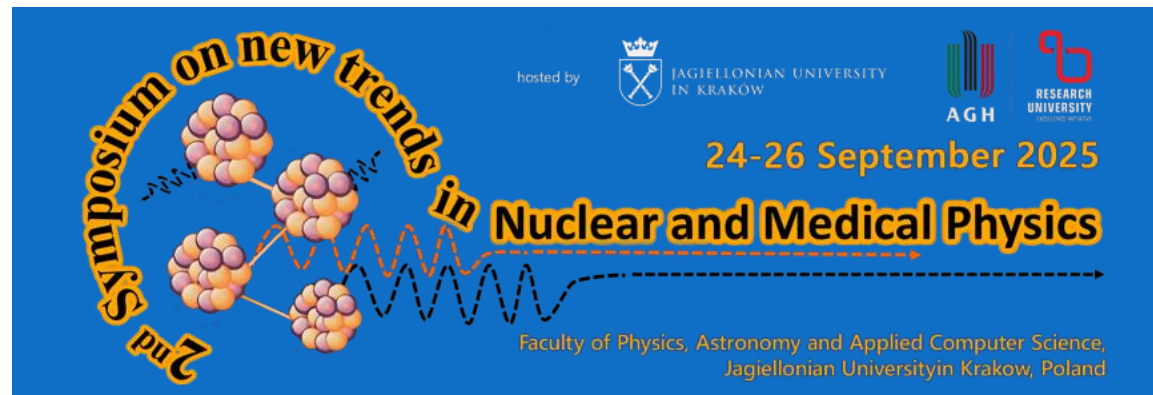


# Miniature Scintillating Detectors and SiPMs: a brief Summary and a few Applications

Paolo Finocchiaro

Istituto Nazionale di Fisica Nucleare  
Laboratori Nazionali del Sud, Catania, Italy





Our activities during the last two decades



more and more use of SiPM

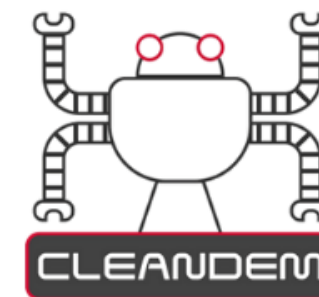
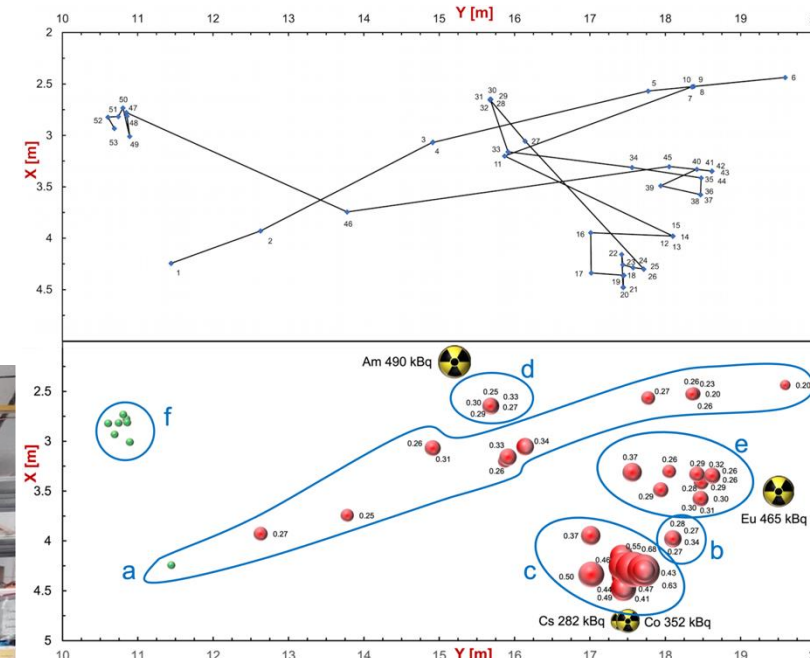
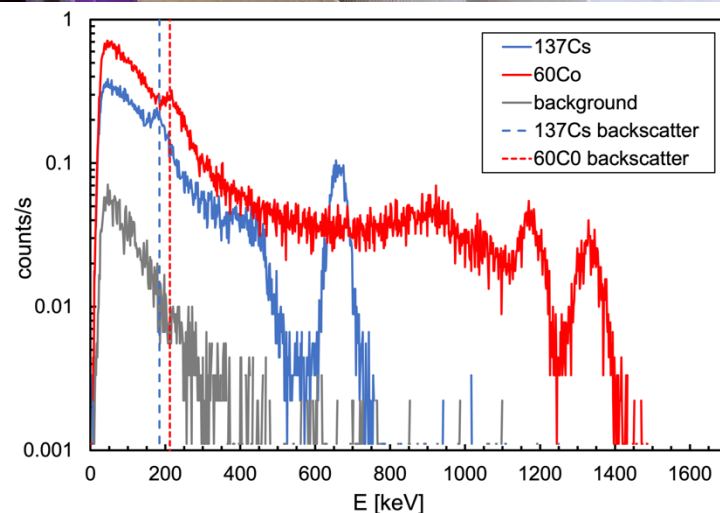
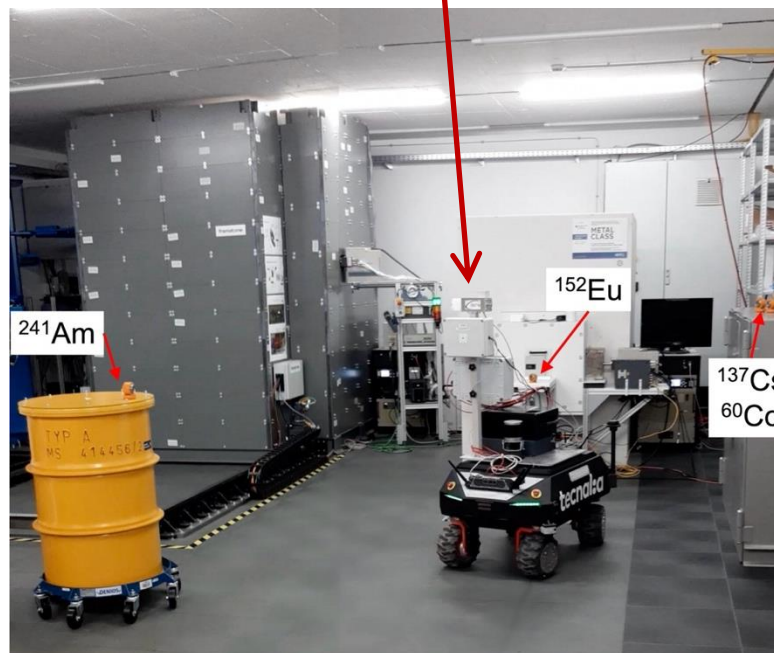
...in particular quite recently...

# Robotic inspection system in radioactive environment

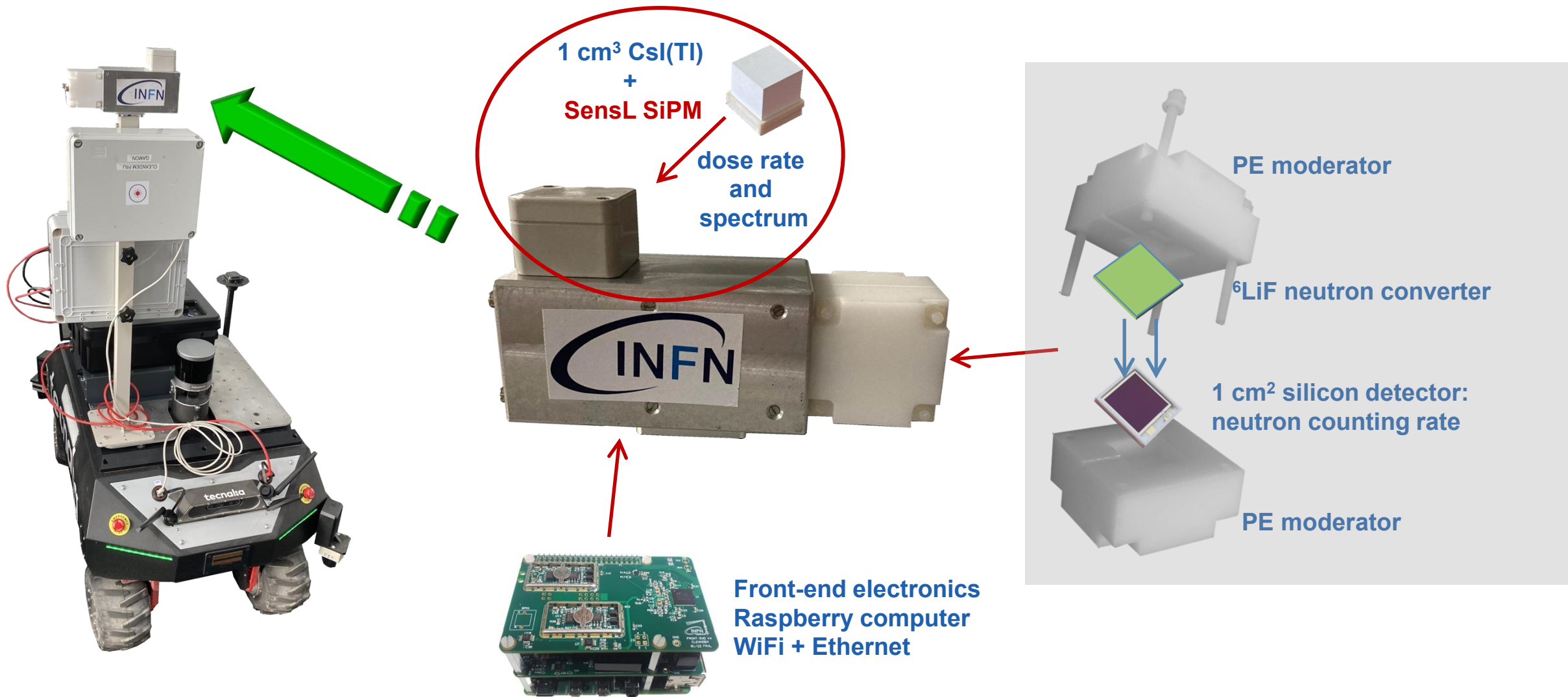


1cm<sup>3</sup> CsI(Tl) scintillator  
+  
6mm × 6mm SensL SiPM

MiniRadMeter



# MiniRadMeter: gamma and neutron dose rate monitor

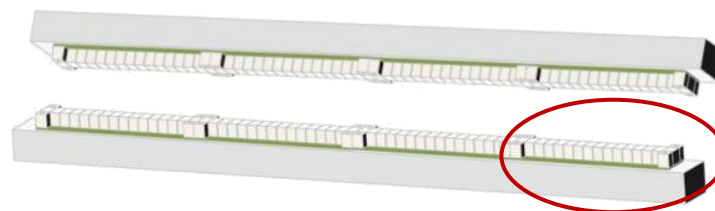
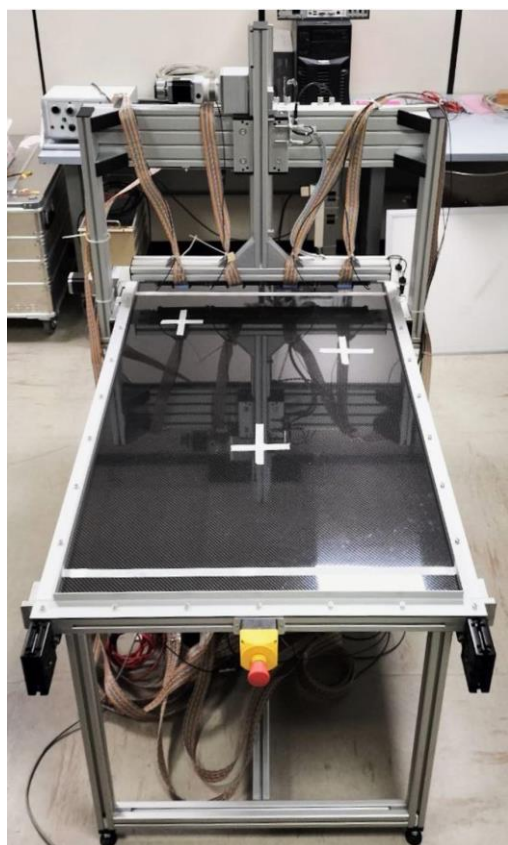




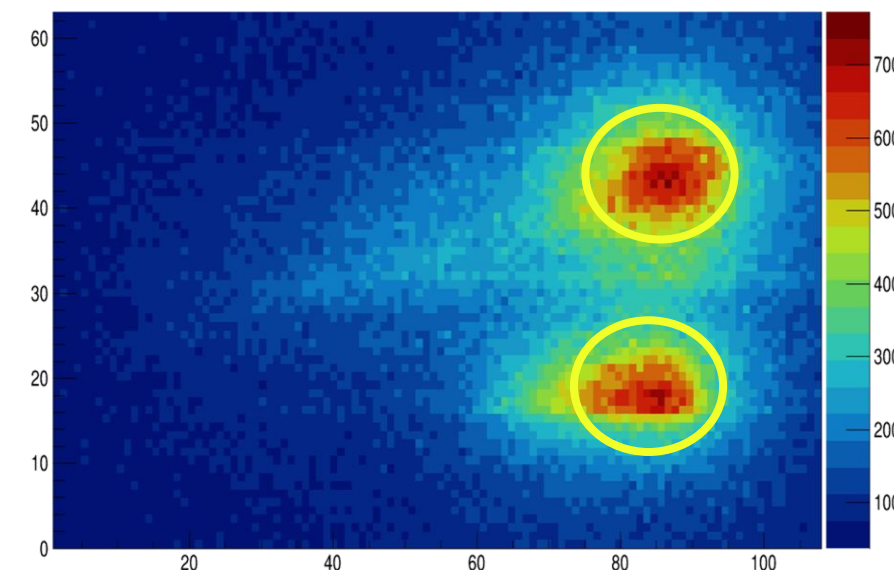
# Proximity Imaging Scanner for Sort and Segregate Operations

## PI3SO

128 × 1cm<sup>3</sup> CsI(Tl) scintillators +  
128 6mm × 6mm Hamamatsu SiPM

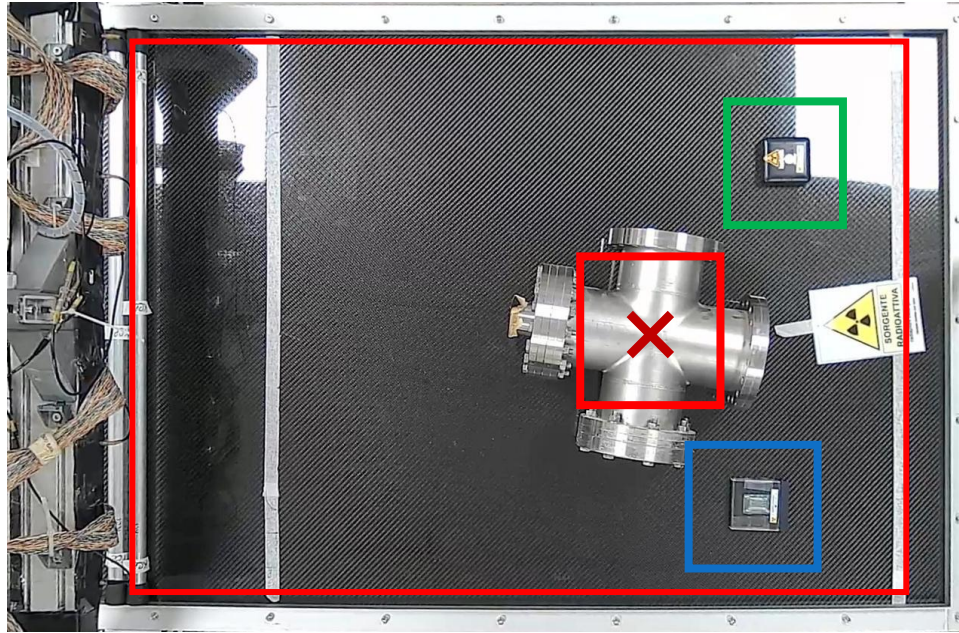


× 8

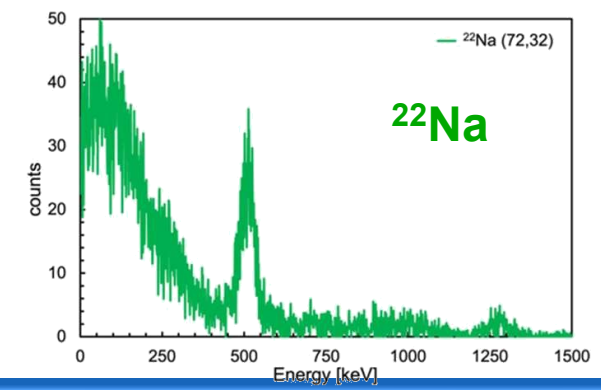
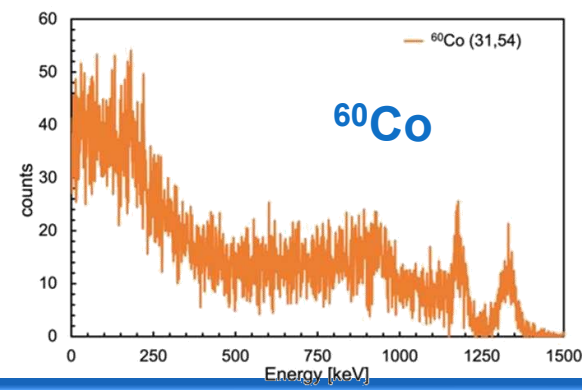
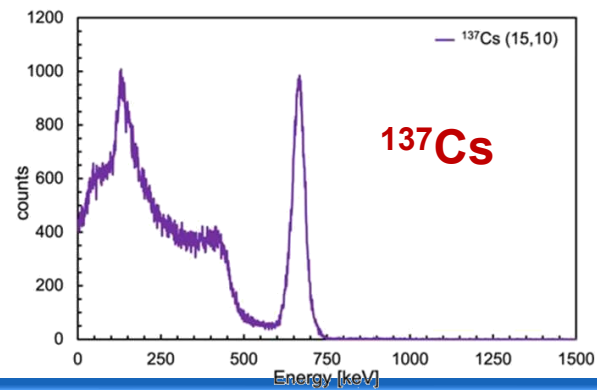
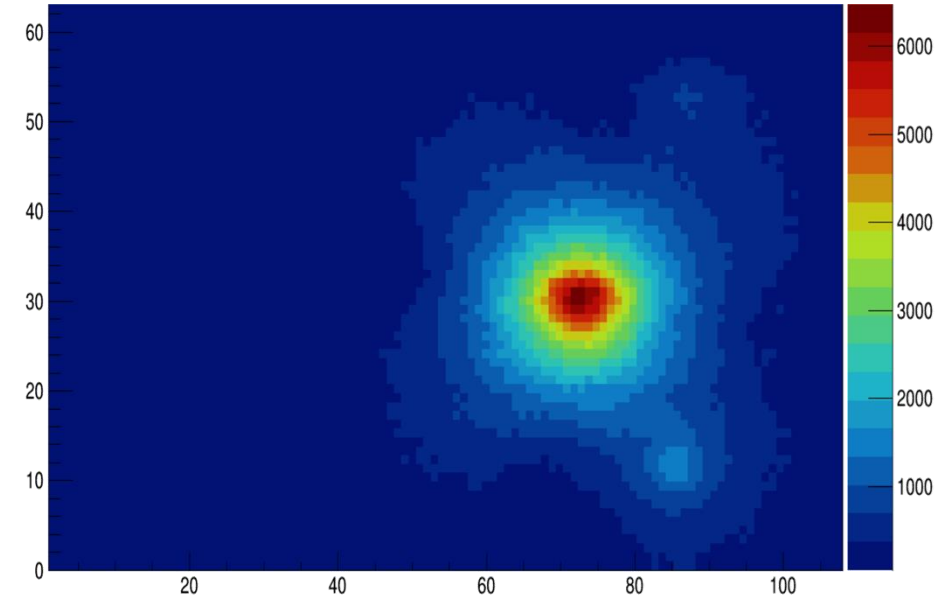


1.4MBq  $^{137}\text{Cs}$  12,6kBq  $^{22}\text{Na}$

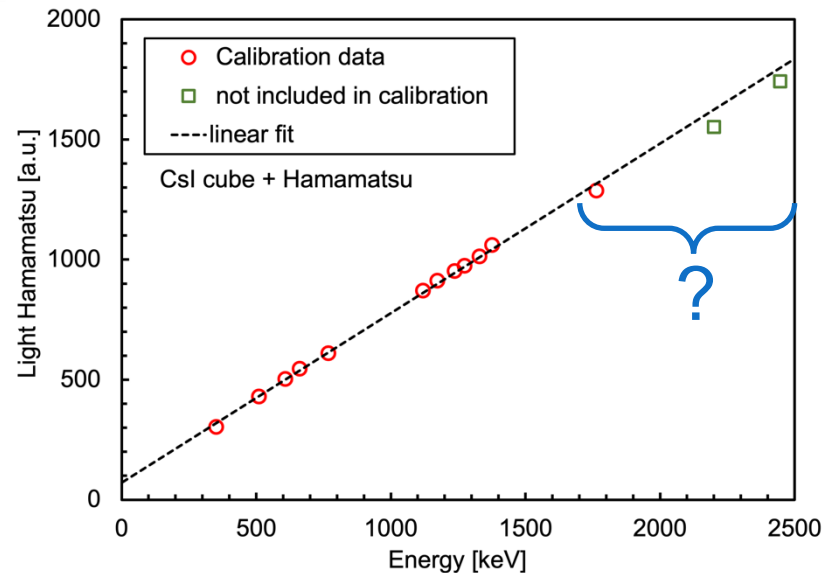
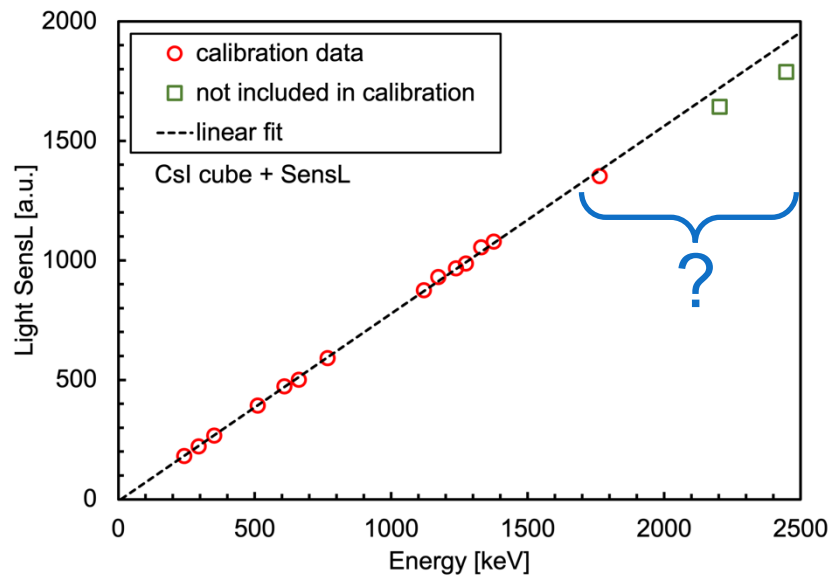
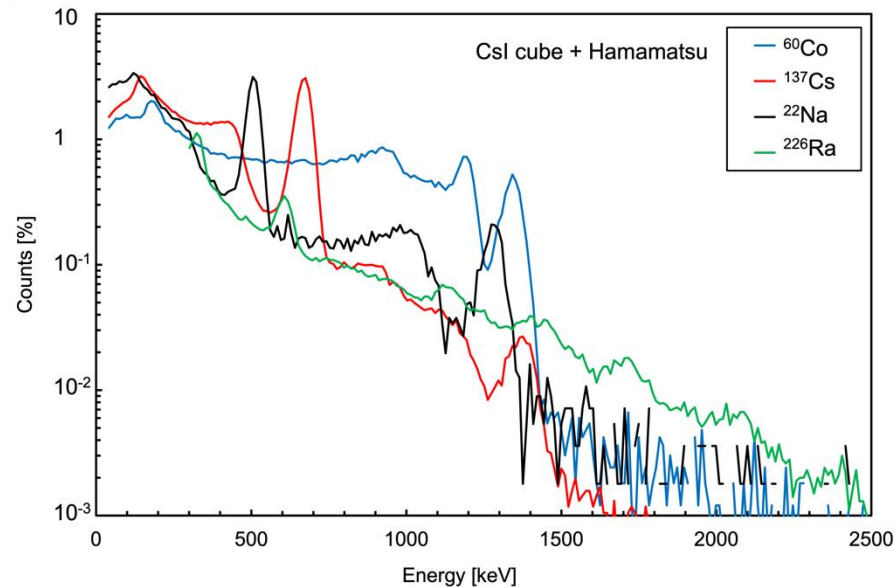
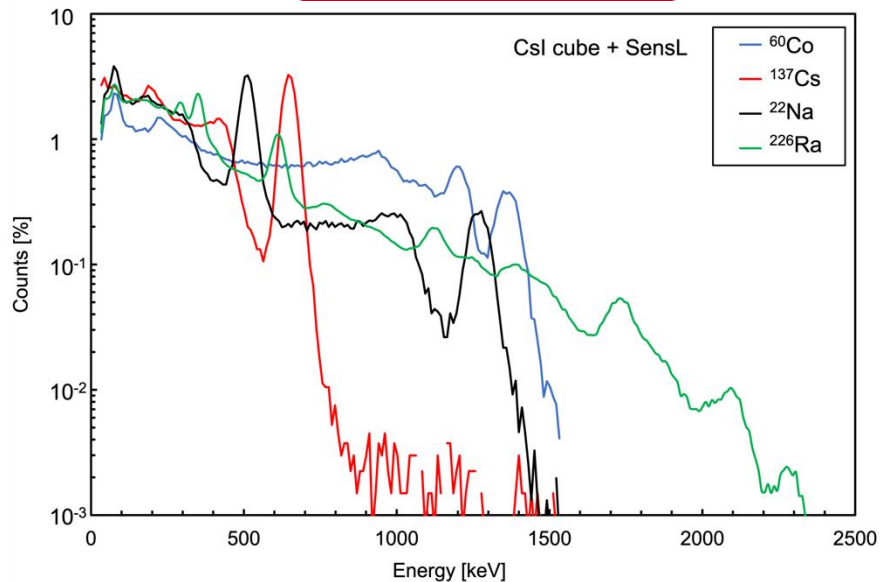
PI3SO



50,0kBq  $^{60}\text{Co}$





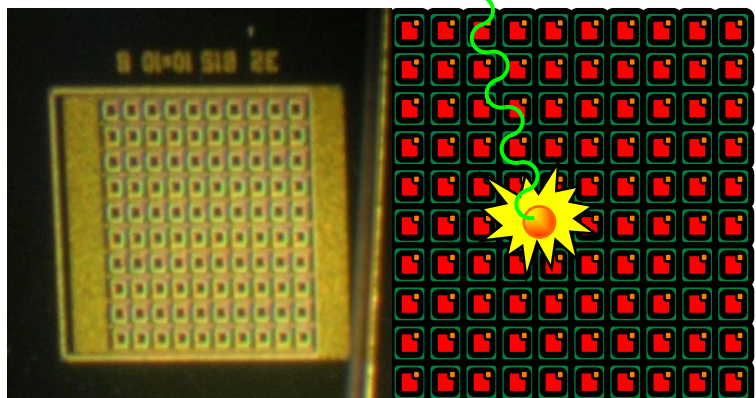


are the SiPMs  
non linear?



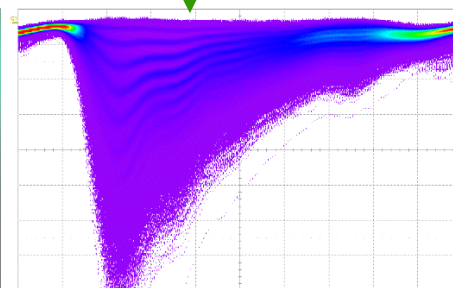
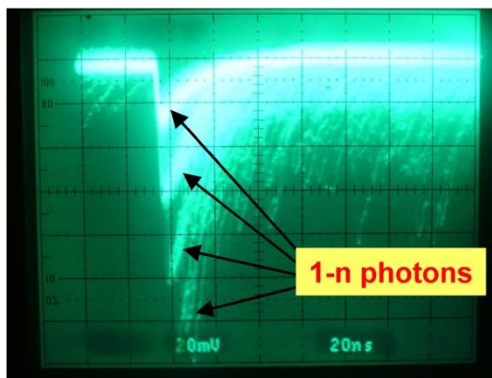
# What is a SiPM?

Photon

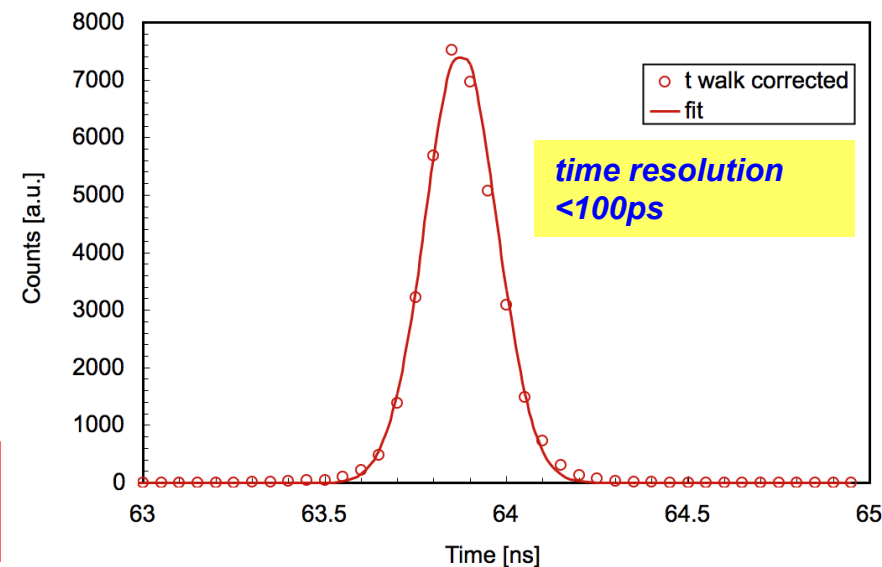
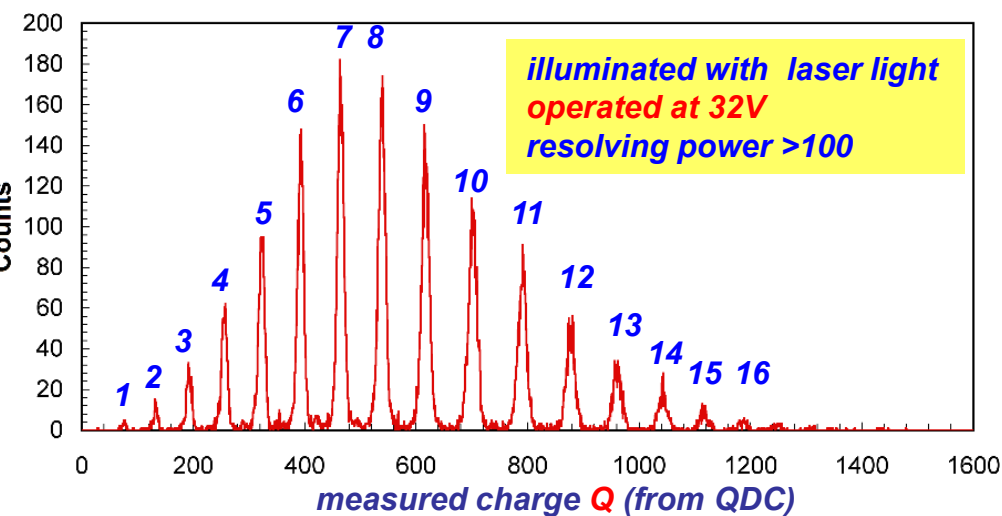


low bias voltage (30-60V)  
high physical amplification (gain)

1 photon gives rise to  
a signal of  $\approx 10^6$  electrons



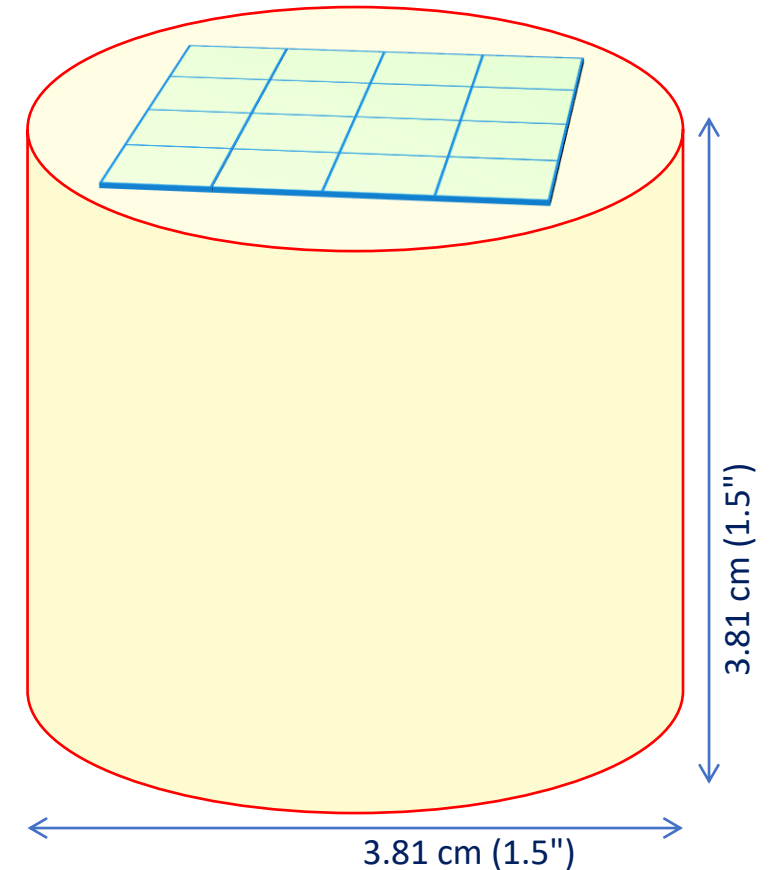
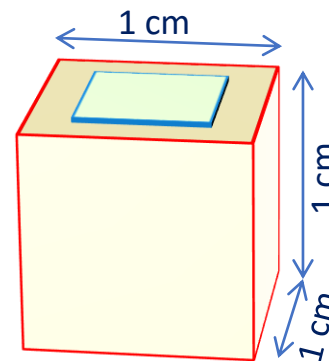
1-cell  $\Rightarrow$  charge =  $k$   
 $n$ -cells  $\Rightarrow$  charge =  $nk$



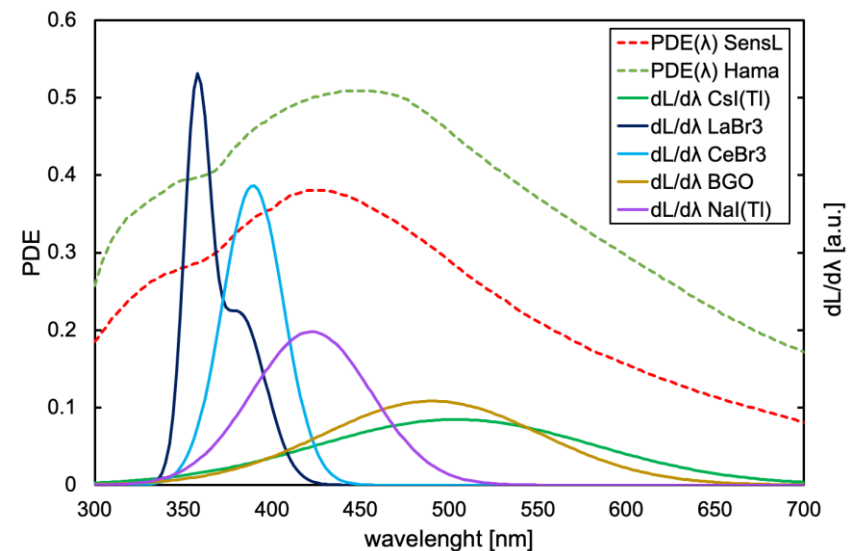
## The model

we modeled

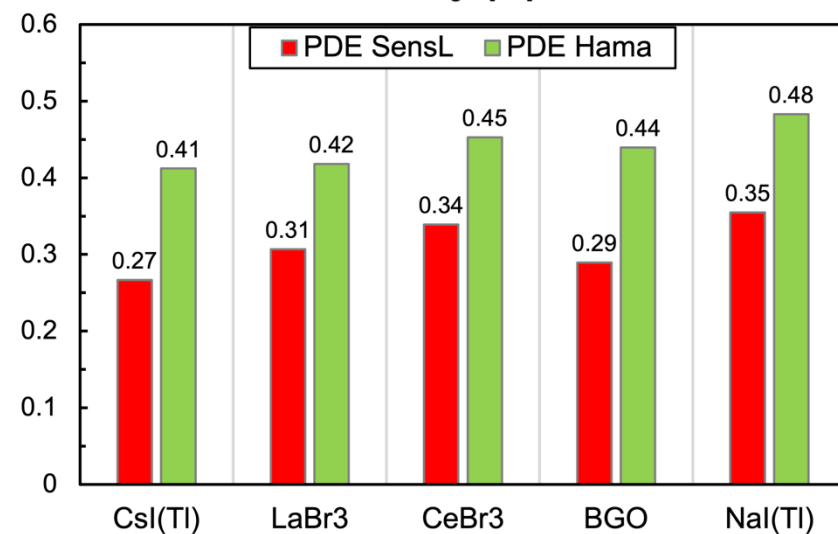
- 2 geometries: cube, cylinder
- 2 SiPMs 6mm × 6mm:
  - SensL MICROFC-60035-SMT
  - Hamamatsu S14160-6050HS
- 5 crystal types:
  - CsI(Tl)
  - LaBr<sub>3</sub>(Ce)
  - CeBr<sub>3</sub>
  - BGO
  - NaI(Tl)



	CsI(Tl)	LaBr3(Ce)	CeBr3	BGO	Nal(Tl)
Light yield [photons/keV]	60	70	70	10	45
Decay time [ns]	960	30	20	300	250
Refractive index at $\lambda$ max	1.8	1.9	2.1	2.1	1.8
Weighted PDE SensL [%]	<b>27%</b>	<b>31%</b>	<b>34%</b>	<b>29%</b>	<b>35%</b>
Weighted PDE Hamamatsu [%]	<b>41%</b>	<b>42%</b>	<b>45%</b>	<b>44%</b>	<b>48%</b>



	MICROFC-60035-SMT SensL (now OnSemi)	S14160-6050HS Hamamatsu
number of microcells	18980	14331
microcell recharge time [ns]	100	92





## Simple naive model for the light collection efficiency

No geometry considered

Photon produced inside hits the inner surface

Assume it hits the SiPM with probability  $\varepsilon$  equal to the area ratio

Otherwise it is reflected ( $r$ ) or absorbed ( $1 - r$ )

$P_1$  = probability of collection after 1 step

$P_n$  = probability of collection after  $n$  steps

$$P_1 = \varepsilon$$

$$P_2 = \varepsilon(1 - \varepsilon)r$$

$$P_3 = \varepsilon[(1 - \varepsilon)r]^2$$

...

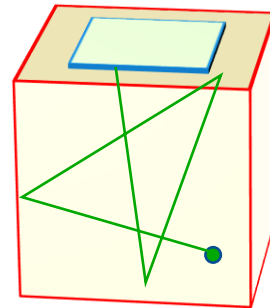
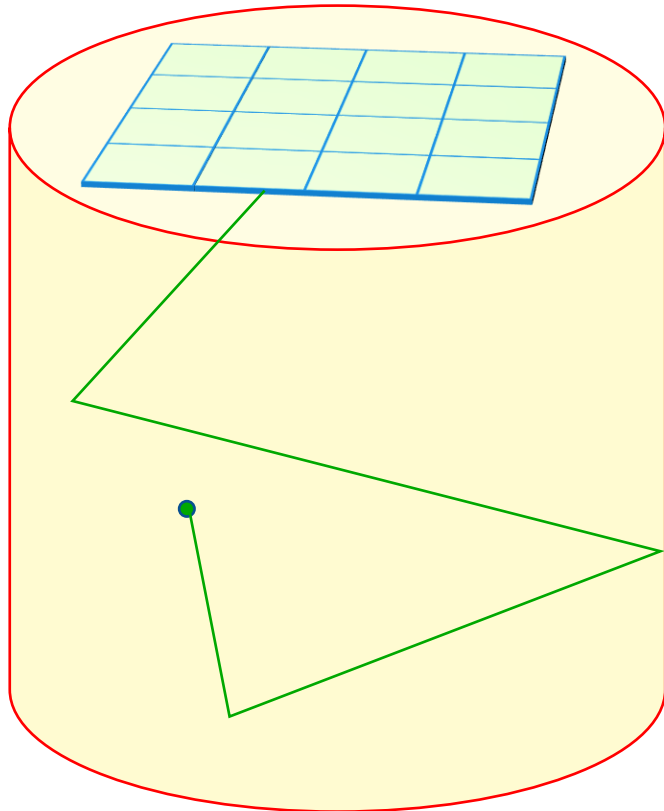
$$P_n = \varepsilon[(1 - \varepsilon)r]^{n-1}$$

$$P = \sum_n P_n = \sum_n \varepsilon[(1 - \varepsilon)r]^{n-1} = \varepsilon \frac{1 - [(1 - \varepsilon)r]^n}{1 - (1 - \varepsilon)r} \approx \frac{\varepsilon}{1 - r + r\varepsilon}$$

Light collection efficiency  $P$  = overall collection probability

$P$  calculated for  $r = 0.9$  to  $1.0$ , step =  $0.01$

## Cross-check with a GEANT4 Monte Carlo model



Lambertian inner (white) surface reflection (distributed as  $\cos\theta$ )

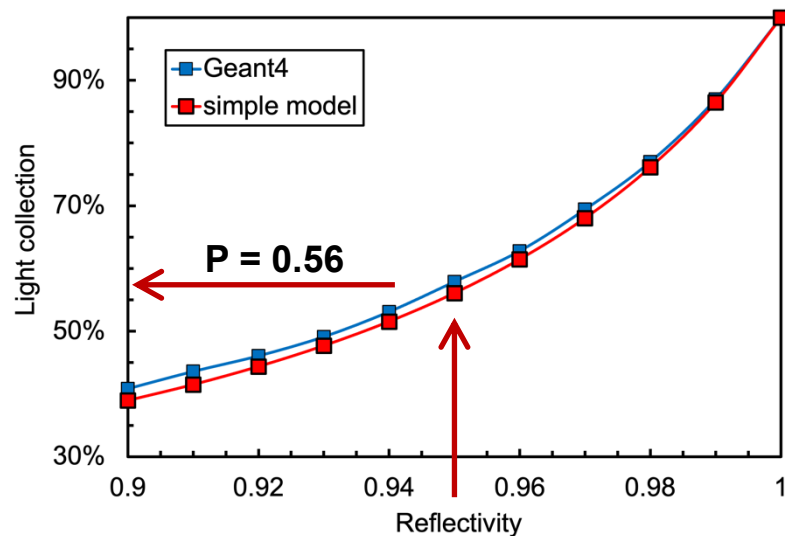
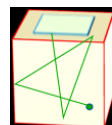
$10^5$  photons were generated and tracked in each run

11 runs in cubic geometry ( $r = 0.9$  to  $1.0$ , step=0.01)

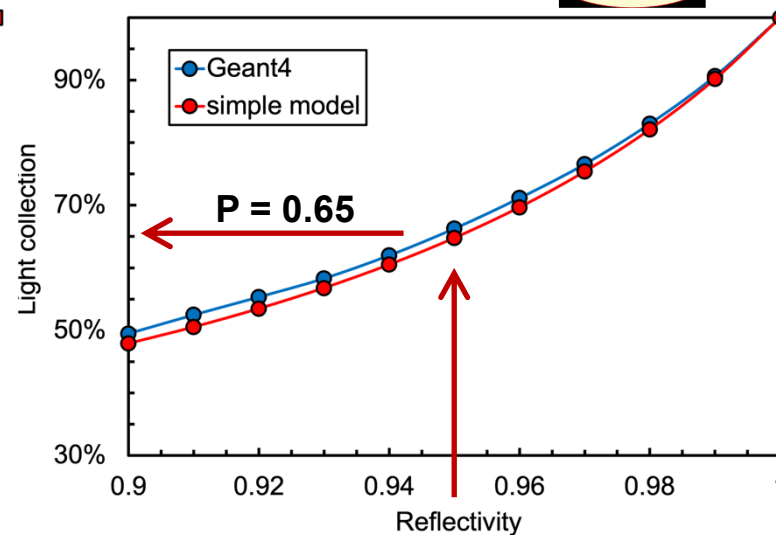
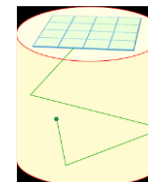
11 runs in cylindrical geometry ( $r = 0.9$  to  $1.0$ , step = 0.01)

Light collection efficiency  $P = \text{n. of photons on the SiPM} / 10^5$

Cube  $\varepsilon = 0.06$



Cylinder  $\varepsilon = 0.084$



At  $r = 0.95$  the difference is  $\leq 2\%$

...curiously...

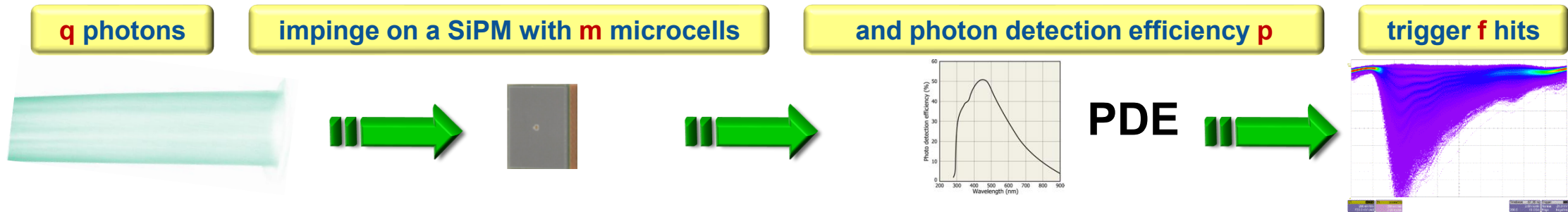
...if using  $\varepsilon^+ = \varepsilon \times 1.067...$

...the difference reduces to  $\approx 0.1\%$

Chosen a realistic value of  $r = 0.95$



## Multiple hit effect on SiPM?



$$f(q) = m \left[ 1 - \left( 1 - \frac{p}{m} \right)^q \right]$$

**exact formula (binomial distribution)**

$$\lim_{n \rightarrow \infty} \left( 1 + \frac{x}{n} \right)^n = e^x$$

**exploit the notable limit**

$$f(q) = m \left( 1 - e^{-\frac{pq}{m}} \right)$$

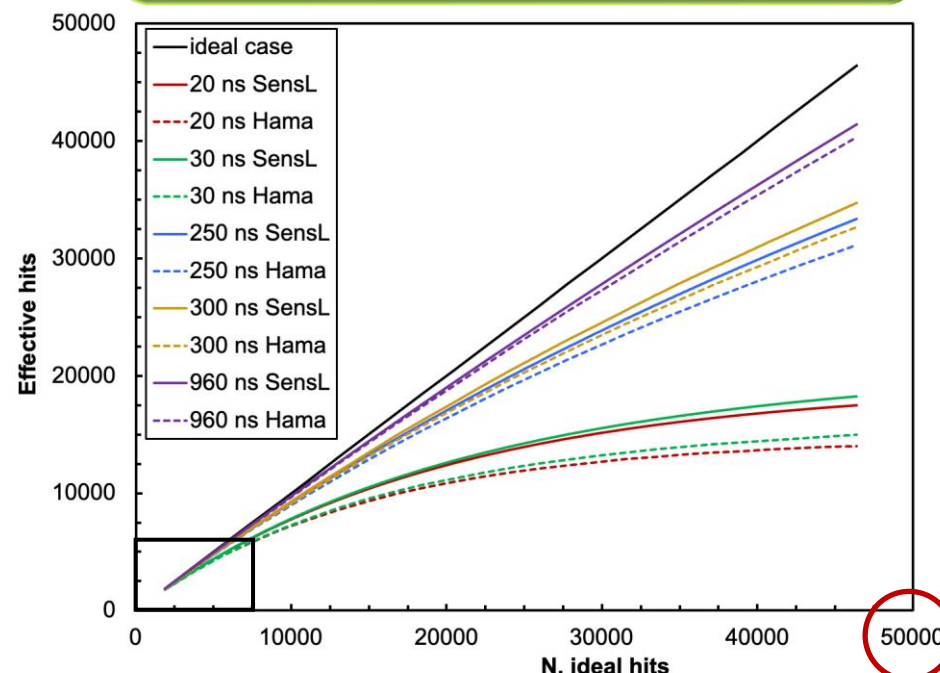
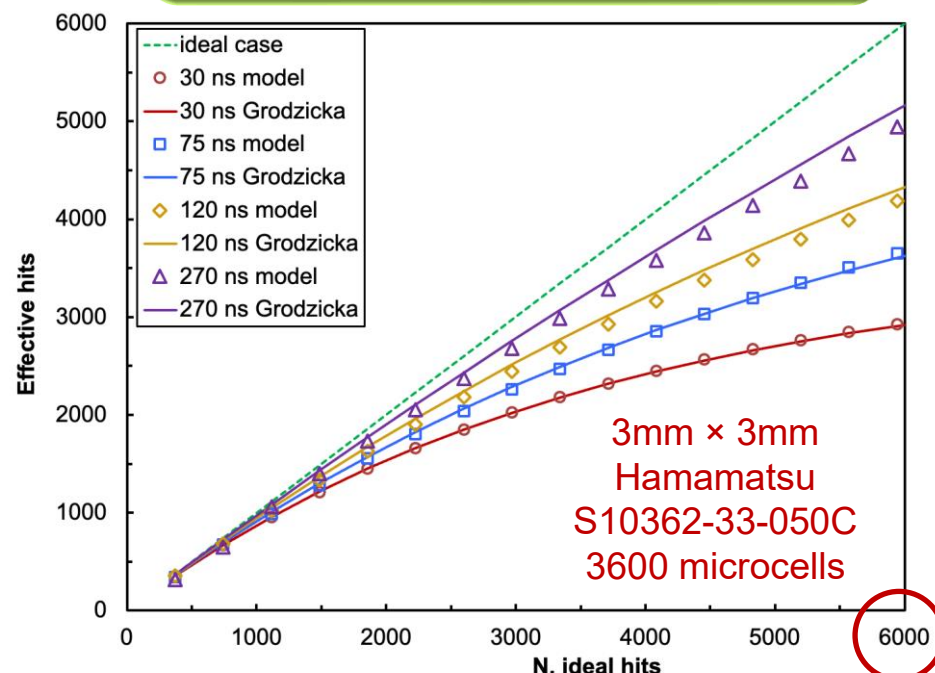
**perfect approximation**

- **follow the time evolution**
- **in 5ns steps**
- **disable the triggered cells**
- **during their recharge time**

## Comparison of our model with the Grodzicka formula gaussian-shaped light pulses



## Comparison of our model with the extrapolation of Grodzicka formula Intense exponential-shaped light pulses



Contents lists available at [ScienceDirect](https://www.sciencedirect.com)  
Nuclear Instruments and Methods in  
Physics Research A  
journal homepage: [www.elsevier.com/locate/nima](http://www.elsevier.com/locate/nima)

New method for evaluating effective recovery time and single photoelectron response in silicon photomultipliers

Martyna Grodzicka\*, Tomasz Szczęśniak, Marek Moszyński, Marek Szawłowski, Krystian Grodzicki

National Centre for Nuclear Research, A. Soltana 7, PL 05-400 Świerk, Otwock, Poland

18980 microcells SensL MICROFC-60035-SMT  
14331 microcells Hamamatsu S14160-6050HS

### Different results due to

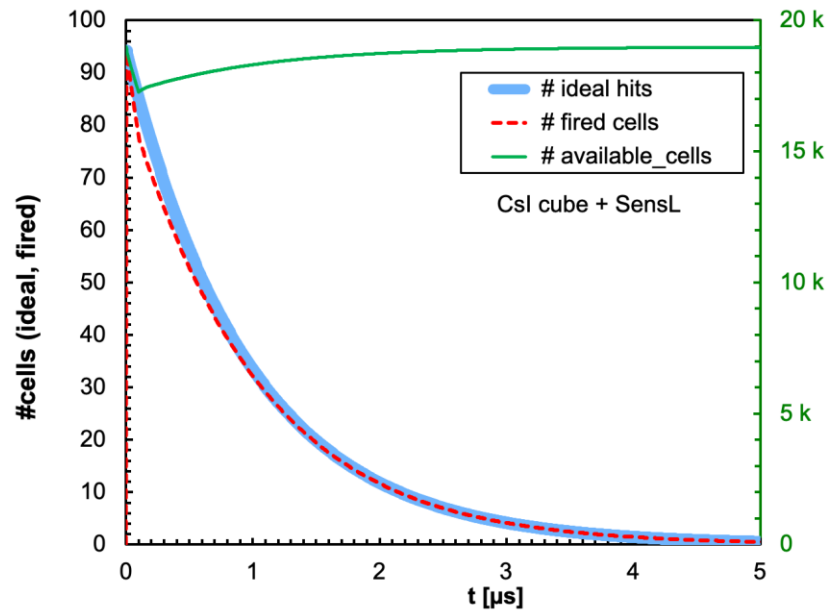
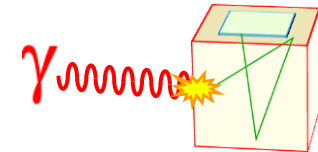
- exp vs gauss pulse shape
- following time evolution

**CsI(Tl)**

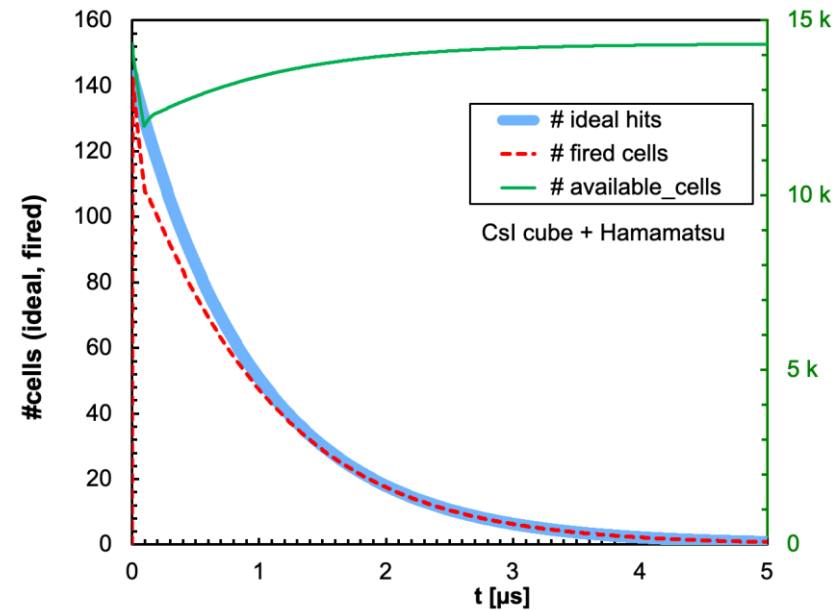
$\tau = 960 \text{ ns}$

**L.Y. = 60 Ph/keV**

**2 MeV deposited  
gamma ray**



**SensL 18980 cells  
weighted PDE = 27%**



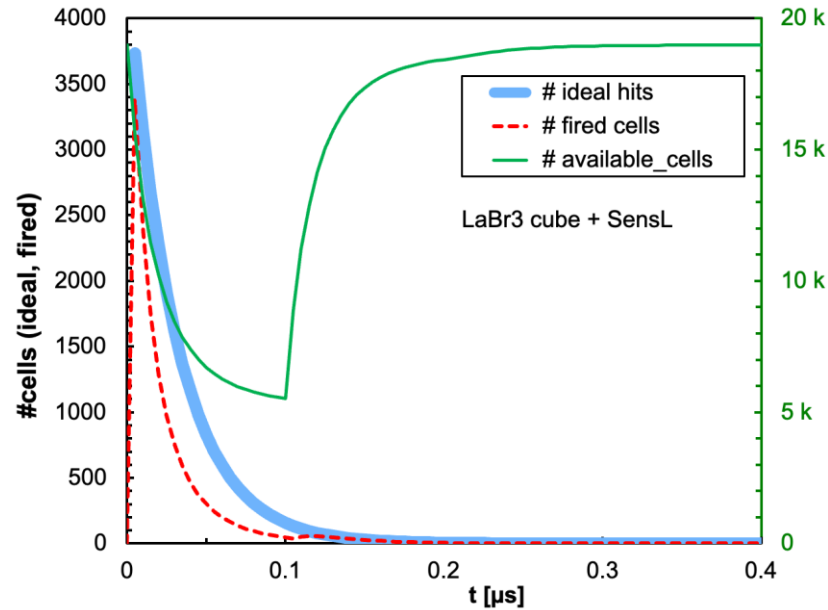
**Hamamatsu 14331 cells  
weighted PDE = 41%**



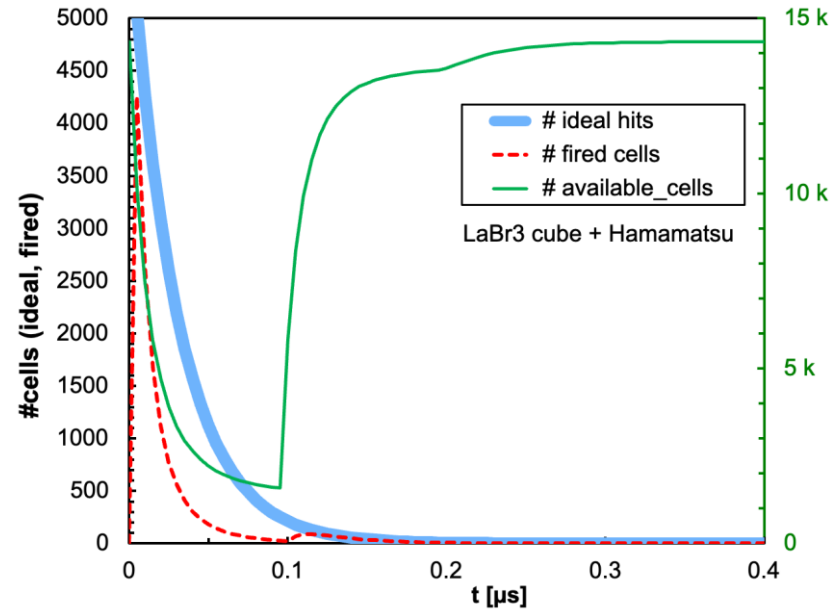
**LaBr3(Ce)**

$\tau = 30 \text{ ns}$

**L.Y. = 70 Ph/keV**

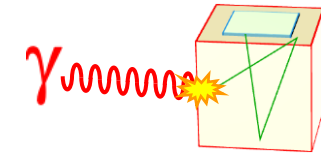


**SensL 18980 cells  
weighted PDE = 31%**



**Hamamatsu 14331 cells  
weighted PDE = 42%**

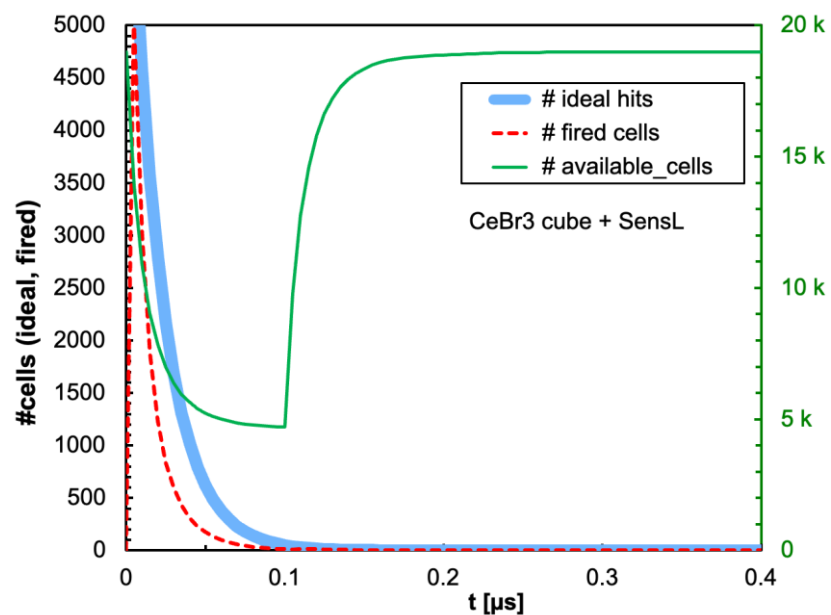
**2 MeV deposited  
gamma ray**



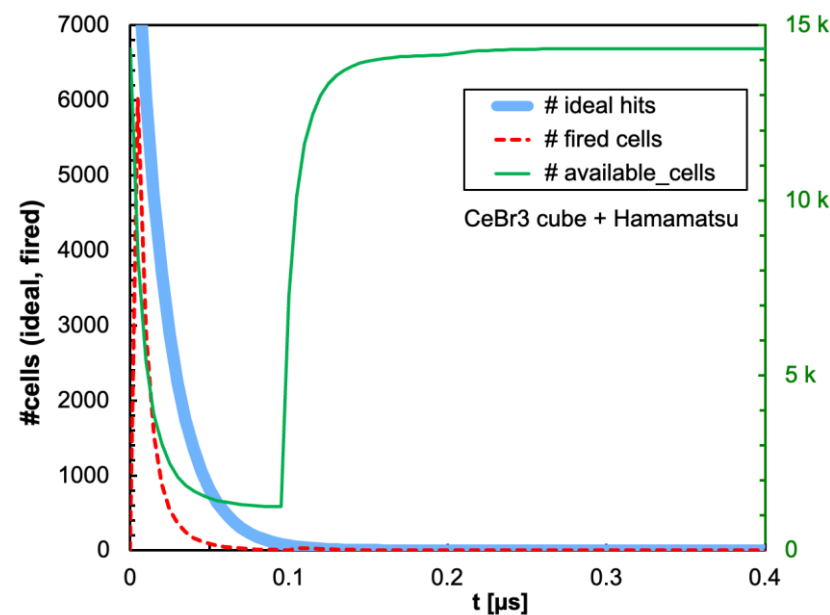
**CeBr3**

$\tau = 20 \text{ ns}$

**L.Y. = 70 Ph/keV**

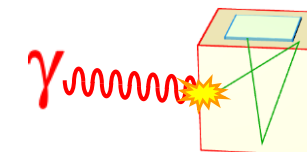


**SensL 18980 cells  
weighted PDE = 34%**



**Hamamatsu 14331 cells  
weighted PDE = 45%**

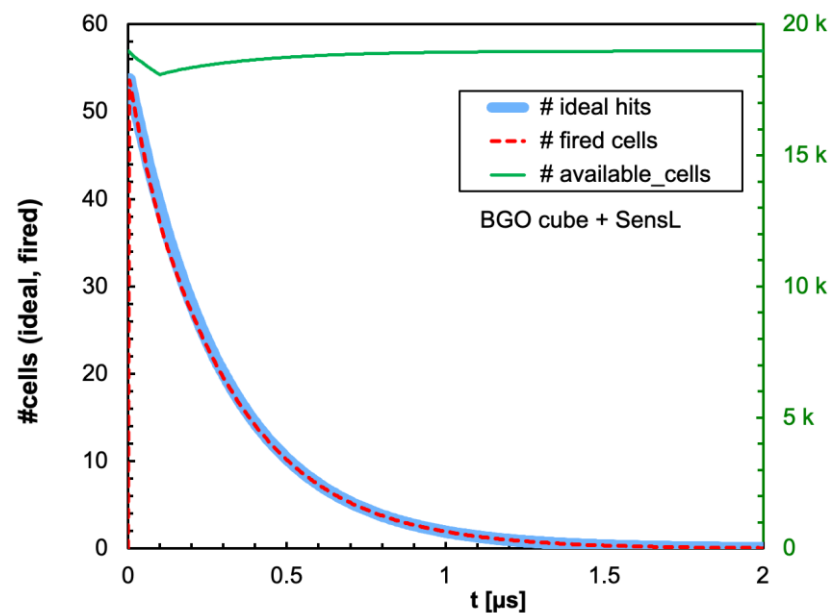
**2 MeV deposited  
gamma ray**



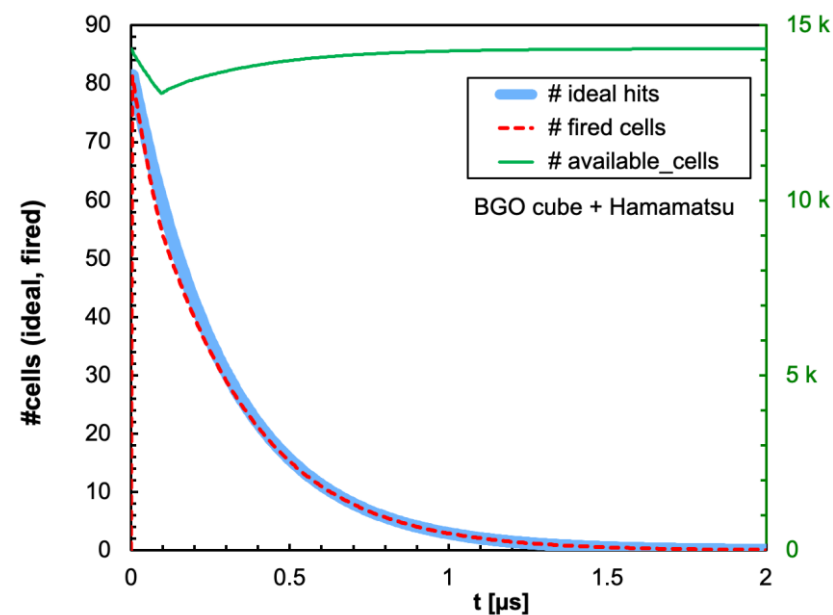
**BGO**

$\tau = 300$  ns

L.Y. = 10 Ph/keV

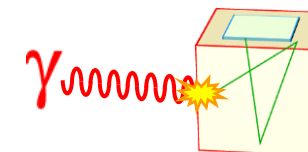


**SensL 18980 cells  
weighted PDE = 29%**



**Hamamatsu 14331 cells  
weighted PDE = 44%**

**2 MeV deposited  
gamma ray**

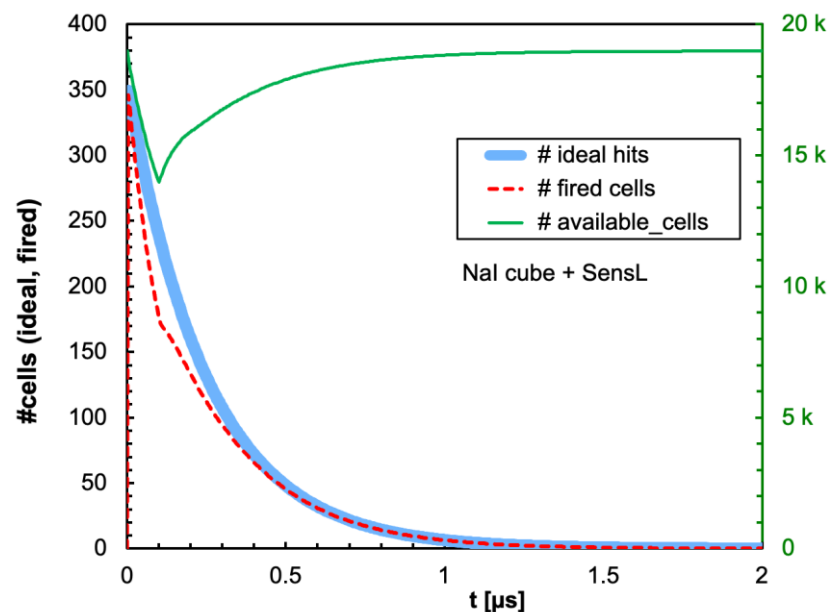




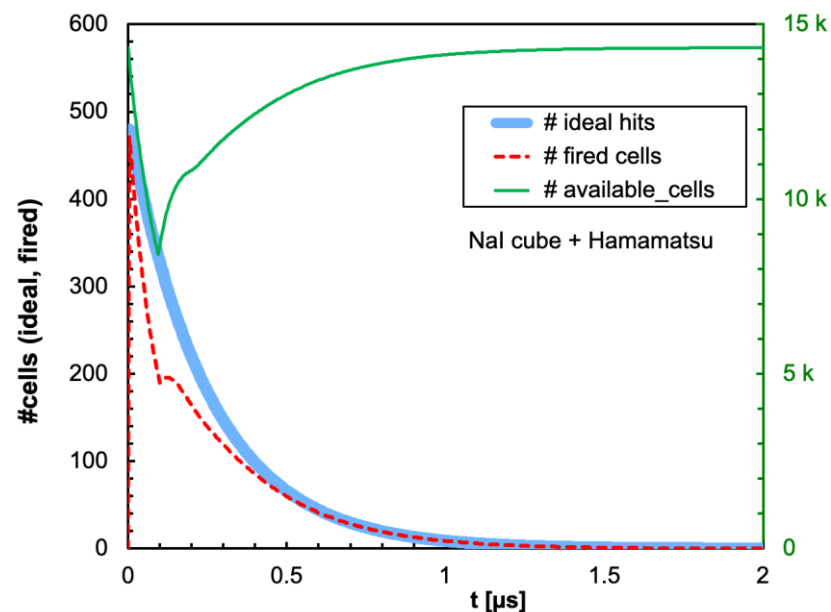
**Nal(Tl)**

$\tau = 250 \text{ ns}$

**L.Y. = 45 Ph/keV**

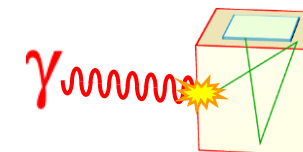


**SensL 18980 cells  
weighted PDE = 35%**

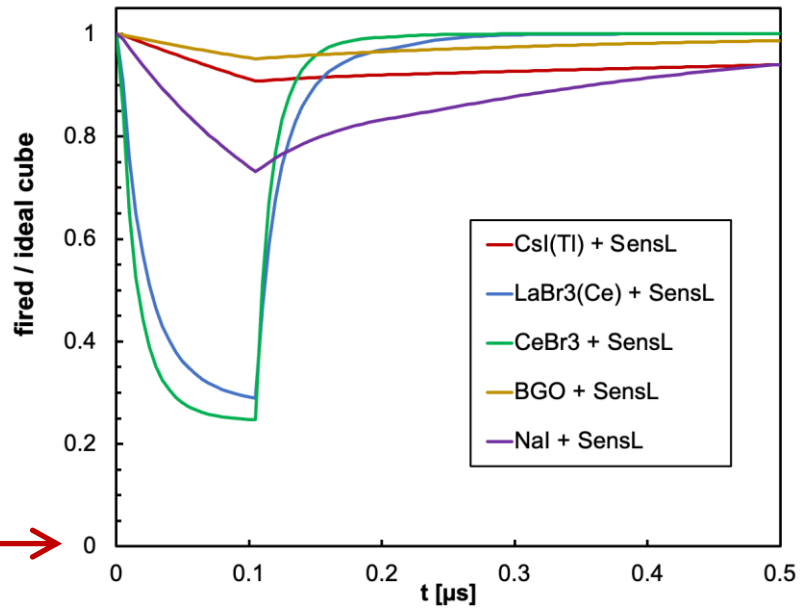


**Hamamatsu 14331 cells  
weighted PDE = 48%**

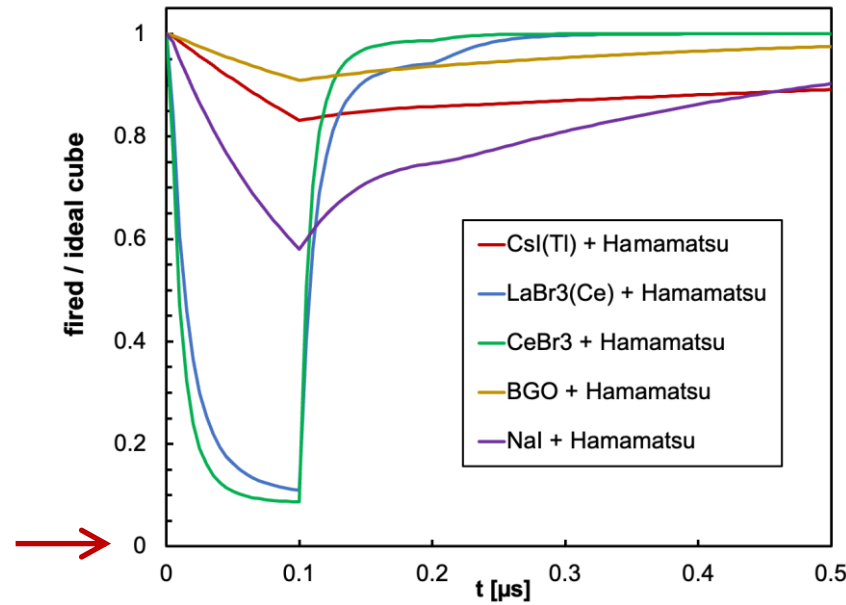
**2 MeV deposited  
gamma ray**



## fired to ideal #microcells ratio

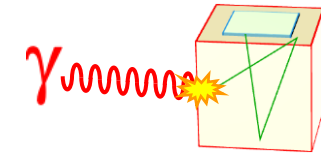


SensL 18980 cells



Hamamatsu 14331 cells

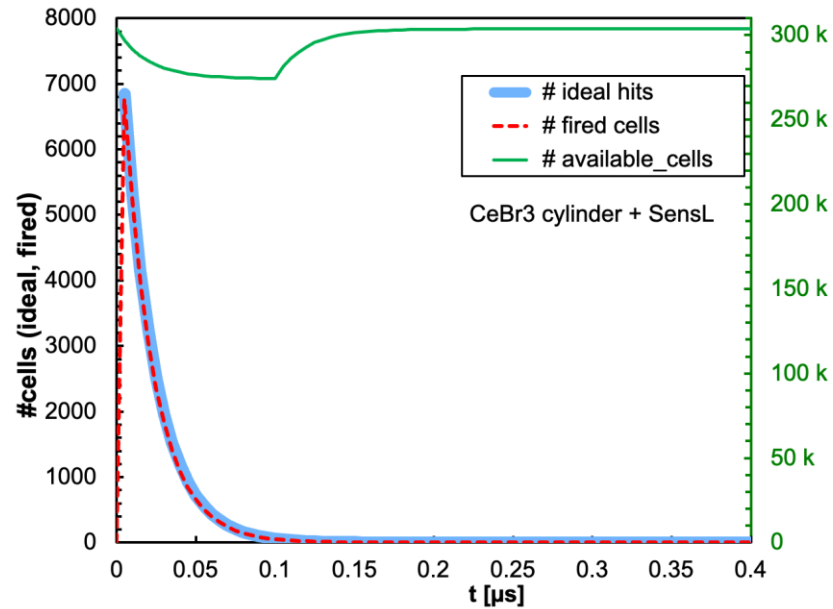
2 MeV deposited  
gamma ray



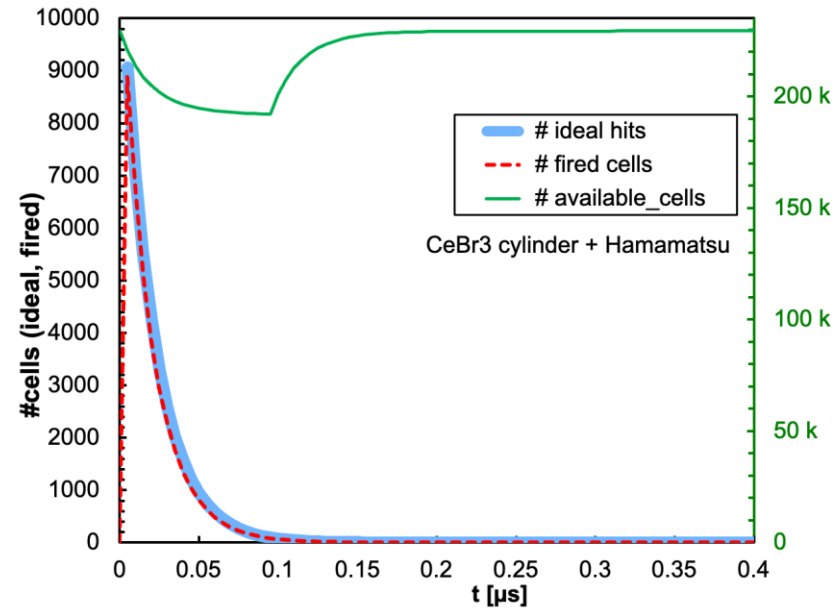
**CeBr3**

$\tau = 20 \text{ ns}$

**L.Y. = 70 Ph/keV**

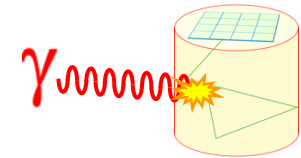


**SensL  $18980 \times 16$  cells  
weighted PDE = 34%**



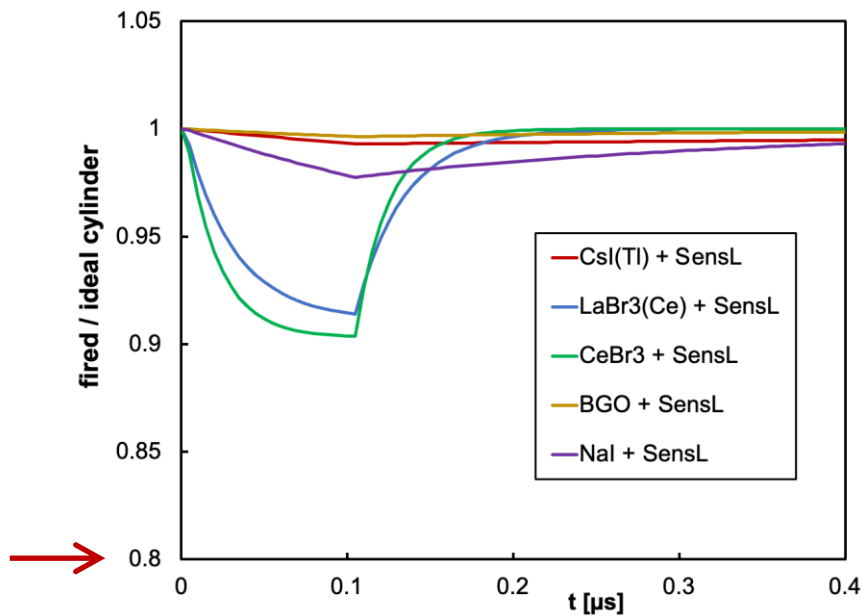
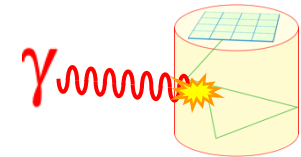
**Hamamatsu  $14331 \times 16$  cells  
weighted PDE = 45%**

**2 MeV deposited  
gamma ray**

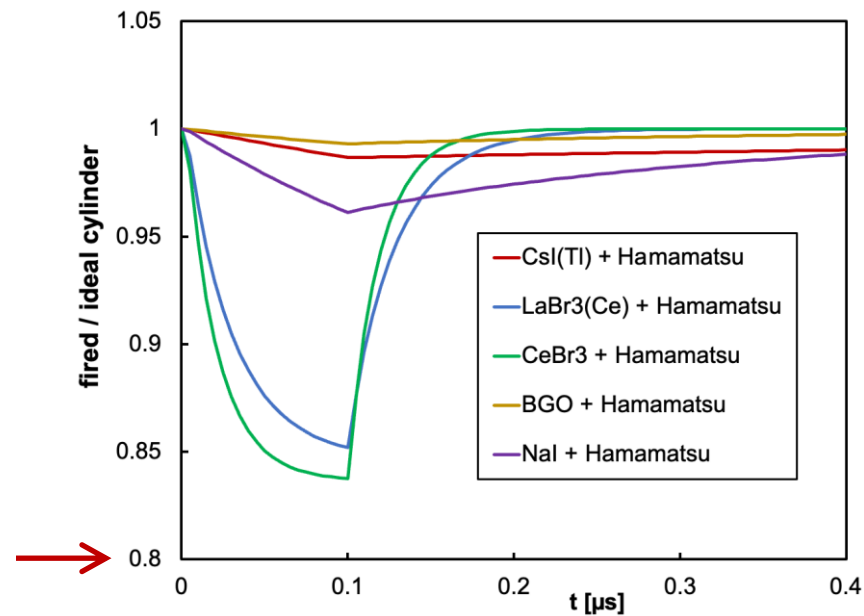


## fired to ideal #microcells ratio

2 MeV deposited  
gamma ray



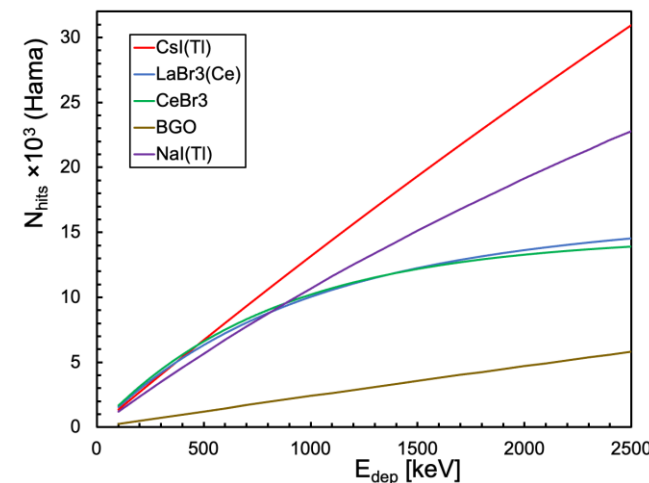
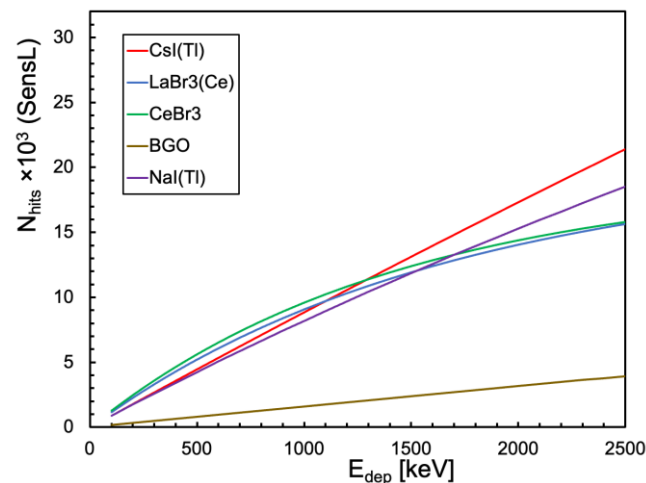
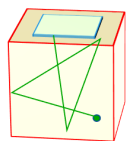
SensL 18980 × 16 cells



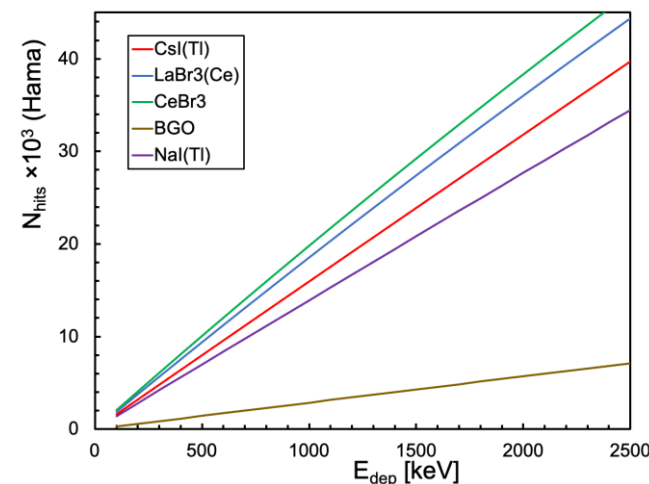
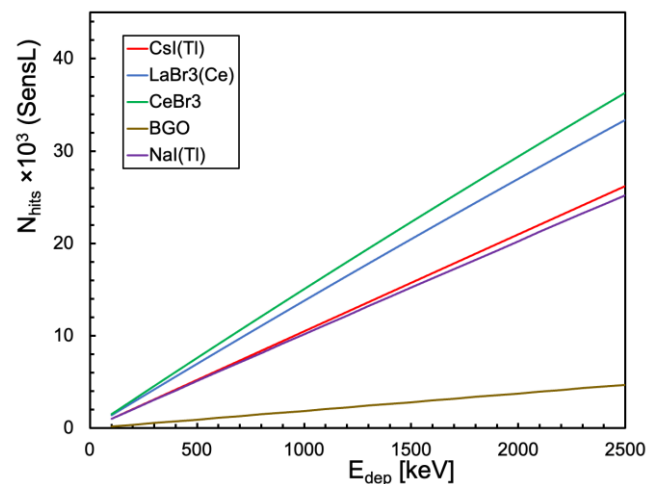
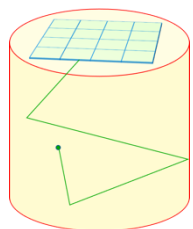
Hamamatsu 14331 × 16 cells

## SensL 18980 cells, smaller PDE

## Hamamatsu 14331 cells, larger PDE

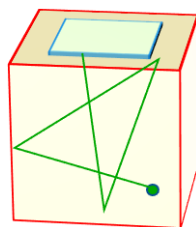


1 SiPM

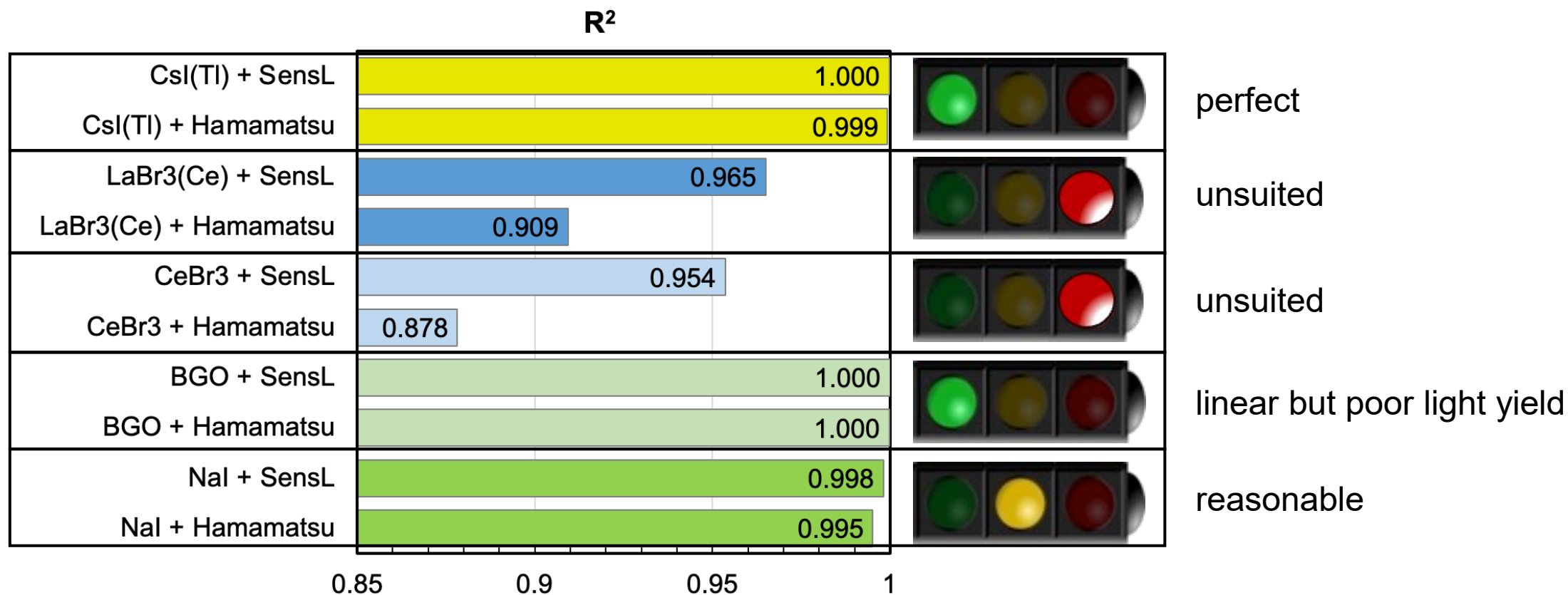


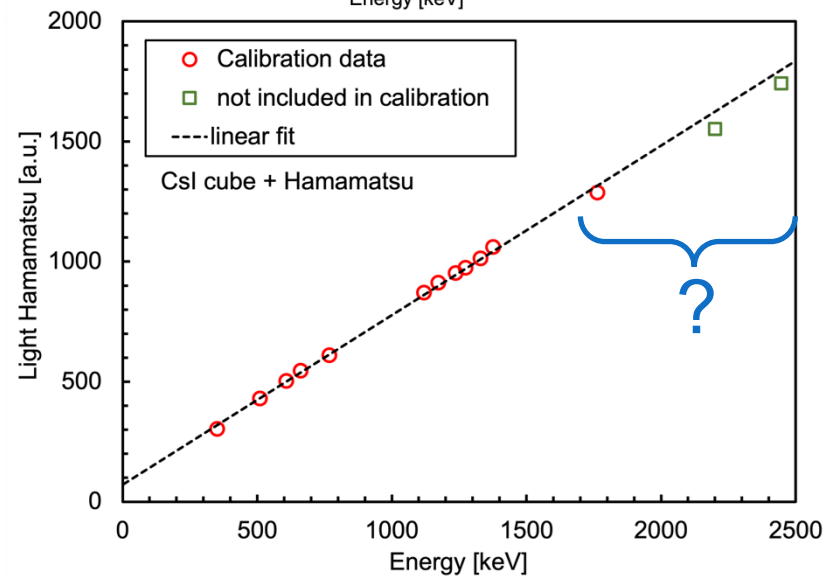
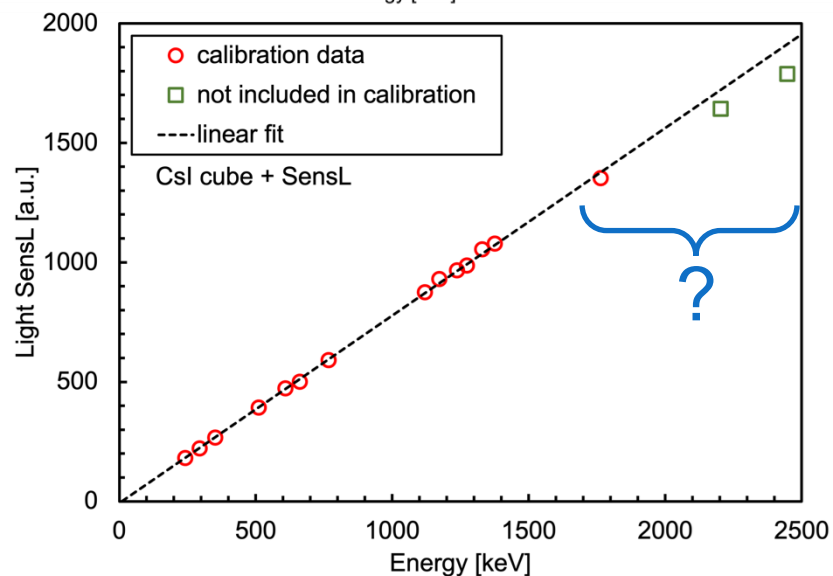
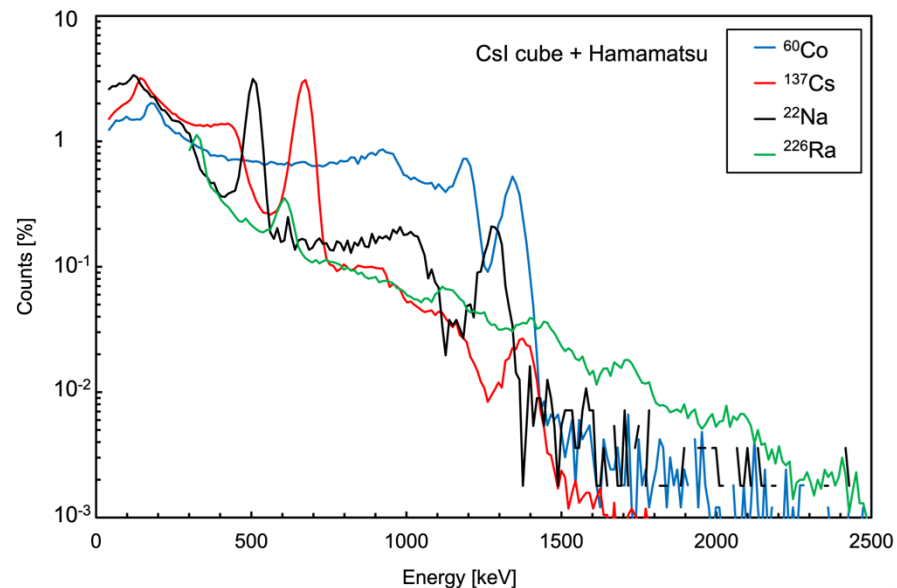
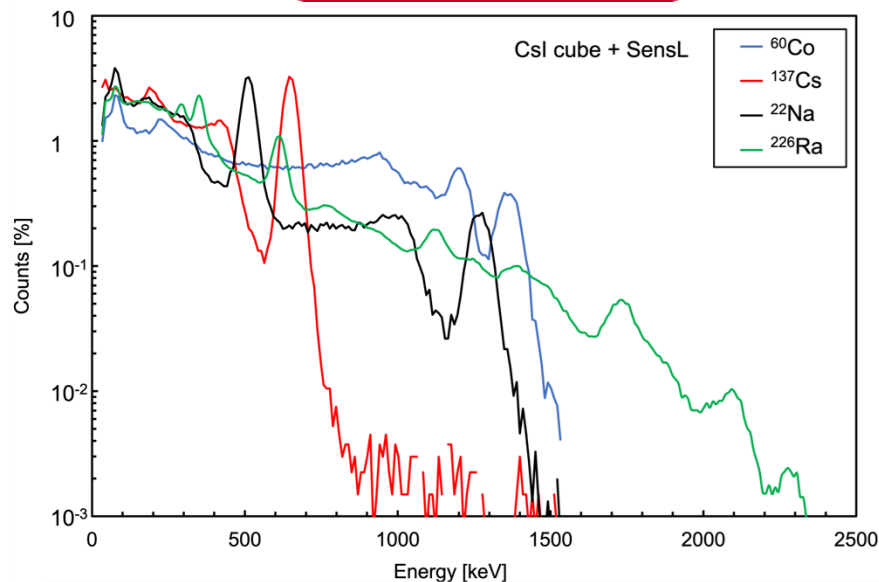
16 SiPMs





## Response linearity: $R^2$ from linear fit





is one SiPM + CsI(Tl)  
cube non-linear?

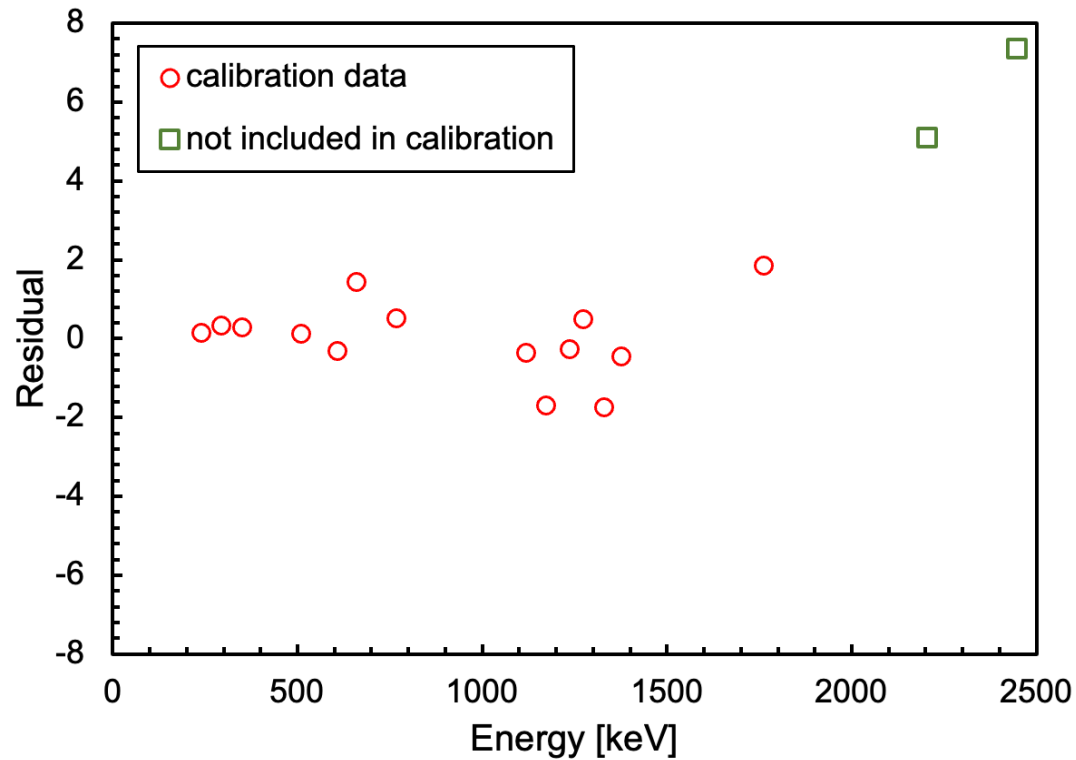
Not really, likely it is  
CsI(Tl) non-linearity

also reported by  
other authors

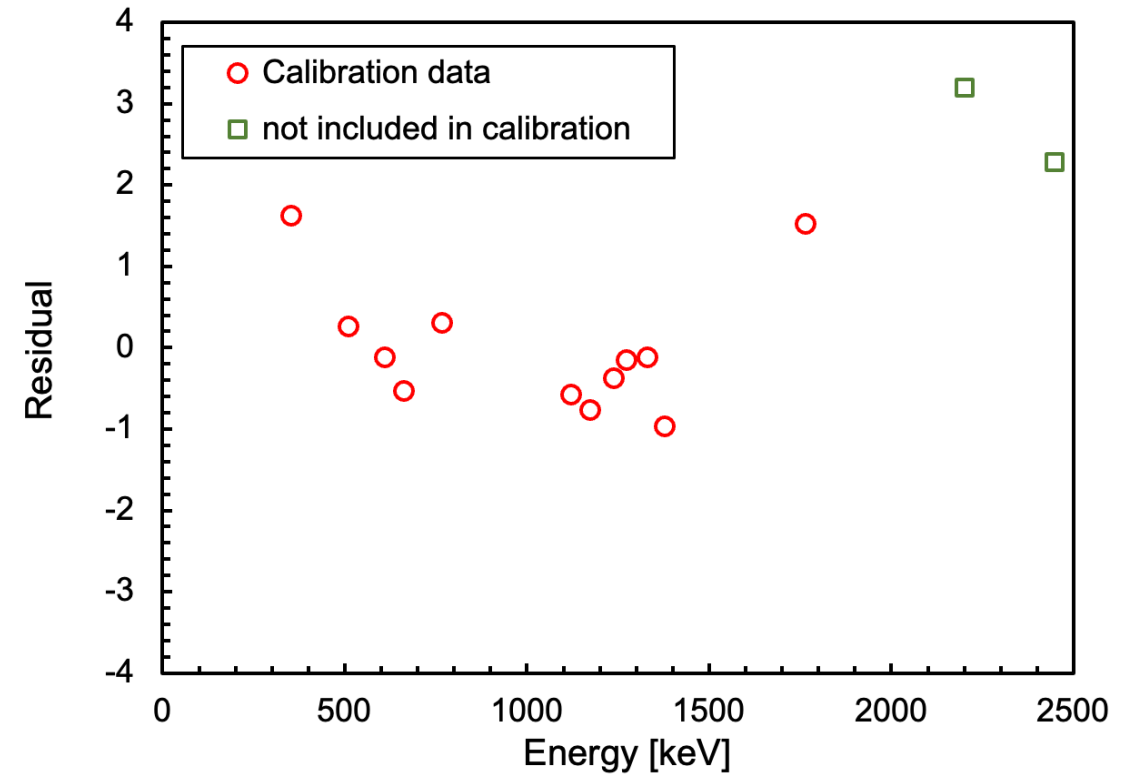
## Residuals

**CLEANDM**

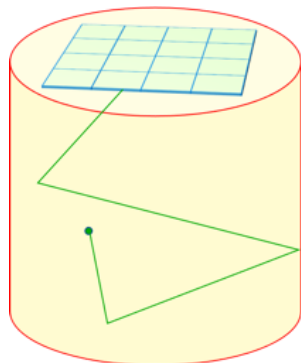
**PI3SO**



**SensL**

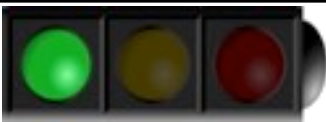


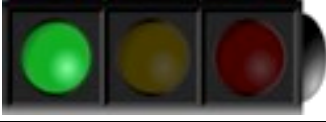
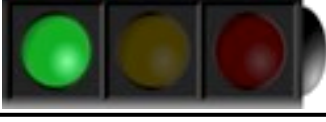


**Hamamatsu**



## Response linearity: $R^2$ from linear fit

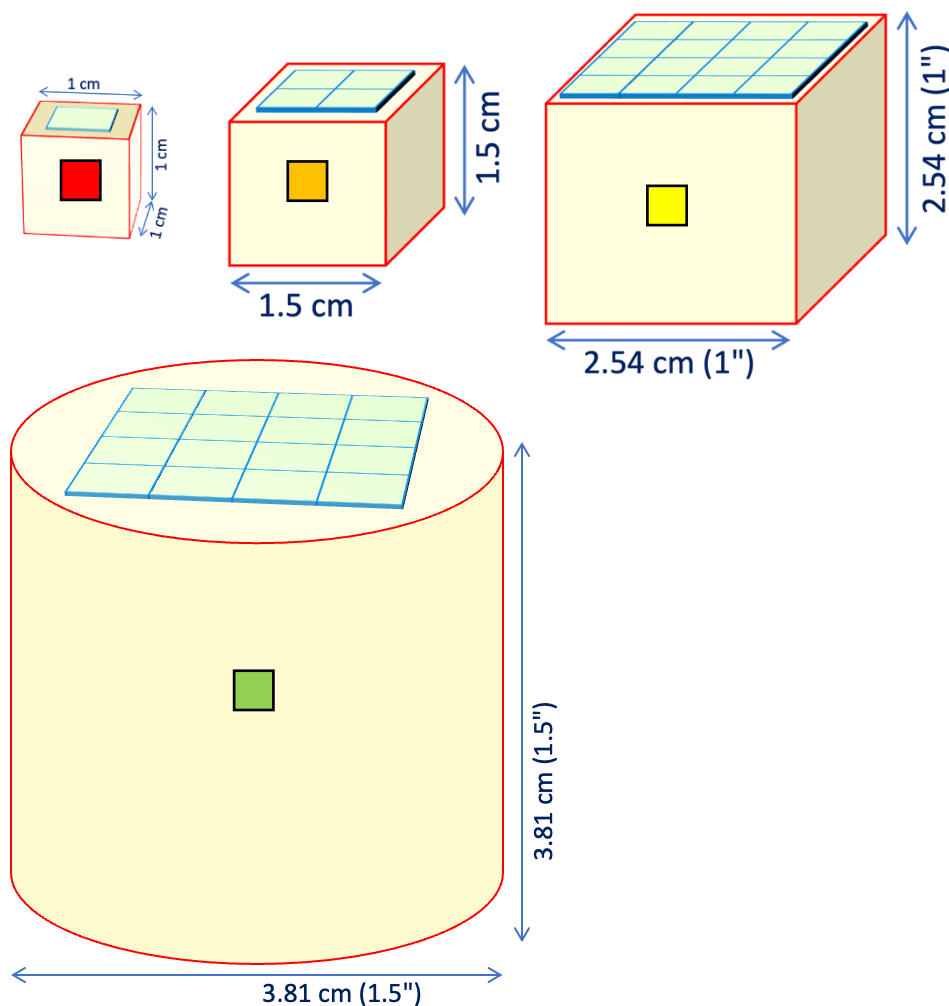
$R^2$

CsI(Tl) + SensL	1.0000		perfect
CsI(Tl) + Hamamatsu	1.0000		
LaBr3(Ce) + SensL	0.9998		very good, perfect E resolution
LaBr3(Ce) + Hamamatsu	0.9996		
CeBr3 + SensL	0.9997		very good, perfect E resolution
CeBr3 + Hamamatsu	0.9995		
BGO + SensL	1.0000		perfect but poor light yield
BGO + Hamamatsu	1.0000		
Nal + SensL	1.0000		perfect
Nal + Hamamatsu	1.0000		

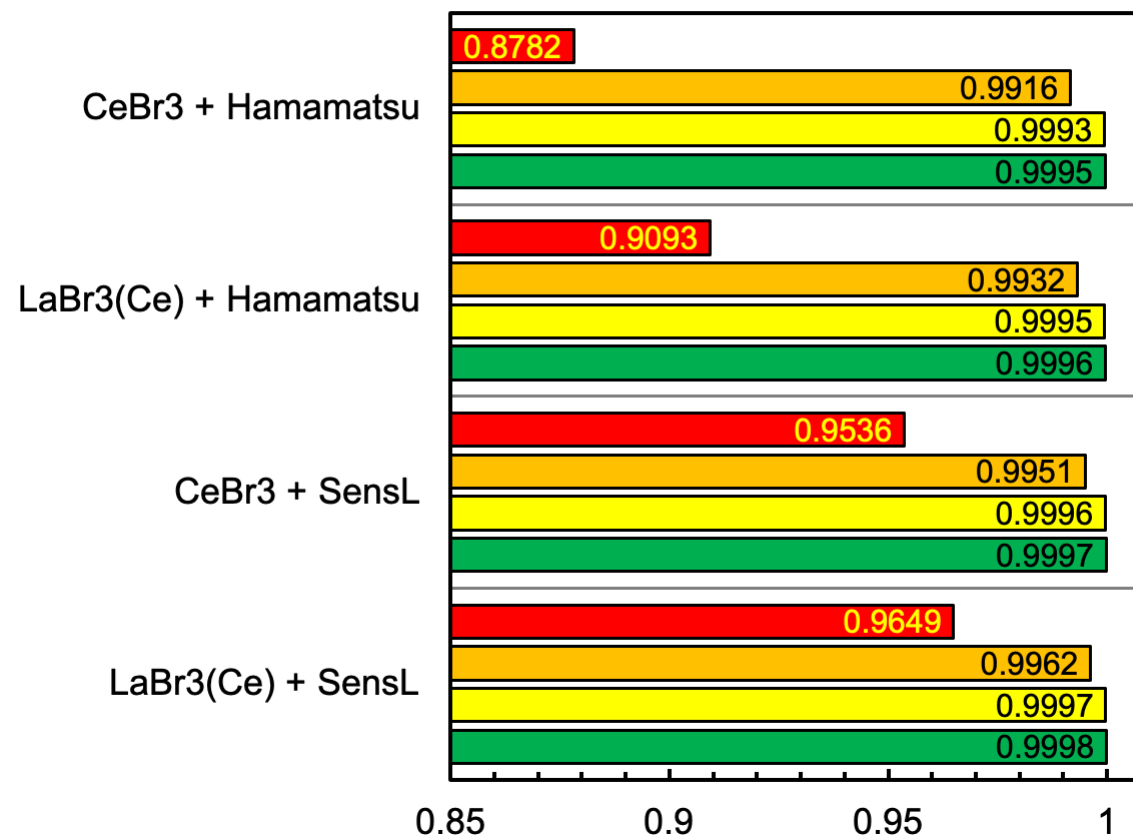
0.99

1

## Additional configurations investigated behavior with LaBr<sub>3</sub>(Ce) and CeBr<sub>3</sub>



- 1 cm cube, 1 SiPMs
- 1.5 cm cube, 4 SiPMs
- 2.54 cm cube, 16 SiPMs
- 3.81 cm cylinder, 16 SiPMs





## Summary

- ➡ Model and tools developed to quickly evaluate the response of SiPM \*
- ➡ Studied possible non-linearity of SensL and Hamamatsu 6mm × 6mm SiPMs when coupled to CsI(Tl), LaBr<sub>3</sub>(Ce), CeBr<sub>3</sub>, BGO, NaI, scintillators in different geometries and in arrays
- ➡ CsI(Tl) is the best candidate for small crystal and single SiPM, also good for bigger crystals
- ➡ Bigger crystals with 4 × 4 SiPM array perfect for LaBr<sub>3</sub>(Ce) and CeBr<sub>3</sub>

Paper submitted to Sensors  
Preprint available at <https://doi.org/10.20944/preprints202509.0685.v1>

\* The tools are available on request in form of MS Excel workbooks, just send me an email at [FINOCCHIARO@LNS.INFN.IT](mailto:FINOCCHIARO@LNS.INFN.IT)





Paper submitted to Sensors  
Preprint available at <https://doi.org/10.20944/preprints202509.0685.v1>

\* The tools are available on request in form of MS Excel workbooks,  
just send me an email at [FINOCCHIARO@LNS.INFN.IT](mailto:FINOCCHIARO@LNS.INFN.IT)

# THANK YOU