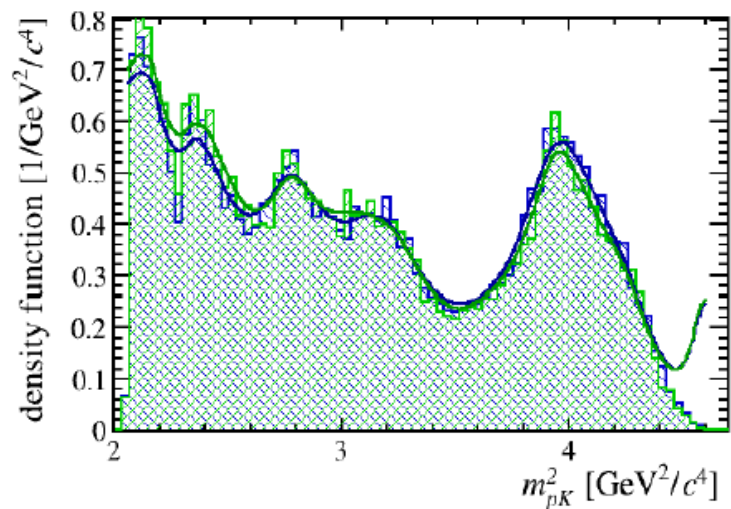
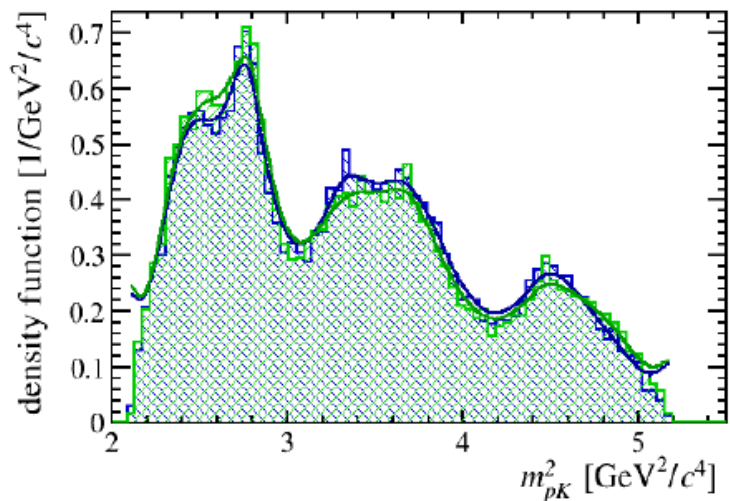
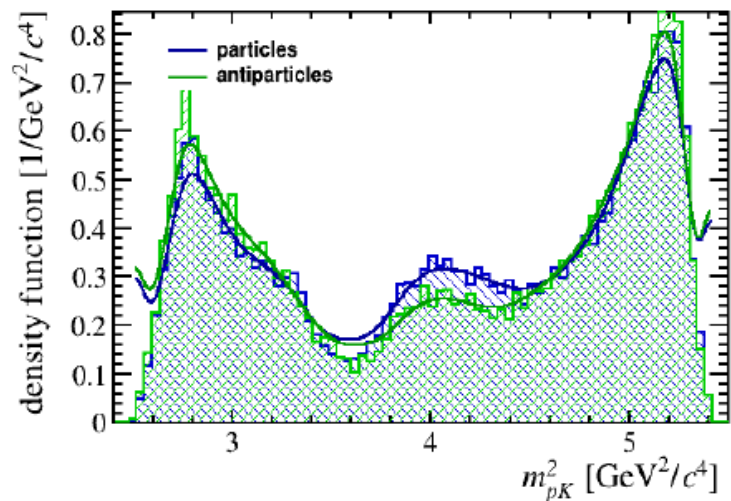


Commonly used kernels

KDE APPROACH – NO CPV SAMPLE



KDE APPROACH – CPV SAMPLE (20%)



LOST PROPERTY



"Sorry Doc, we had a load of Anti-Matter around 13 billion years ago, but it got lost when we moved"

SPARES

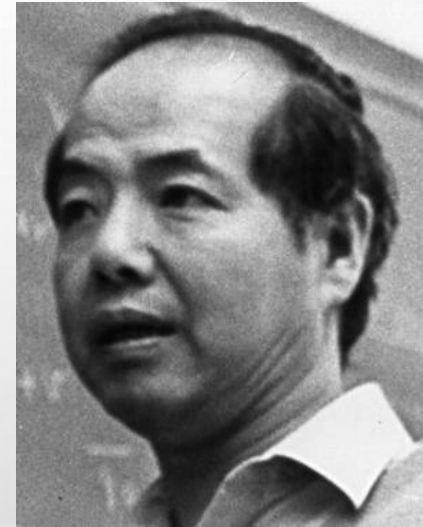
SYMMETRIES...

T.D.Lee:

“The root to all symmetry principles lies in the assumption that it is impossible to observe certain basic quantities; the non-observables”

Four main types:

- **Particle permutations:**
Bose-Einstein's and Fermi-Dirac's statistics
- **Continuous transformations:**
translations, rotations, boosts,...
- **Discrete symmetries:**
space parity, time parity, charge parity
- **Unitary symmetries: gauge invariance**
 U_1 (charge), SU_2 (isospin), SU_3 (color),..



⇒ If we found symmetry that cannot be, even in principle, observed **exact symmetry**

⇒ Otherwise **broken symmetry**

Noether's theorem:

SYMMETRY

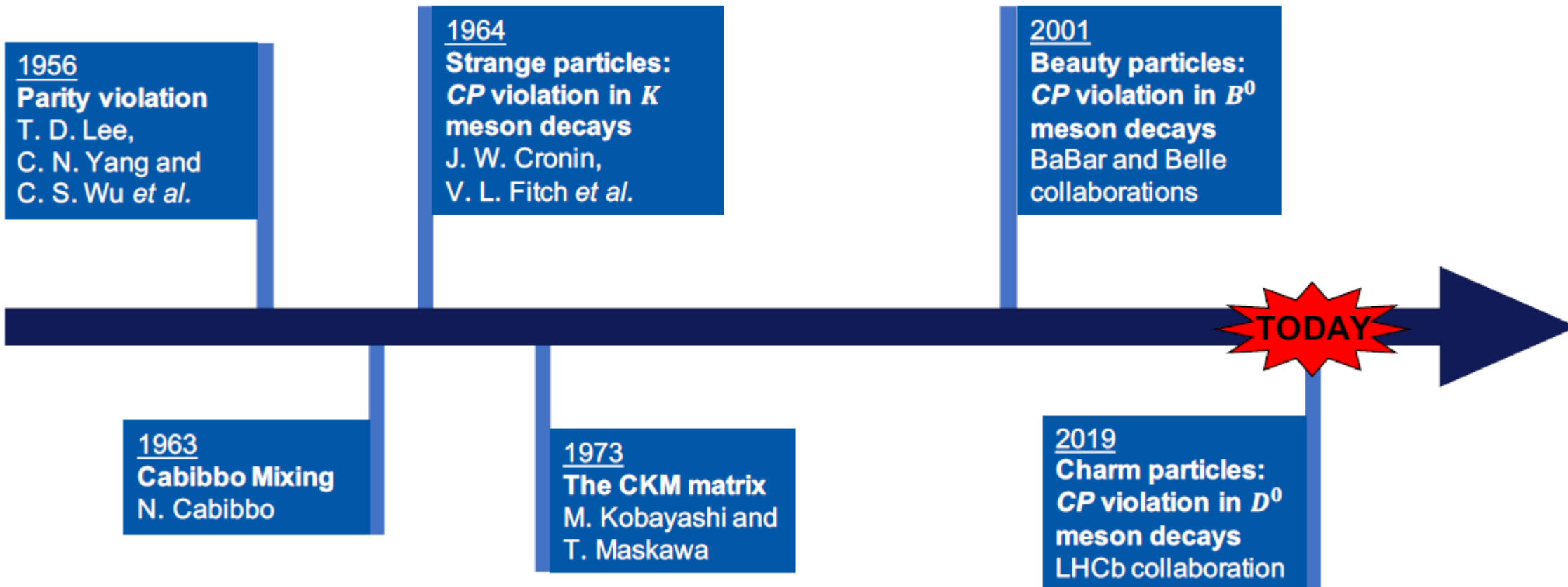


Conservation Law

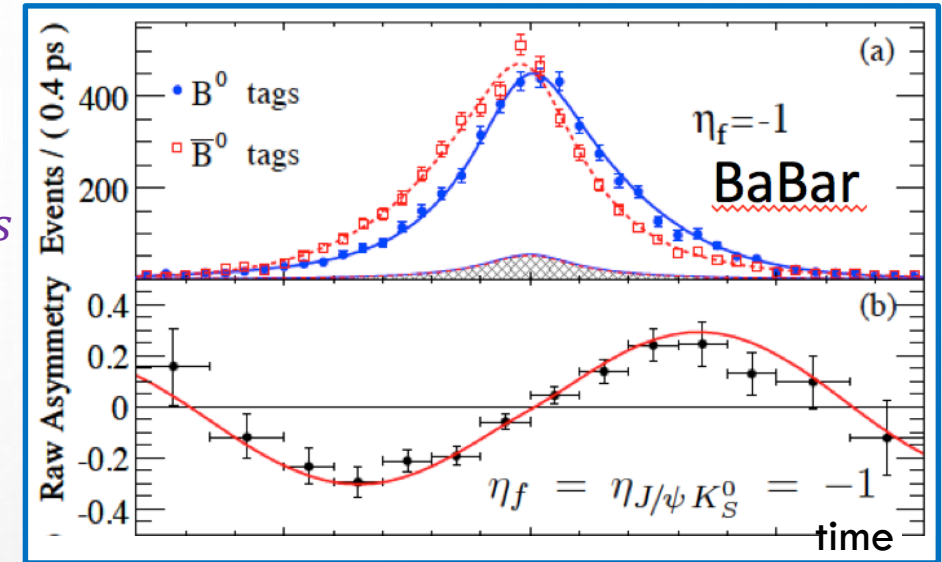
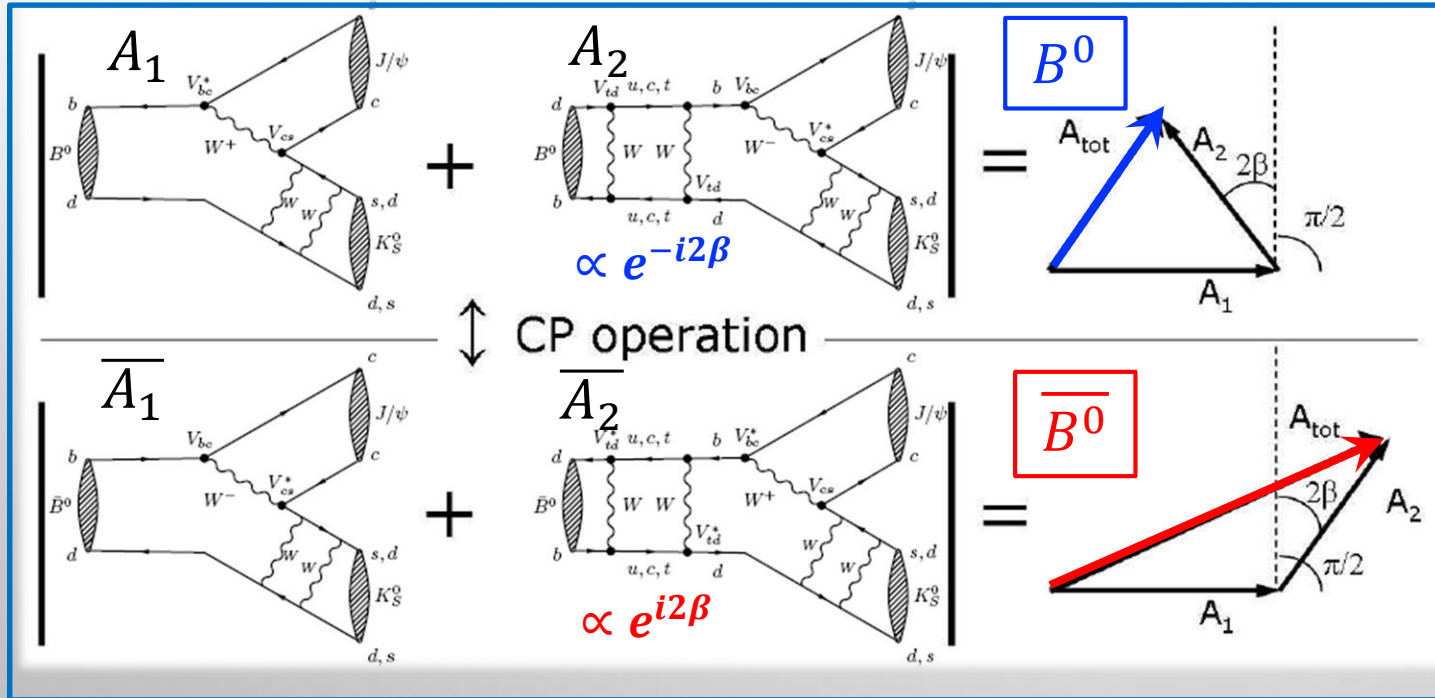


AGH

SHORT HISTORY OF FLAVOUR PHYSICS



- Przejście kwantowe z dwoma amplitudami A_1 i A_2 :
 - Eg.: $A_1 = B^0 \rightarrow J/\psi K_S$ and $A_2 = B^0 \rightarrow \bar{B}^0 \rightarrow J/\psi K_S$



$$|A_1| = |\bar{A}_1|, |A_2| = |\bar{A}_2|,$$

$$\text{but } |A_1 + A_2| \neq |\bar{A}_1 + \bar{A}_2|$$

ŁAMANIE CP : EKSPERYMENT Z „DWOMA SZCZELINAMI”

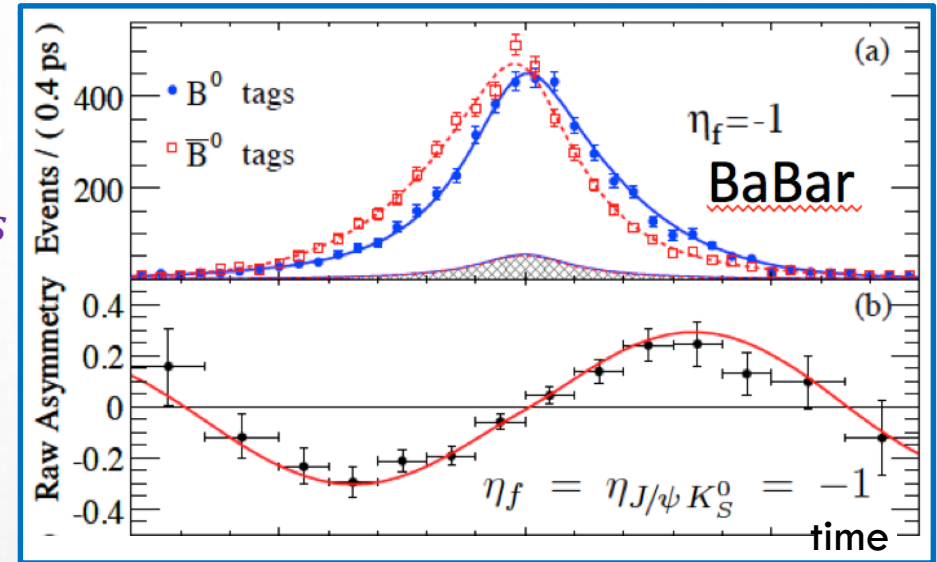
- Przejście kwantowe z dwoma amplitudami A_1 i A_2 :
 - Eg.: $A_1 = B^0 \rightarrow J/\psi K_S$ and $A_2 = B^0 \rightarrow \bar{B}^0 \rightarrow J/\psi K_S$

$$A = A_1 + A_2 e^{i\phi} e^{i\delta} \quad \bar{A} = A_1 + A_2 e^{-i\phi} e^{i\delta}$$

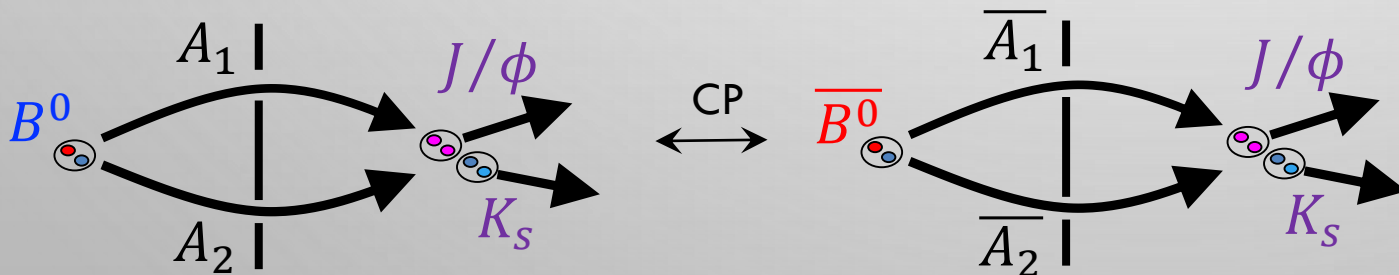
$$|A|^2 = |A_1|^2 + |A_2|^2 + A_1 A_2 (e^{i\phi} e^{i\delta} + e^{-i\phi} e^{-i\delta})$$

$$|\bar{A}|^2 = |A_1|^2 + |A_2|^2 + A_1 A_2 (e^{-i\phi} e^{i\delta} + e^{i\phi} e^{-i\delta})$$

$$|A - \bar{A}|^2 = 4 A_1 A_2 \sin \phi \sin \delta$$



$|A_1| = |\bar{A}_1|$, $|A_2| = |\bar{A}_2|$,
but $|A_1 + A_2| \neq |\bar{A}_1 + \bar{A}_2|$



- Łamanie CP to efektywnie interferencja kwantowo mechaniczna!!

Pożyczony od M. Merk (LHCb)

Non-observables	Symmetry Transformations	Conservation Laws or Selection Rules
Difference between identical particles	Permutation	B.-E. or F.-D. statistics
Absolute spatial position	Space translation $\vec{r} \rightarrow \vec{r} + \vec{\Delta}$	momentum
Absolute time	Time translation $t \rightarrow t + \tau$	energy
Absolute spatial direction	Rotation $\hat{r} \rightarrow r'$	angular momentum
Absolute velocity	Lorentz transformation	generators of the Lorentz group
Absolute right (or left)	$\vec{r} \rightarrow -\vec{r}$	parity
Absolute sign of electric charge	$e \rightarrow -e$	charge conjugation
Relative phase between states of different charge Q	$\psi \rightarrow e^{iQ\theta} \psi$	charge
Relative phase between states of different baryon number B	$\psi \rightarrow e^{iB\theta} \psi$	baryon number
Relative phase between states of different lepton number L	$\psi \rightarrow e^{iL\theta} \psi$	lepton number
Difference between different coherent mixture of p and n states	$\begin{pmatrix} p \\ n \end{pmatrix} \rightarrow U \begin{pmatrix} p \\ n \end{pmatrix}$	isospin

The D^0 and \bar{D}^0 mesons are produced as flavor eigenstates
 They propagate and decay according to

$$i \frac{\partial}{\partial t} \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix} = \left(\mathbf{M} - \frac{i}{2} \mathbf{\Gamma} \right) \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix}$$

Mixing occurs because D^0 and \bar{D}^0 are linear combinations of mass eigenstates

$$\begin{aligned} |D_1\rangle &= p|D^0\rangle + q|\bar{D}^0\rangle \\ |D_2\rangle &= p|D^0\rangle - q|\bar{D}^0\rangle \end{aligned}$$

The mass eigenstates develop in time as follow

$$\begin{aligned} |D_{1,2}(t)\rangle &= e_{1,2}(t) |D_{1,2}(0)\rangle \\ e_{1,2}(t) &\equiv \exp \left[-i \left(M_{1,2} - \frac{i}{2} \Gamma_{1,2} \right) t \right] \end{aligned}$$

Two parameters characterize the D^0 and \bar{D}^0 mixing

$$\begin{aligned} x &\equiv \frac{\Delta M}{\Gamma}, \quad \Delta M \equiv M_1 - M_2 \\ y &\equiv \frac{\Delta \Gamma}{2\Gamma}, \quad \Delta \Gamma \equiv \Gamma_1 - \Gamma_2 \end{aligned}$$

If either x or y are different from zero, mixing occurs

$$\begin{aligned} |\langle \bar{D}^0 | D^0(t) \rangle|^2 &= \frac{1}{2} \left| \frac{q}{p} \right|^2 e^{-\Gamma t} [\cosh(y\Gamma t) - \cos(x\Gamma t)] \\ |\langle D^0 | \bar{D}^0(t) \rangle|^2 &= \frac{1}{2} \left| \frac{p}{q} \right|^2 e^{-\Gamma t} [\cosh(y\Gamma t) - \cos(x\Gamma t)] \end{aligned}$$