Magnetic and electric dipole moments of short-lived particles and proposal for their measurements with bent crystals at CERN

Alexander Yu. Korchin

National Science Center "Kharkiv Institute of Physics and Technology" & V.N. Karazin Kharkiv National University, Ukraine





Marian Smoluchowski Institute of Physics, Jagiellonian University, 16.12.2024

- Introduction: orbital and spin magnetic dipole moment (MDM)
- Electric dipole moment (EDM): violation of T- and CP-invariance
- $\bullet\,$ Short-lived charmed baryons with lifetime $\sim 10^{-13}$ s and their MDMs
- Precession of spin of a fermion in external magnetic and electric fields
- Feasibility of measuring magnetic and electric dipole moments of short-lived baryons using bent crystals
- Application to τ lepton from $D^+_s \to \tau^+ \nu_\tau$ decay
- Proposal for the LHC

First consider non-relativistic quantum mechanics based on **Schrodinger** equation. Hamiltonian of a particle in external electromagnetic field $A^{\mu} = (A^0, \vec{A})$ is

$$H = \frac{1}{2m}(\vec{p} - \frac{e}{c}\vec{A})^2 + eA^0 = \frac{\vec{p}^2}{2m} + eA^0 - \frac{e}{mc}\vec{A}\vec{p} + i\hbar\vec{\nabla}\vec{A} + \frac{e^2}{2mc^2}\vec{A}^2$$

If there is only constant magnetic field \vec{B} , then $A^0 = 0$, and $\vec{A} = \frac{1}{2}(\vec{B} \times \vec{r})$, and

$$H = \frac{\vec{p}^2}{2m} - \vec{\mu}_{orb} \vec{B} + \mathcal{O}(e^2)$$
$$\vec{\mu}_{orb} = \frac{e}{2m} (\vec{r} \times \vec{p}) = \frac{e}{2m} \vec{L},$$

where \vec{L} is the orbital moment. Like in classical electrodynamics, magnetic moment is determined by mechanical moment.

The spin magnetic moment does not appear in non-relativistic description.

Unification of special relativity and quantum mechanics.

The Dirac equation (linear in derivatives) for spin-1/2 fermion in external electromagnetic field $A^{\mu} = (A^0, \vec{A})$

$$i\frac{\partial}{\partial t}\psi = \left[c\vec{\alpha}\left(\vec{p} - \frac{e}{c}\vec{A}\right) + \beta mc^{2} + eA^{0}\right]\psi,$$

for the 4-component spinor $\psi = \begin{pmatrix} \varphi \\ \chi \end{pmatrix}$, and β and $\vec{\alpha}$ are 4 × 4 Dirac matrices. For non-relativistic velocities $v \ll c$, one can reduce Dirac equation to the Pauli equation for the 2-component spinor φ , using $\varphi \gg \chi$:

$$i\frac{\partial}{\partial t}\varphi = \left[\frac{1}{2m}(\vec{p} - \frac{e}{c}\vec{A})^2 + eA^0 - \frac{e\hbar}{2mc}\vec{\sigma}\vec{B}\right]\varphi$$

The important feature is appearance of the spin MDM

$$ec{\mu}_{spin} = 2 \, rac{e}{2m\,c} \, ec{S}, \qquad ext{where} \quad ec{S} = rac{\hbar}{2} ec{\sigma}$$

Magnetic moments in quantum physics: spin and MDM

The total magnetic moment is

$$ec{\mu}=ec{\mu}_{orb}+ec{\mu}_{spin}=rac{e}{2mc}(ec{L}+2ec{S})$$

It is customary to write the spin MDM in the form

$$ec{\mu}_{spin}=grac{e}{2mc}\,ec{S}=rac{g}{2}\,rac{e\hbar}{2mc}\,ec{\sigma},\qquad ext{with }g=2,$$

and g is called g-factor, or gyromagnetic factor. Usually the Bohr magneton is introduced

$$\mu_B \equiv \frac{|e|\hbar}{2mc}$$

which for the electron is $\mu_B \approx 0.927 \cdot 10^{-20} \, \frac{\text{erg}}{\text{Gauss}} = 2 \times 10^{-11} \, |\textbf{e}| \cdot \textbf{cm},$

Then the absolute value of MDM is measured in units of μ_B

$$\frac{\mu_{spin}}{\mu_B} = \frac{e}{|e|} \frac{g}{2}$$

For the point-like Dirac electron *g*-factor is equal to 2. However there are radiative corrections and possibly New Physics contributions. What do we know for leptons and quarks?

16 Dec 2024 5 / 40

Electron g-factor: experiment vs. theory for $\mu/\mu_B=g/2$



What can we say about agreement of theory with experiment?

Take the difference of central values and compare with total standard deviation σ

$$\Delta = \mu/\mu_B(exp) - \mu/\mu_B(theor) = 105 \times 10^{-1}$$
$$\sigma = \sqrt{\sigma_{theor}^2 + \sigma_{exp}^2} = 82 \times 10^{-14}$$

6 / 40

Since $\Delta = 1.28 \sigma$ agreement of QED with measurement for electron is indeed good.

Muon g - 2: experiment vs. theory

Introduce $a \equiv \frac{1}{2}(g-2)$, which is anomalous magnetic moment. Below is $a \times 10^{10}$.

	2011		2017 *to be discussed
QED	11658471.81 (0.02)	\longrightarrow	11658471.90 (0.01) [Phys. Rev. Lett. 109 (2012) 111808]
EW	15.40 (0.20)	\longrightarrow	15.36 (0.10) [Phys. Rev. D 88 (2013) 053005]
LO HLbL	10.50 (2.60)	\rightarrow	9.80 (2.60) [EPJ Web Conf. 118 (2016) 01016]*
NLO HLbL			0.30 (0.20) [Phys. Lett. B 735 (2014) 90]*
	HLMNT11		<u>KNT17</u>
LO HVP	694.91 (4.27)	\longrightarrow	692.23 (2.54) this work*
NLO HVP	-9.84 (0.07)	\longrightarrow	-9.83 (0.04) this work*
NNLO HVP			1.24 (0.01) [Phys. Lett. B 734 (2014) 144] *
Theory total	11659182.80 (4.94)	\longrightarrow	11659181.00 (3.62) this work
Experiment			11659209.10 (6.33) world avg
Exp - Theory	26.1 (8.0)	\longrightarrow	28.1 (7.3) this work
Δa_{μ}	3.30		3.9σ this work

To compare theory and experiment calculate

$$\Delta = a(exp) - a(theor) \approx 28.1 \times 10^{-9}$$
$$\sigma = \sqrt{\sigma_{theor}^2 + \sigma_{exp}^2} = 7.3 \times 10^{-9}$$

We see that $\Delta = 3.9 \sigma$ which means a big disagreement for the muon α

16 Dec 2024 7 / 40



Comparison of theoretical predictions for the muon with experiment (From G. Colangelo et al., Prospects for precise predictions of a_{μ} in the Standard Model, arXiv 2203.1581 [hep-ph]).

16 Dec 2024 8 / 40

Quark magnetic moment

Because of the quark confinement one cannot measure MDM of a free quark, but only for quarks inside baryons or mesons.

In general, for a quark like for any fermion we define

$$u_q = \frac{|e| Q_q \hbar}{2m_q c} \frac{g_q}{2}$$

 g_q - is quark gyromagnetic factor, $Q_q = +2/3$ for u, c, t and $Q_q = -1/3$ for d, s, b. For a point-like Dirac quark $g_q = 2$, however there are radiative corrections similarly to electron and muon, but with the strong coupling constant α_s .



For example, for the charm quark $\alpha_s(m_c) = 0.3378 \gg \alpha_{em} \approx 0.0073$, and the radiative corrections to g_c up to 3 loops [Grozin et al., 2008] are

$$a_c \equiv rac{g_c}{2} - 1 = +0.0717 + 0.07995 + 0.1137 + \mathcal{O}(lpha_s^4) = 0.2655 + \mathcal{O}(lpha_s^4)$$

Unfortunately, there is no convergence in α_s expansion, so the result cannot be reliable α_{\circ}

16 Dec 2024 9 / 40

Electric dipole moment (EDM)

EDM is even more interesting and intriguing characteristic of a particle, because for particle at rest the only vector available is its spin:

$$ec{\mu}\simec{S}, \qquad ec{d}\simec{S}$$

The magnetic moment and magnetic field \vec{B} behave similarly with respect to space reflection \hat{P} :

$$\hat{P}: \quad \vec{\mu} \to \vec{\mu}, \quad \vec{B} \to \vec{B},$$

and time inversion \hat{T} :

$$\hat{T}:$$
 $\vec{\mu} \to -\vec{\mu},$ $\vec{B} \to -\vec{B},$

Therefore Hamiltonian $H_{mag} = -\vec{\mu} \cdot \vec{B}$ is invariant under \hat{P} and \hat{T} transformations.

However, the electric dipole moment and electric field behave differently under space reflection $\hat{P}:$

 $\hat{P}: \quad \vec{d} \to \vec{d}, \quad \vec{E} \to -\vec{E},$

and time inversion \hat{T} :

$$\hat{T}: \vec{d} \to -\vec{d}, \quad \vec{E} \to \vec{E},$$

Therefore Hamiltonian $H_{elec} = -\vec{d} \cdot \vec{E}$ violates both \hat{P} and \hat{T} .

Parity is violated in weak interactions. But if time inversion \hat{T} is violated, then due to *CPT* theorem [J. Schwinger 1951, G. Luders 1952, W. Pauli 1957], *CP* symmetry should also be violated if EDM is not zero.

A. Korchin (KIPT & KhNU) Dipole moments of short-lived particles

16 Dec 2024 10 / 40

Electric dipole moment (EDM) of particles



Search for sources of CP violation is important, in particular, because it is related to the problem of matter-antimatter asymmetry in the Universe.

One of the conditions in Sakharov's critaria is violation of *CP* symmetry (in fact, there is *CP* violation in SM due to CKM quark-mixing matrix, but the effect is many orders of magnitude below what is needed [Farrar, Shaposhnikov, 1994]), $\mathbb{R} \to \mathbb{R} \to \mathbb{R}$

16 Dec 2024 11 / 40

EDM of leptons and quarks

For leptons and quarks one can define EDM

$$d=\frac{|e|Q}{2m}\frac{\eta}{2}$$

where η is analogue of *g*-factor for MDM.

What is known at present? There are no direct measurements of EDM. Theoretically, *d* for leptons is not zero but extremely small because of the 4-loop diagrams in the Standard Model. EDM usually scales with mass, for example

$$d_ au \sim d_e \, rac{m_ au}{m_e} pprox$$
 3500 d_e

	experiment: <i>d</i> , <i>e</i> · <i>cm</i> [PDG]	SM prediction: d , $ e \cdot cm$
electron	$< 0.11 imes 10^{-28}$	$\sim 10^{-45}$
muon	$< 1.8 imes 10^{-19}$	$\sim 10^{-42}$
au lepton	$(-0.22,+0.45) imes 10^{-16}$ (real)	$\sim 10^{-41}$
	$(-0.25,+0.0080) imes 10^{-16}$ (imaginary)	
neutron	$< 3 imes 10^{-26}$	$(1-6) imes 10^{-32}$
charm quark	not known	?

12 / 40

Status of EDM for various particles



Overall status of EDM measurements (from J. Beacham et al., Physics beyond colliders at CERN ... , J. Phys. G: Nucl. Part. Phys. 47 (2019) 010501).

Red area - current measurement, orange - foreseen measurement,

purple - SM prediction due to CP violation in Cabibbo-Kobayashi-Maskawa matrix,

grey bars - from CP violation in QCD (θ_{QCD} assuming maximal possible consistent with neutron EDM),

white regions show discovery regions for experiments.

Relatively long-lived baryons with $au \sim 10^{-10}$ s

For the light baryons, consisting of u, d, s quarks, the MDMs are given in units of nuclear magneton $\mu_N = \frac{e\hbar}{2m_nc}$, so that $g/2 = \mu/\mu_N$.

Magnetic Moments of Baryons

Baryon	$\mu/\mu_{ m N}$ (E	xperiment)	Quark model:	$\mu/\mu_{ m N}$
Р	+2.792 847 386	6 ± 0.000000063	$(4\mu_{ m u}-\mu_{ m d})/3$	
n	-1.913 042 75	$\pm \ 0.000\ 000\ 45$	$(4\mu_{ m d}-\mu_{ m u})/3$	
Λ^0	-0.613	± 0.004	$\mu_{ m s}$	
Σ^+	+2.458	± 0.010	$(4\mu_{ m u}-\mu_{ m s})/3$	+2.67
Σ^0			$(2\mu_{\rm u} + 2\mu_{\rm d} - \mu_{\rm s})/3$	+0.79
$\Sigma^0 \to \Lambda^0$	-1.61	± 0.08	$(\mu_{\rm d}-\mu_{\rm u})/\sqrt{3}$	-1.63
Σ-	-1.160	± 0.025	$(4\mu_{ m d}-\mu_{ m s})/3$	-1.09
Ξ^0	-1.250	± 0.014	$(4\mu_{ m s}-\mu_{ m u})/3$	-1.43
Ξ~	-0.650~7	$\pm~0.002~5$	$(4\mu_{ m s}-\mu_{ m d})/3$	-0.49
Ω^{-}	-2.02	± 0.05	$3\mu_{ m s}$	-1.84

The masses of constituent quarks here are: $m_u = m_d = 336$ MeV $m_s = 538$ MeV $m_s = 538$ MeV $m_s = 538$

14 / 40

A. Korchin (KIPT & KhNU) Dipole moments of short-lived particles 16 Dec 2024

Charmed baryons

Charmed baryons include charm quark(s) with electric charge $\frac{2}{3}|e|$ and mass $m_c = 1.27$ GeV.

Baryon	Flavor	$SU(3)_f$	Charm	Mass (MeV)	Cross sec	tion, μ b	Life-length $c\tau$,
	content				fixed targ.	collider	or width Γ
Λ_c^+	[ud]c	3	1	2286.5 ± 0.1	10.13	758.1	$60.0\pm1.2\mu{ m m}$
Ξ_c^+	[us]c	3	1	2467.9 ± 0.2	0.588	65.5	$132.5\pm7.8\mu{ m m}$
Ξ_c^0	[ds]c	3	1	2470.9 ± 0.3	0.510	65.6	$33.6\pm3.6\mu{ m m}$
Σ_{c}^{++}	иис	6	1	2454.0 ± 0.1	0.863	42.0	$1.9\pm0.1\text{MeV}$
Σ_c^+	{ud}c	6	1	2452.9 ± 0.4	0.697	42.2	< 4.6 MeV
Σ_c^0	ddc	6	1	2453.8 ± 0.1	0.461	41.6	$1.8\pm0.1{ m MeV}$
$\Xi_c^{\prime+}$	{ <i>us</i> } <i>c</i>	6	1	2578.4 ± 0.5	0.083	6.3	_
$\Xi_c^{\prime 0}$	$\{ds\}c$	6	1	2579.2 ± 0.5	0.072	6.6	-
Ω_c^0	SSC	6	1	2695.2 ± 1.7	0.028	3.0	$80.3\pm10\mu{ m m}$
Ξ_{cc}^{++}	сси	3	2	3621.4 ± 0.8	$< 10^{-4}$	$\sim 10^{-3}$	$76.7\pm10\mu{ m m}$
Ξ_{cc}^+	ccd	3	2	3518.9 ± 0.9	$< 10^{-4}$	$< 10^{-3}$	-
Ω_{cc}^{+}	ccs	3	2	-	$< 10^{-4}$	$\sim 10^{-3}$	_

Here [ud] means antisymmetric, {ud} means symmetric. We would like to study baryons which have lifetime $\sim 10^{-13}$ s, or $c\,\tau\sim 100~\mu\text{m}$, and also

- have the largest production cross sections,
- are positively charged (for channeling in crystals),
- their magnetic moment is equal to magnetic moment μ_c of the charm quark, $\lambda_{\rm magnetic}$

A. Korchin (KIPT & KhNU) Dipole

16 Dec 2024 15 / 40

MDM of charmed baryons in constituent quark model

For calculation of MDM only the spin-flavor wave functions are important:

$$|\Lambda_{c}^{+}([ud]c); \frac{1}{2}, \uparrow\rangle = \frac{1}{\sqrt{2}}(ud - du)c \times \frac{1}{\sqrt{2}}(\uparrow\downarrow - \downarrow\uparrow)\uparrow$$

 $|\Sigma_{c}^{+}(\{ud\}c); \frac{1}{2}, \uparrow\rangle = \frac{1}{\sqrt{2}}(ud + du)c \times \frac{1}{\sqrt{6}}\{2\uparrow\uparrow\downarrow - (\downarrow\uparrow + \uparrow\downarrow)\uparrow\}, \quad \text{etc. for all baryons}$

These wave functions allow one to find MDM of all charmed baryons:

$$\begin{split} \mu(\Lambda_c^+) &= \mu(\Xi_c^+) = \mu(\Xi_c^0) = \mu_c, \\ \mu(\Sigma_c^{++}) &= \frac{1}{3}(4\mu_u - \mu_c), \qquad \mu(\Sigma_c^+) = \frac{1}{3}(2\mu_u + 2\mu_d - \mu_c), \\ \mu(\Sigma_c^0) &= \frac{1}{3}(4\mu_d - \mu_c), \qquad \mu(\Xi_c^{\prime+}) = \frac{1}{3}(2\mu_u + 2\mu_s - \mu_c), \quad \text{etc. for all} \end{split}$$

We see that MDM of two baryons are equal to MDM of the charm quark:

$$\mu(\Lambda_c^+) = \mu(\Xi_c^+) = \mu_c, \text{ where } \mu_c = \frac{|e|\hbar}{3m_c c} \frac{g_c}{2}$$

16 / 40

that can give information on the g-factor of the charm quark, at least approximately.

Precession of spin in external magnetic and electric fields

How to measure MDM/EDM of particles which live such a short time $\tau_{\Lambda_c} \sim 2 \times 10^{-13}$ s?

First, we need to accelerate it to increase its lifetime and the distance it passes, $L = \gamma v \tau_0$.

For the LHC, the energy is a few TeV, then Lorentz factor $\gamma = E/m_{\Lambda_c} \sim 10^3$, and the length can be macroscopic, $L \sim 10$ cm.

Next one can use phenomenon of spin precession in external fields.

In the rest frame of particle the vector of spin (or one can say about polarization $\vec{\mathcal{P}} = \frac{2}{\hbar} < \vec{S} >$) satisfies

$$rac{dS}{dt^*} = ec{\mu} imes ec{B}^* + ec{d} imes ec{E}^*,$$

where \vec{B}^* and \vec{E}^* are magnetic and electric fields in the **rest frame** and t^* is the proper time. Both $\vec{\mu}$ and \vec{d} are proportional to \vec{S} .

If, for example, $\vec{B}^* \neq 0$ and $\vec{E}^* = 0$, then the spin rotates around the magnetic field with the angular velocity

$$\omega = \frac{eB^*}{mc} \frac{g}{2}$$

Precession of spin in external fields

One needs description of spin precession for a fermion moving with ultrarelativistic energies with Lorentz factor $\gamma \gg 1$.

Theory:

L.H. Thomas, Nature 117, 514 (1926)

V. Bargmann, L. Michel, V.L. Telegdi, Phys. Rev. Lett. 2, 435 (1959)
J.D. Jackson, "Classical electrodynamics", sec. 11.11, John Wiley, 3rd ed., 1999
V.B. Beresteckii, E.M. Lifshitz, L.P. Pitaevskii, "Quantum electrodynamics", sec. 41, 1982
V. Lyuboshits, Yad. Fiz. 31 (1980) 986; I. Kim, Nucl. Phys. B229 (1983) 251
V.G. Baryshevsky, Phys. Lett. B757 (2016) 426

One transforms $\vec{B}^* \to \vec{B}$ and $\vec{E}^* \to \vec{E}$ from the rest frame to Lab frame:

$$\vec{B}^{\star} = \gamma (\vec{B} - \frac{\vec{v} \times \vec{E}}{c}) - \frac{\gamma^2}{1+\gamma} \frac{\vec{v}(\vec{v}\vec{B})}{c^2}$$
$$\vec{E}^{\star} = \gamma (\vec{E} + \frac{\vec{v} \times \vec{B}}{c}) - \frac{\gamma^2}{1+\gamma} \frac{\vec{v}(\vec{v}\vec{E})}{c^2}$$

and also transforms the time $t^* \rightarrow t = \gamma t^*$. In addition, a non-inertial frame of moving particle is accounted for by the Thomas correction [L.H. Thomas, 1927]:

$$rac{\gamma^2}{1+\gamma}rac{ec{S} imes(ec{v} imesec{a})}{c^2}$$

 $\vec{a} = \frac{d\vec{v}}{dt}$ is acceleration of a particle.

ヘロト 不得下 不足下 不足下 一足

Precession of spin in external fields

Now let us write equation of motion in external fields of a charged particle with charge Q:

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{Q}{m\gamma} \left(\vec{E} + \frac{\vec{v} \times \vec{B}}{c} - \frac{\vec{v}(\vec{v}E)}{c^2} \right) = \vec{\omega}_0 \times \vec{v} + \frac{Q}{m\gamma} \frac{1}{\gamma^2 - 1} \frac{\vec{v}(\vec{v}E)}{c^2},$$
$$\vec{\omega}_0 = \frac{Q}{mc\gamma} \left(\frac{\gamma^2}{\gamma^2 - 1} \frac{\vec{v} \times \vec{E}}{c} - \vec{B} \right) \quad \text{angular velocity of rotation of particle velocity}$$

The final equations for the spin precession in Laboratory frame

$$\begin{split} & \frac{d\vec{S}}{dt} = \vec{\Omega} \times \vec{S}, \\ & \vec{\Omega} = \vec{\omega}_{MDM} + \vec{\omega}_{EDM}, \\ & \vec{\omega}_{MDM} = \vec{\omega}_B + \vec{\omega}_E, \\ & \vec{\omega}_B = -\frac{Q}{mc} \Big[\Big(\frac{g}{2} - 1 + \frac{1}{\gamma} \Big) \vec{B} - \Big(\frac{g}{2} - 1 \Big) \frac{\gamma}{1 + \gamma} \frac{\vec{v}(\vec{B} \vec{v})}{c^2} \Big], \\ & \vec{\omega}_E = -\frac{Q}{mc} \Big(\frac{g}{2} - \frac{\gamma}{1 + \gamma} \Big) \frac{\vec{E} \times \vec{v}}{c}, \\ & \vec{\omega}_{EDM} = -\frac{\eta Q}{2mc} \Big[\vec{E} + \frac{\vec{v} \times \vec{B}}{c} - \frac{\gamma}{1 + \gamma} \frac{\vec{v}(\vec{v}E)}{c^2} \Big] \end{split}$$

16 Dec 2024 19 / 40

Rotation of spin (polarization vector) in a bent crystal

Here $\vec{\xi_i}$ is initial polarization, $\vec{\xi_f}$ is final polarization,

 Θ_{μ} is rotation angle of the polarization and Θ is rotation angle of the momentum.



The gradient of the inter-plane electric field of a silicon crystal reaches the maximum value about 5 GeV/cm. This corresponds to the induced magnetic field in the instantaneous rest frame of a particle

$$ec{B}^* = \gamma \left(rac{ec{v}}{c} imes ec{E}
ight) \sim 1000 ext{ Tesla},$$

if the particle moves with relativistic energies about TeV.

With Lorentz factor $\gamma \sim 10^3$ the particle can move ~ 10 cm in a crystal before the decay, $_{\odot}$

20 / 40

Channeling of particle in electric field of bent crystal

cente

Spin precession in electric field of bent crystal

In a bent crystal there is strong electric field \vec{E} , perpendicular to velocity of particle, $\vec{E} \perp \vec{v}$, so that the energy of particle is conserved and it moves with constant velocity $|\vec{v}| \sim c$.

The component of electric field is along OX and particle velocity along OZ, then momentum of particle rotates with angular velocity around OY:

$$\omega_0 = \frac{QE}{m\gamma v} = \frac{v}{R},$$

where R is the curvature radius of a crystal.

Then the spin rotation velocity due to MDM is also along OY and is equal to

$$\omega_{MDM} = \gamma \,\omega_0 \, (\frac{g}{2} - 1 - \frac{g}{2\gamma^2} + \frac{1}{\gamma}) \approx \gamma \,\omega_0 \, (\frac{g}{2} - 1) = \gamma \,\omega_0 \, a$$

where $a \equiv g/2 - 1$ is anomalous magnetic moment.

The spin rotation velocity due to EDM is along different axis, OX:

$$\omega_{\rm EDM} = \gamma \,\omega_0 \, \frac{\eta q}{2c}$$

So that the total vector of angular velocity of the spin rotation is

$$\vec{\Omega} = \vec{n}_x \, \omega_{EDM} - \vec{n}_y \, \omega_{MDM}$$

Spin precession in electric field of bent crystal

Integration over time leads to relations for the angle of spin rotation

$$\vec{\Phi} = \theta' \vec{n}_{x} - \theta \vec{n}_{y}, \theta \approx \gamma \theta_{0} a, \qquad \theta' = \gamma \theta_{0} \frac{\eta v}{2c}$$

The rotation angle of the velocity is $\theta_0 = L/R$, where L is the arc length that baryon passes in the channeling regime, and R is curvature of the crystal.

What is the typical rotation angle θ_0 of the particle trajectory, if velocity $v \sim c$? Take $L \approx 10$ cm and curvature radius of crystal $R \approx 10$ m. Then

$$\theta_0 = \frac{L}{R} = \frac{v t}{R} = \frac{v \gamma \tau_0}{R} \sim \frac{10 \, cm}{10 \, m} \sim 10 \, \mathrm{mrad} \approx 0.6^\circ$$

Now we estimate the rotation angle of the spin. Assume that there is MDM (no EDM) and take $a \sim 0.01$. Then

$$heta pprox \gamma \, heta_{
m 0} \, {
m a} \sim 10^{
m 3} imes 0.6^{\circ} imes 0.01 pprox 6^{\circ}$$

Even small a is enhanced by very large Lorentz factor γ . If we measure θ and know θ_0 , then g-factor can be found.

After particle's passing the crystal, the polarization vector acquires the components which depend on initial polarization $\bar{\xi_i}$ and rotation angles θ and θ' . If crystal is oriented perpendicular to initial polarization and $\theta' \ll \theta$, then initial polarization is along *OX*, and final one has the components

$$ec{\xi_i} = \xi_i \, ec{n_x} \implies ec{\xi_f} pprox \xi_i \, (\cos heta \, ec{n_x} + \sin heta \, ec{n_z}) pprox \xi_i \, (ec{n_x} + heta \, ec{n_z}), \qquad (ext{if } heta \, ext{is small})$$

which can be used to determine MDM and $a = g/2 - 1 \sim \theta$.

Measurement of EDM is more tricky, because this effect is expected to be much smaller than effect of MDM.

One possibility would be to rotate the crystal with respect to the beam, then component OY of initial polarization arises

$$ec{\xi_i} = \xi_i' \ ec{n_y} \implies ec{\xi_f} pprox \xi_i' \left(rac{ heta'}{ heta} (\cos heta - 1) \ ec{n_x} + ec{n_y} + rac{ heta'}{ heta} \sin heta \ ec{n_z}
ight) pprox \xi_i' \left(ec{n_y} + heta' \ ec{n_z}
ight)$$

which can be convenient for measurement of EDM and $\eta \sim \theta'.$

Fermilab experiment of 1992

Method was tested at Fermilab in 1992 for $\Sigma^+(uus)$ baryon with lifetime $\approx 10^{-10}$ s.



16 Dec 2024 25 / 40

Concept of possible experiment at CERN



Published for SISSA by 2 Springer

Received: May 10, 2017 Revised: July 5, 2017 Accepted: July 13, 2017 Published: August 28, 2017

Feasibility of measuring the magnetic dipole moments of the charm baryons at the LHC using bent crystals

A.S. Fomin,^{a,b,c} A.Yu. Korchin,^{b,c} A. Stocchi,^a O.A. Bezshyyko,^d L. Burmistrov,^a S.P. Fomin,^{b,c} I.V. Kirillin,^{b,c} L. Massarcire^r, A. Natochii,^{a,d} P. Robbe,^a W. Scandale^{a,f,d} and N.F. Shul'ga^{b,c}



Polarization of Λ_c^+ coming in a crystal



Left: polarisation of $\Lambda_c^+(udc)$ as a function of its p_T measured by the E791 experiment (E.M. Aitala et al. Phys. Lett. B 471 (2000) 449).

Right: polarization of $\Lambda(uds)$ hyperon as a function of x_F (LHCb, ATLAS, HERA, ...).

How to determine final Λ_c^+ polarization?

Slide from presentation of Achille Stocchi

Polarisation (${\cal P}$) of Λ c and weak asymmetry decay parameter (lpha)

₽ (Λc)

<u>The polarisation</u> \mathcal{P} <u>of Ac has not been yet measured precisely.</u> There are some old experiment and the indicative values are $\mathcal{P}(\Lambda_c) \approx [0.4-0.6]$ ($\mathcal{P}(\Lambda_c) \approx 0.6$ (e.g. Bis-2) P (Ac) ~ 0.6
To be also measured by this experiment

α	The pa				
cha	nnel	Br		α	~
$(\Lambda_c \rightarrow \Lambda \pi) \times Br$	(A → pπ)	1,07% x 64 % ~ 0,007	~ 1	0.59	u input parameter
$(\Lambda_c \rightarrow \Lambda \pi) \times Br$	(Λ → n π⁰)	1,07% x 35,8 % ~ 0,004	~ 0.6	0.59	input parameter
$(\Lambda_c \rightarrow \Sigma^+ \pi^0) \times I$	Br(Σ+→p π ⁰)	1,00% x 51,5 % ~ 0,005	~ 0.7	0.44	
$(\Lambda_c \rightarrow \Sigma^+ \pi^0) X$	Br(Σ+→n π+	1,00% x 48,3 % ~ 0,005	~ 0.6	~0	For the numerical study
$(\Lambda_c \rightarrow \Lambda ev) X$	$Br(\Lambda \rightarrow p \pi)$	2,00% x 64 % ~ 0,0128	~ 1.8	0.60	we use
$(\Lambda_c \rightarrow \Lambda \mu \nu) X$	$Br(\Lambda \rightarrow p \pi)$	2,00% x 64 % ~ 0,0128	~ 1.8	0.60	🗭 (Λc)x α~ 0.6x0.59 ~ 0.35
$(\Lambda_c \rightarrow p K^- \pi^+)$)	5,00% ~ 0,05	~12.5	not know	n

Two observations :

1) Consider that the sensitivity of the analysis goes as $(\mathbf{P} \times \alpha)^2$

2) More decay channels can be use. In particular if the α parameter of $\Lambda_c \rightarrow p K^-\pi^+$ decay mode is measured and happened to be large, it would allow to give access to much larger statistics. Possible at LHCb !

16 Dec 2024 28 / 40

Feasibility of MDM/EDM measurement for au lepton



Published for SISSA by 🖄 Springer

RECEIVED: October 17, 2018 REVISED: January 17, 2019 ACCEPTED: March 12, 2019 PUBLISHED: March 26, 2019

29 / 40

Feasibility of τ -lepton electromagnetic dipole moments measurement using bent crystal at the LHC

A.S. Fomin,^{*a,b*} A.Yu. Korchin,^{*a,c*} A. Stocchi,^{*d*} S. Barsuk^{*d*} and P. Robbe^{*d*}

Tau-lepton is a short-lived fermion with lifetime 2.9×10^{-13} s. How to produce polarized τ ? One can take charm-strange meson $D_s^+ = (c \bar{s})$ with sizable branching fraction (5.5%) of the decay

$$D_s^+ o au^+ +
u_{ au}$$

 D_s^+ mesons are produced in the *pp* collisions at the LHC with very high energies, of a few TeV, and then decay to **100 % polarized** τ **leptons.**

Measurement of MDM and EDM for τ -lepton

Then τ leptons can be directed into a bent crystal, get in the channeling regime, and the direction of τ polarization after the spin precession in the crystal can be determined from angular analysis of its decay products. Schematically

 $p + p \rightarrow D_s^+ + X \rightarrow \tau^+ + \nu_\tau + X \rightarrow \tau^+$ in a crystal $\rightarrow \pi^+ + \pi^+ + \pi^- + \nu_\tau$

Double-crystal setup is proposed by Alex Fomin (IJClab & CERN). Optimal parameters: 1st crystal – silicon (L = 4.5 cm, R = 15 m) or germanium (L = 3 cm, R = 10 m); 2nd crystal – germanium (L = 10 cm, R = 7 m).



30 / 40

Polarization of au in the weak decay $D_s^+ ightarrow au^+ u_ au$

Behavior of polarization vector of $\boldsymbol{\tau}$ in Lab frame is complicated, depending on kinematics.



A. Korchin (KIPT & KhNU)

Dipole moments of short-lived particles

What can we expect in measurements?

Absolute statistical error of the measured anomalous MDM of the τ lepton $a_{\tau} = \frac{1}{2}(g_{\tau} - 2)$ as a function of the total number of protons on target N_{POT} . The green lines show the limits of the DELPHI collaboration (LEP) and expected for the experiment at BELLE 2.



Red line is the SM prediction: $a_{\tau} = 1.17721(5) \times 10^{-3}$ [Eidelman, Passera, 2007].

Possible layout of experiment at the LHC

Feasibility of measuring the magnetic and electric dipole moments of the short-lived particles at the LHC



A.S. Fomin, A.Yu. Korchin, A. Stocchi, O.A. Bezshyyko, L. Burmistrov, S.P. Fomin, I.V. Kirillin, L. Massacrier, A. Natochii, P. Robbe, W. Scandale, N.F. Shul'ga, [arXiv:1705.03382] JHEP 08 (2017) 120 [inSPIF

- A.S. Fomin, Ph.D. thesis, Paris-Sud University, Paris France, (2017) [full text]
- A.S. Fomin, A. Yu. Korchin, A. Stocchi, S. Barsuk, P. Robbe, [arXiv:1810.06699] (2018), JHEP 1903 (2019) 156 [inSPIRE]
- D. Mirarchi, A.S. Fomin, S. Redaelli, W. Scandale, [arXiv:1906.08551] (2019) (submitted to EPJ C) [inSPIRE]
- A.S. Fomin, S. Barsuk, A.Yu. Korchin, V.A. Kovalchuk, E. Kou, M. Liul, A. Natochii, E. Niel, P. Robbe, A. Stocchi, [arXiv:1909.04654] (2019), (submitted to EPJ C) [inSPIRE]

イロト イ理ト イヨト イヨト

Preliminary proposal of \sim 2020

Any direct measurement of MDM/EDM of short-lived charmed baryons, beauty baryons would be the first one.

Collaboration 2019-2020: Orsay (LAL and Paris-Sud University) & CERN & Kharkiv (KIPT and V.N. Karazin University) & Kyiv (T. Shevchenko University) & Rome (INFN)

- A.S. Fomin, A.Yu. Korchin, A. Stocchi, O.A. Bezshyyko, L. Burmistrov, S.P. Fomin, I.V. Kirillin, L. Massacrier, A. Natochii, P. Robbe, W. Scandale, N.F. Shul'ga, *JHEP 08* (2017) 120
- A.S. Fomin, A.Yu. Korchin, A. Stocchi, S. Barsuk, P. Robbe, JHEP 03 (2019) 156
- A.S. Fomin, S. Barsuk, A.Yu. Korchin, V.A. Kovalchuk, E. Kou, M. Liul, A. Natochii, E. Niel, P. Robbe, A. Stocchi, *Eur. Phys. J. C* 80 (2020) 358
- A.Yu Korchin, V.A. Kovalchuk. Int. J. Mod. Phys. A 35 (2020) 11n12, 2050060
- D. Mirarchi, A.S. Fomin, S. Redaelli, W. Scandale, Eur. Phys. J C 80 (2020) 10, 929
- A.S. Fomin, Ph.D Thesis, Paris-Sud University, France, 2017
- A.S. Fomin et al. "Electromagnetic dipole moments of unstable particles", Milano, Italy, 2-4 October 2019
- A.S. Fomin et al. FTE@LHC and NLOAccess STRONG 2020 joint kick-off Meeting, CERN, Geneva, 7-8 November 2019
- ...

< ロト < 同ト < ヨト < ヨト

Slide from presentation of Nicola Neri in CERN meeting 28-29 Feb 2024

Direct measurement of dipole moments of short-lived particles at LHC



Nicola Neri UniMi and INFN Milano/CERN

on behalf of the proto-collaboration

LHCC meeting CERN, 28-29 February 2024

ALADDIN: letter of intent



LETTER OF INTENT ALADDIN: An Lhc Apparatus for Direct Dipole moments INvestigation Submitted to the LHCC on 24 July 2024

K. Akiba¹, F. Alessio², M. Benettoni³, A. Bizzeti^{323,4}, F. Borgato^{3,4}, F. Bucci³², R. Cardinale^{5,6}, S. Cesar^{7,8}, M. Citterio⁸, V. Coco², S. Coelli⁸, P. Collin^{5,2}, E. Dall'Occo³, M. Ferro-Luzzi², A. Fomin², R. Forry², J. Fu¹⁰, P. Gandini⁸, M. Giorqi^{11,12}, J. Grabowsl¹³, S. J. Jaimes Elles¹⁴, S. Jakobsen², F. Kou²¹, G. Lamanna^{11,12}, H. B. Li^{10,16}, S. Libraton¹⁴, D. Marangouto^{7,8}, F. Marinez Vilad¹⁴, J. Mazorra de Cos¹⁴, A. Merl¹⁵, H. Miao^{10,16}, N. Neri^{7,8}, S. Neuber¹³, A. Perrolin^{5,6}, A. Pillon¹¹, J. J. Finzio^{10,2}, M. Preru¹⁰, P. Robbe²¹, L. Rossi^{7,8}, J. Ruiz-Vidal^{14,2}, I. Sanderswood¹⁴, A. Sergi^{5,6}, G. Simi^{3,4}, M. Sorbi^{7,8}, M. Sozzi^{11,12}, F. Spadaro Norella^{5,6}, A. Sloocchi²¹, G. Tonani^{7,8}, T. Tork^{7,8}, A. Triossi^{7,4}, A. Turin^{11,12}, F. Vallazza^{13,20}, S. Vico Gil¹⁴, X. Wang⁸, T. Xin⁸, M. Mar⁸, A. Sino^{17,4}, K. Turin^{11,21}, F. Vallazza^{13,20}, S. Vico Gil¹⁴,

¹Nikhef, National institute for subatomic physics, Amsterdam, Nederlands 2CERN - Geneva, Switzerland ³INFN Sezione di Padova, Padua, Italy ⁴Università degli Studi di Padova, Padua, Italy ⁵Università di Genova, Genova, Italy ⁶INFN Sezione di Genova, Genova, Italy 7Università degli Studi di Milano, Milan, Italy 8 INFN Sezione di Milano, Milan, Italy 9Technische Universität Dortmund (TU), Dortmund, Germany 10 University of Chinese Academy of Sciences, Beijing, China ¹¹Università di Pisa, Pisa, Italy 12 INFN Sezione di Pisa, Pisa, Italy 13 University of Bonn, Bonn, Germany 14IFIC - Universitat de Valencia-CSIC, Valencia, Spain ¹⁵Institute of Physics, Ecole Polytechnique Fédérale de Lausanne (EPFL), Lausanne, Switzerland 16 Institute of High Energy Physics, Beijing, China

16 Dec 2024 36 / 40

Physics aims

Slide from presentation of Nicola Neri in the CERN meeting on 28-29 Feb 2024

Physics reach

- First measurements of charm baryon dipole moments in 2 year data taking assuming $10^6 \ {\rm p/s}$ on target. Only a small fraction of the beam halo is deflected towards the target
- Sensitivity on MDM $2 \cdot 10^{-2} \mu_N$ and EDM $3 \cdot 10^{-16} e$ cm with $1.4 \cdot 10^{13}$ PoT
- Two alternatives: i) dedicated experiment at IR3 (baseline); ii) LHCb detector at IP8
 - Pros/cons: i) optimal experiment and detector, PID / More resources needed. New detector + services (long cables, cooling) in IR3; ii) use existing tracking detector and infrastructure. Experimental area. Less resources needed / No PID for p>100 GeV/c, potential interference with LHCb core program

Exploration of τ g-2 and EDM (improvements are required) ٠ MDM μ and EDM δ precession in a bent crystal W targe $\frac{d\mathbf{S}}{d\boldsymbol{\mu}} = \boldsymbol{\mu} \times \mathbf{B}^* + \boldsymbol{\delta} \times \mathbf{E}^*$ Proposed setup for τ precession E^* PRD 103, 072003 (2021) THEP 03 (2019)

16 Dec 2024

37 / 40

PRL 123, 011801 (2019)



Locations along the LHC ring for the dedicated experiment at IR3 and for the LHCb-based detector option.

The proof-of-principle test (TWOCRYST) is scheduled at IR3 during Run 3 and is expected to take data in 2025 to prove feasibility of the proposed ALADDIN experiment.

38 / 40

Summary

ALADDIN is a proposed fixed-target experiment to be installed at LHC IR3 with a unique program of measurements of charm baryon dipole moments and forward physics.

ALADDIN's main objectives are the measurement of the Λ_c^+ and Ξ_c^+ MDMs with a relative precision better than 10% and a search for the EDMs with a sensitivity at the 10^{-16} e·cm level.

The protons from the LHC beam halo impinge a tungsten target paired to a bent crystal where the charm baryons are produced and channelled with an average momentum of \sim 1.8 TeV.

The detector could be installed starting in the LHC LS3, with minimal impact on the LHC machine, to start the commissioning and data taking during Run 4.



Thank you for attention!



A. Korchin (KIPT & KhNU) Dipole moments of short-lived particles

16 Dec 2024 40 / 40