

# LFV and dark sector searches at Belle (II) experiment

*Swagato Banerjee*



*On behalf of the Belle and Belle II collaborations*



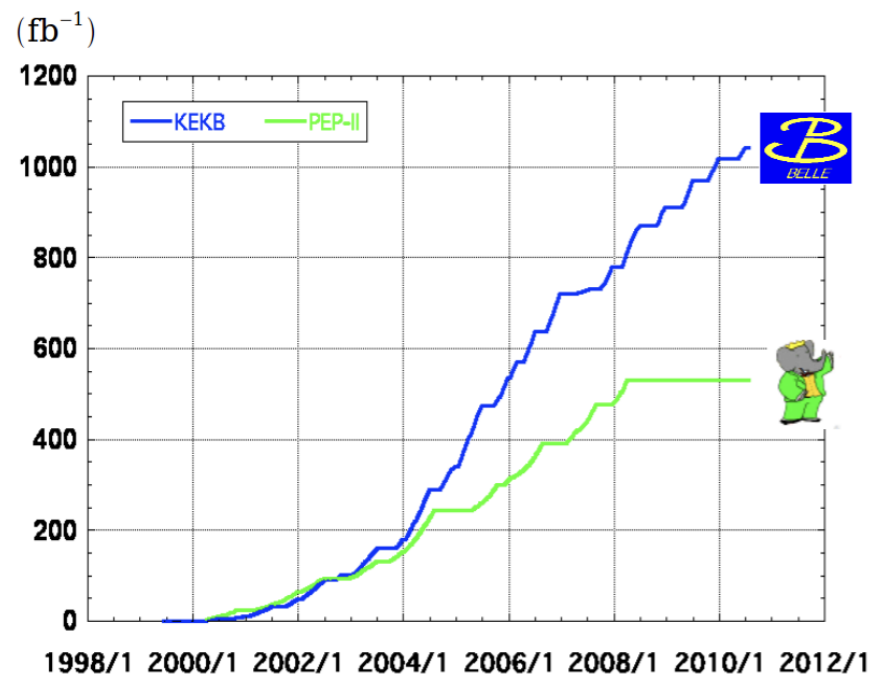
UJ Particle Physics Phenomenology and Experiments Seminar

Krakow

Sep 12, 2022

# B factories are also $\tau$ factories

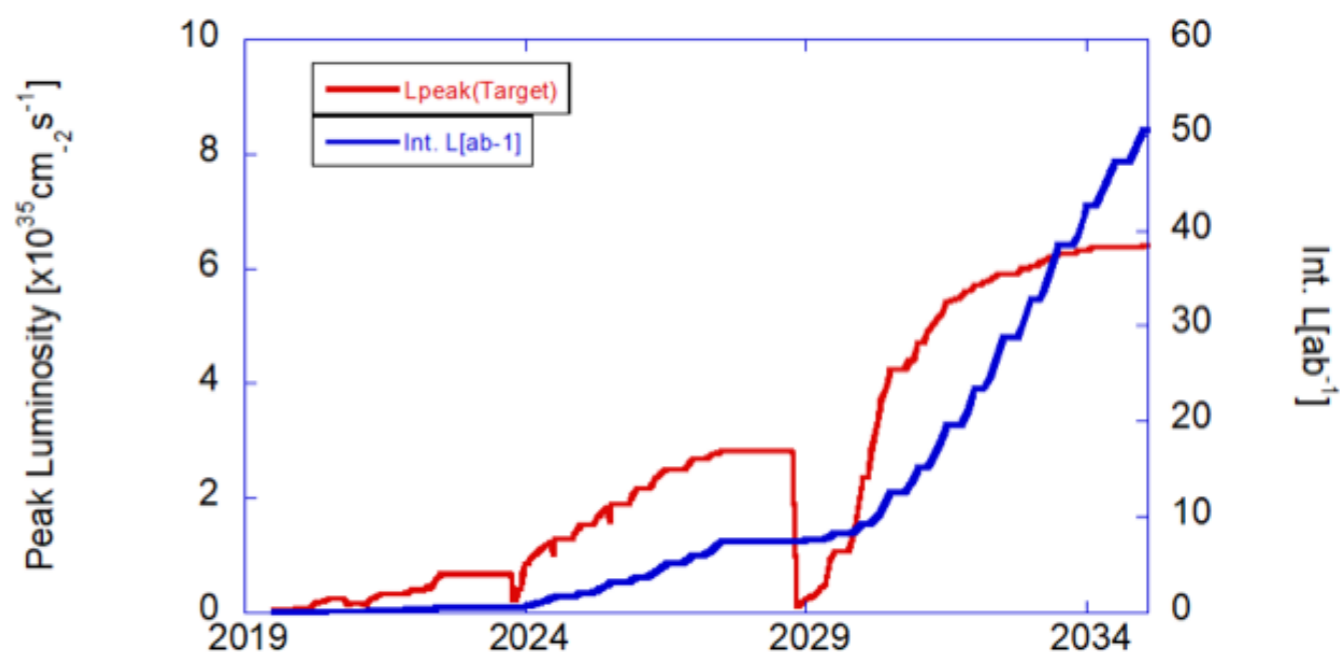
## Integrated luminosity of B factories



**> 1 ab<sup>-1</sup>**  
**On resonance:**  
 $\Upsilon(5S)$ : 121 fb<sup>-1</sup>  
 $\Upsilon(4S)$ : 711 fb<sup>-1</sup>  
 $\Upsilon(3S)$ : 3 fb<sup>-1</sup>  
 $\Upsilon(2S)$ : 25 fb<sup>-1</sup>  
 $\Upsilon(1S)$ : 6 fb<sup>-1</sup>  
**Off reson./scan:**  
 ~ 100 fb<sup>-1</sup>

**~ 550 fb<sup>-1</sup>**  
**On resonance:**  
 $\Upsilon(4S)$ : 433 fb<sup>-1</sup>  
 $\Upsilon(3S)$ : 30 fb<sup>-1</sup>  
 $\Upsilon(2S)$ : 14 fb<sup>-1</sup>  
**Off resonance:**  
 ~ 54 fb<sup>-1</sup>

## Projected luminosity at SuperKEKB/Belle II



$$\sigma(e^+e^- \rightarrow b\bar{b}) = 1.05 \text{ nb}$$

$$\sigma(e^+e^- \rightarrow \tau^+\tau^-) = (0.919 \pm 0.003) \text{ nb}$$

SwB, B. Pietrzyk, J.Roney, Z.Was  
[Phys.Rev.D 77 \(2008\) 054012](#)

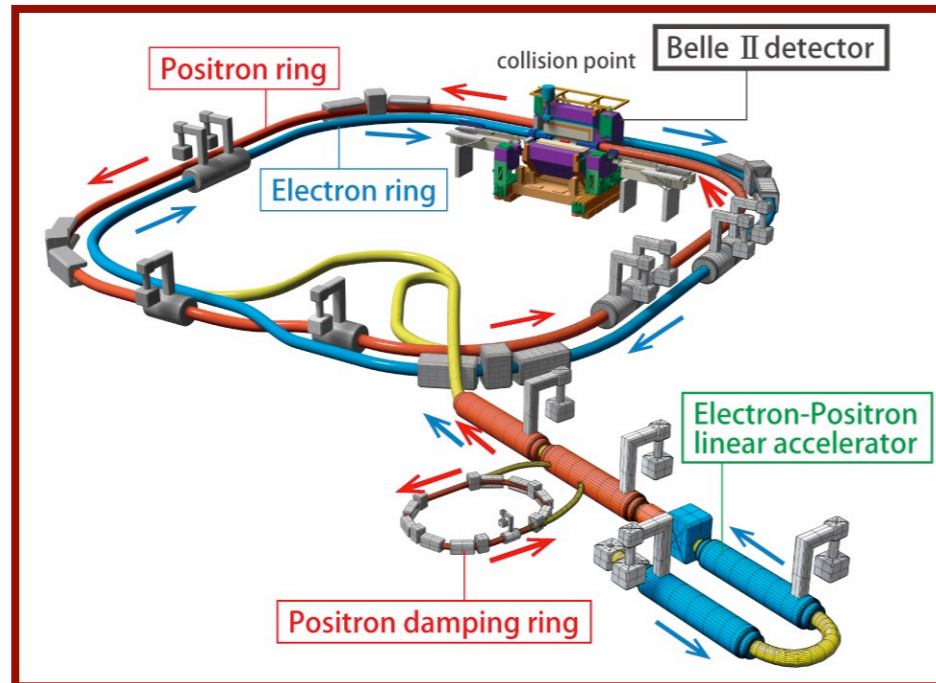
$\tau$ -pairs produced at Belle with  $\simeq 1 \text{ ab}^{-1}$  of data  $\simeq 10^9$

$\tau$ -pairs expected at Belle II with  $\simeq 50 \text{ ab}^{-1}$  of data  $\simeq 5 \times 10^{10}$

World's largest dataset of  $\tau$ -leptons simulated with Monte Carlos:

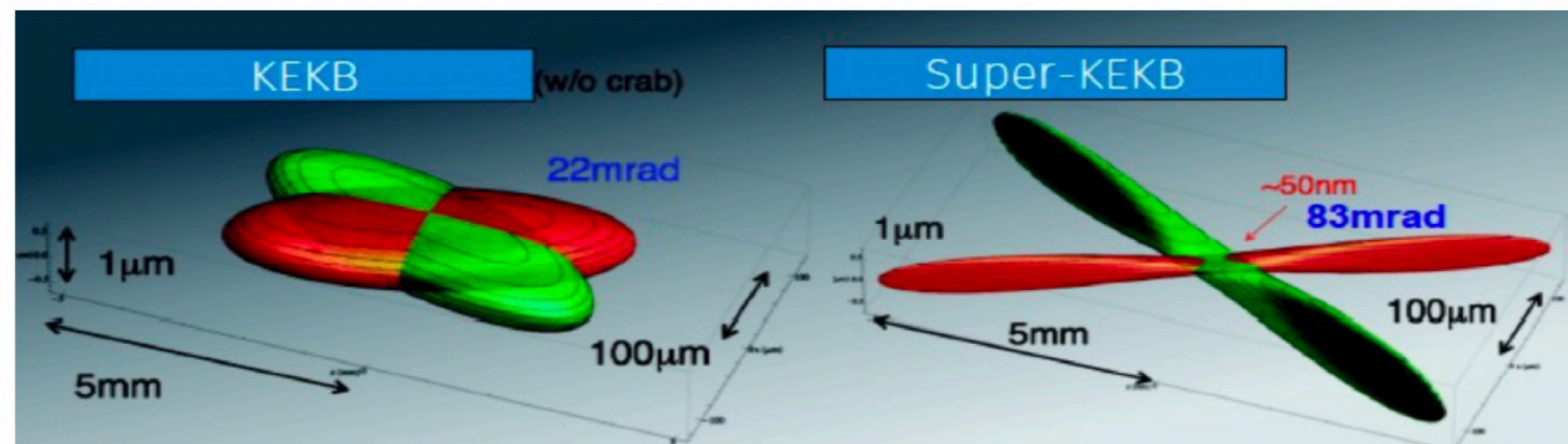
- KK2F [S.Jadach, B.F.L.Ward, Z.Was, [Comput.Phys.Commun. 130 \(2000\) 260](#)]
- TAUOLA [S.Jadach, Z.Was, R.Decker, J.H.Kuhn, [Comput.Phys.Commun. 76 \(1993\) 361](#)]
- PHOTOS [E.Barberio, Z.Was, [Comput.Phys.Commun. 79 \(1994\) 291](#)]

# SuperKEKB/Belle II



Design instantaneous luminosity at SuperKEKB of  $6.5 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$ , e.g. factor of 30 more than KEKB:

- Nano-beam scheme
- Reducing e<sup>-</sup> beam energy gives  $(7/8)^4 = 59\%$  reduction in synchrotron radiation



	Energy (GeV) LER/HER	$\beta_y^*$ (mm) LER/HER	$\epsilon_x$ (nm) LER/HER	$\epsilon_y$ LER/HER	$\varphi$ (mrad)	$I_{\text{beam}}$ (A) LER/HER	Luminosity ( $\text{cm}^{-2}\text{s}^{-1}$ ) $\times 10^{34}$
KEKB Achieved	3.5/8.0	5.9/5.9	18/24	0.13/0.09	11	1.6/1.2	2.11
SuperKEKB	4.0/7.0	0.27/0.3	3.2/2.4	0.09/0.09	41.5	2.8/2.0	65

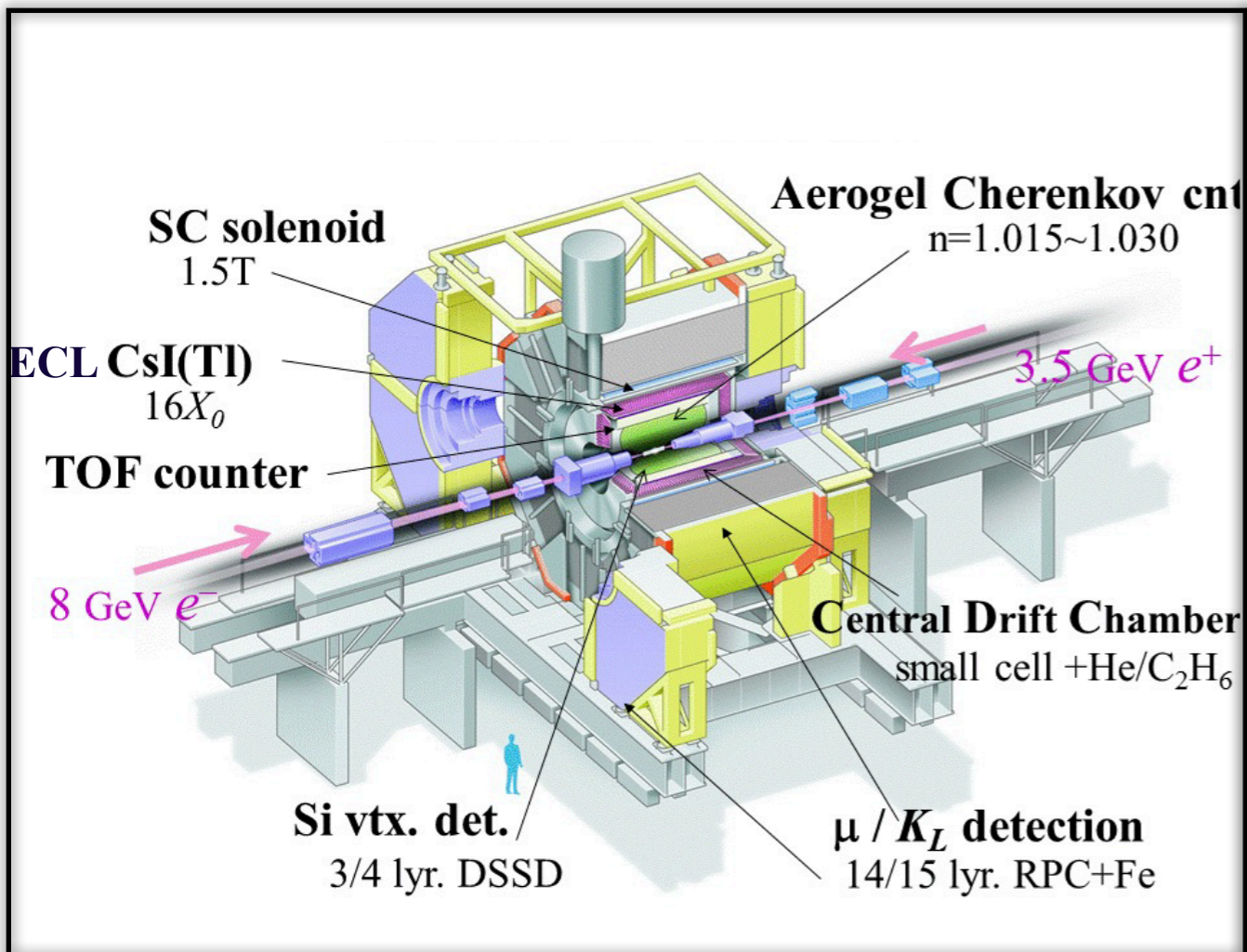
factor 20

factor 1.5

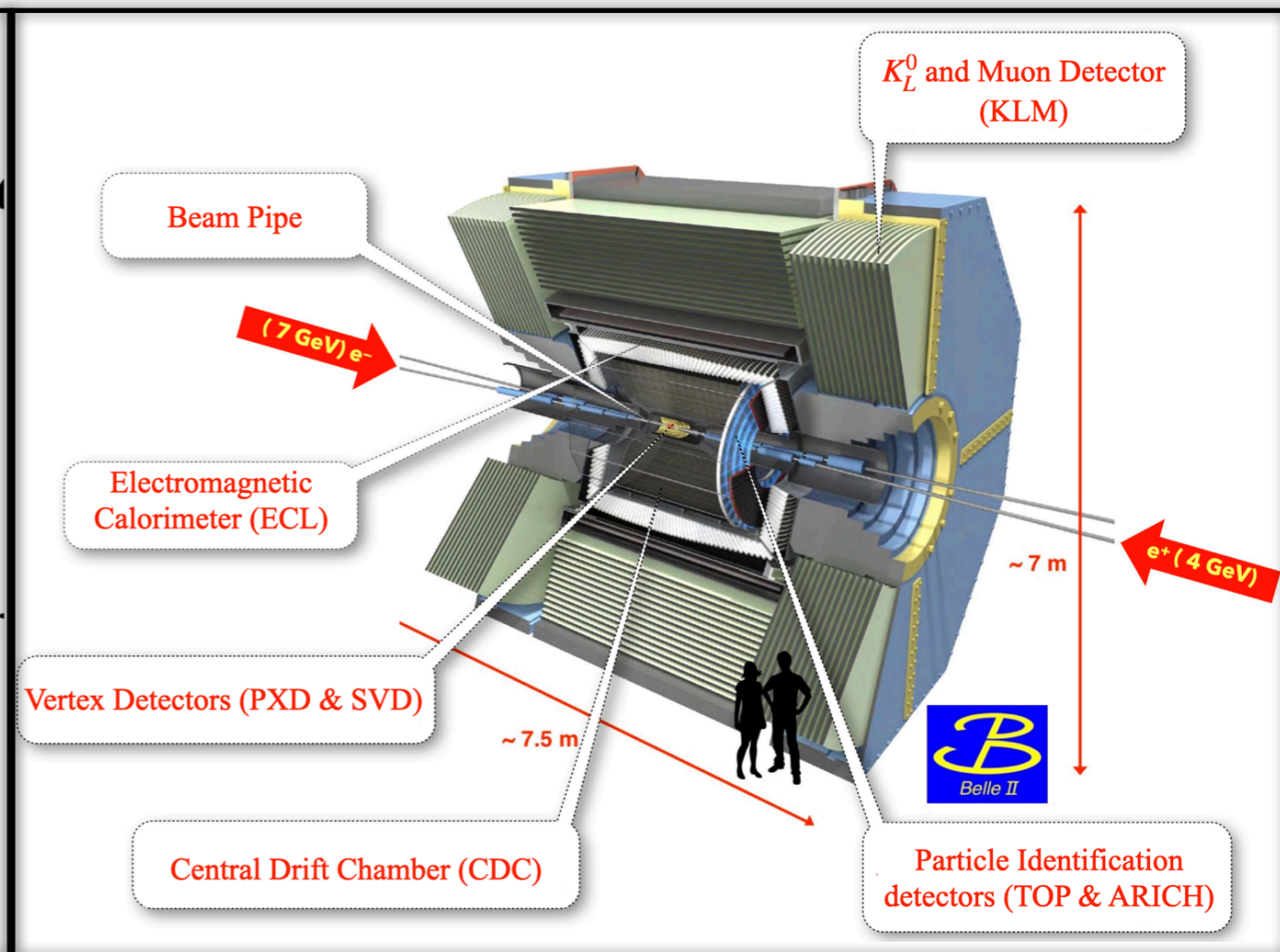
Factor of 30 increase in instantaneous luminosity

# Belle and Belle II detectors

## Belle Detector



## Belle II Detector



# Overview of this talk

- **Search for dark leptophilic scalar at Belle**

- $e^+e^- \rightarrow \tau^+\tau^-\phi_L; \phi_L \rightarrow e^+e^-/\mu^+\mu^-$

- **Search for lepton flavor violation at Belle**

- $\tau^\pm \rightarrow e^\pm\gamma$

- $\tau^\pm \rightarrow \mu^\pm\gamma$

- **Search for lepton flavor violation at Belle II**

- $\tau \rightarrow e/\mu$  invisible

- **Future prospects of LFV searches in  $\tau$  sector**

- Belle II, LHC, STCF, EIC, FCC



[BELLE-CONF-2201](#)

[arXiv:2207.07476 \[hep-ex\]](#)

[JHEP 10 \(2021\) 19](#)

[arXiv:2103.12994 \[hep-ex\]](#)



Shown at ICHEP2022

Snowmass Whitepaper

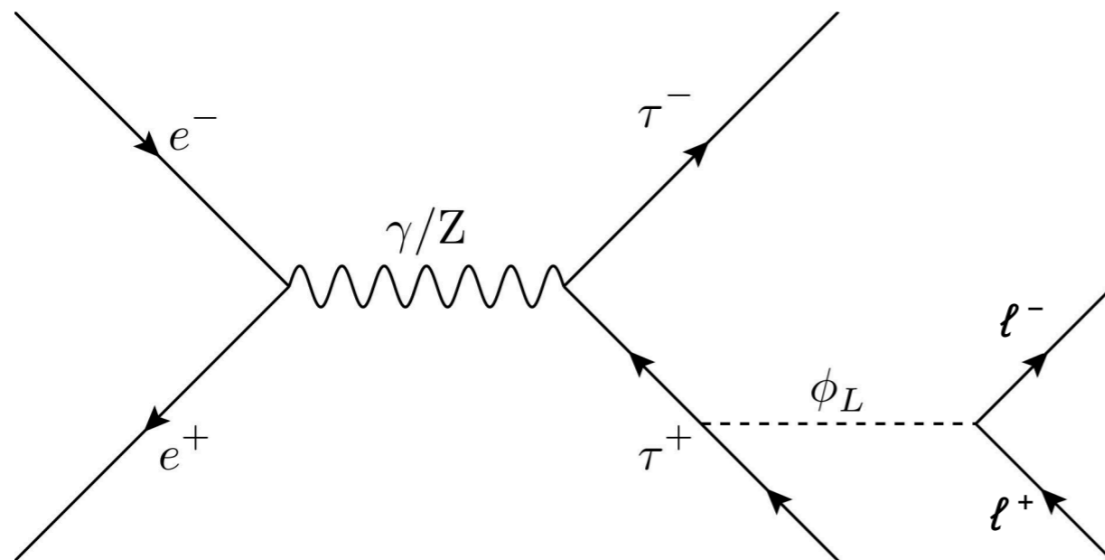
[arXiv:2203.14919 \[hep-ph\]](#)

# Dark leptophilic scalar

Dark sector portal can explain  $(g-2)_\mu$  excess and lepton flavor universality violation:

- Many of the beyond standard model (BSM) theories predict the existence of **additional scalars** other than the Higgs boson.
- The mixing between this dark scalar and the SM Higgs boson gives rise to couplings **proportional to SM fermion masses**.
- If this new scalar couples to both **quarks and leptons**, the existence of such particles is **strongly constrained** by the searches for rare flavor-changing neutral current decays of mesons, e.g.  $B \rightarrow K\phi$  and  $K \rightarrow \pi\phi$ .

However, **these bounds are evaded** if the coupling of the scalar to quarks is suppressed and this scalar interacts **preferentially with leptons**.



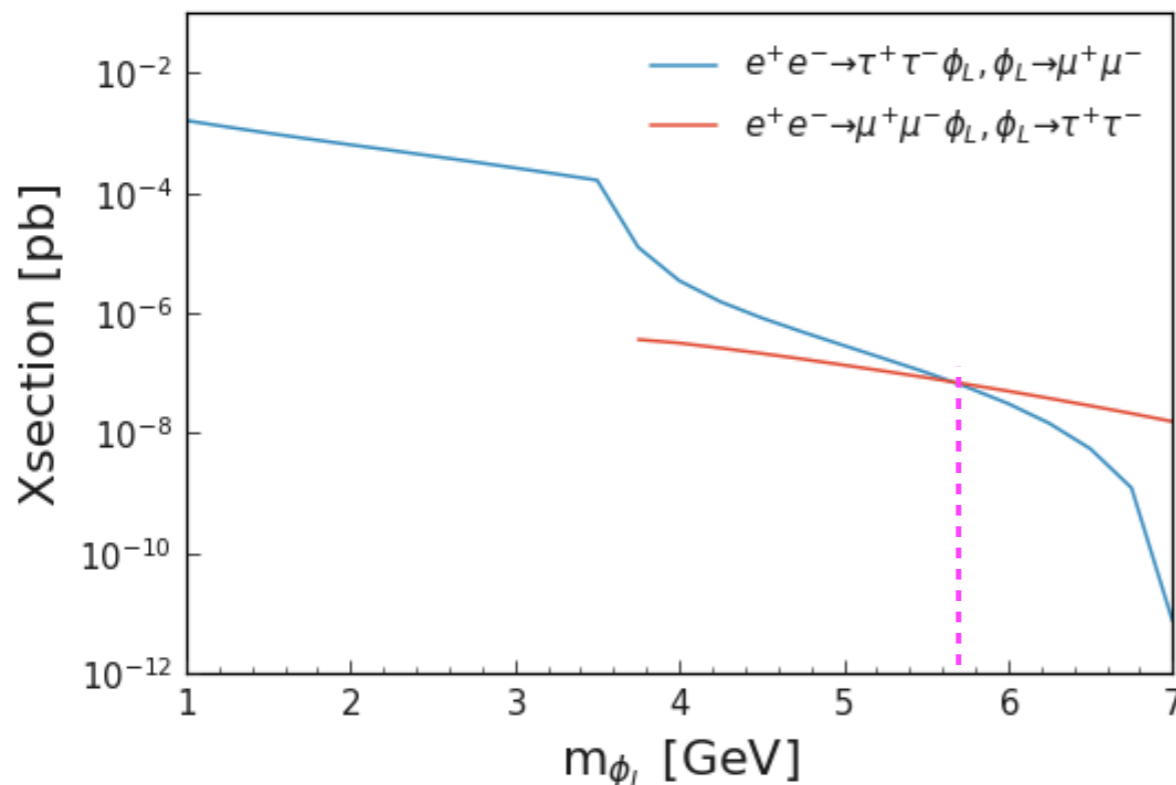
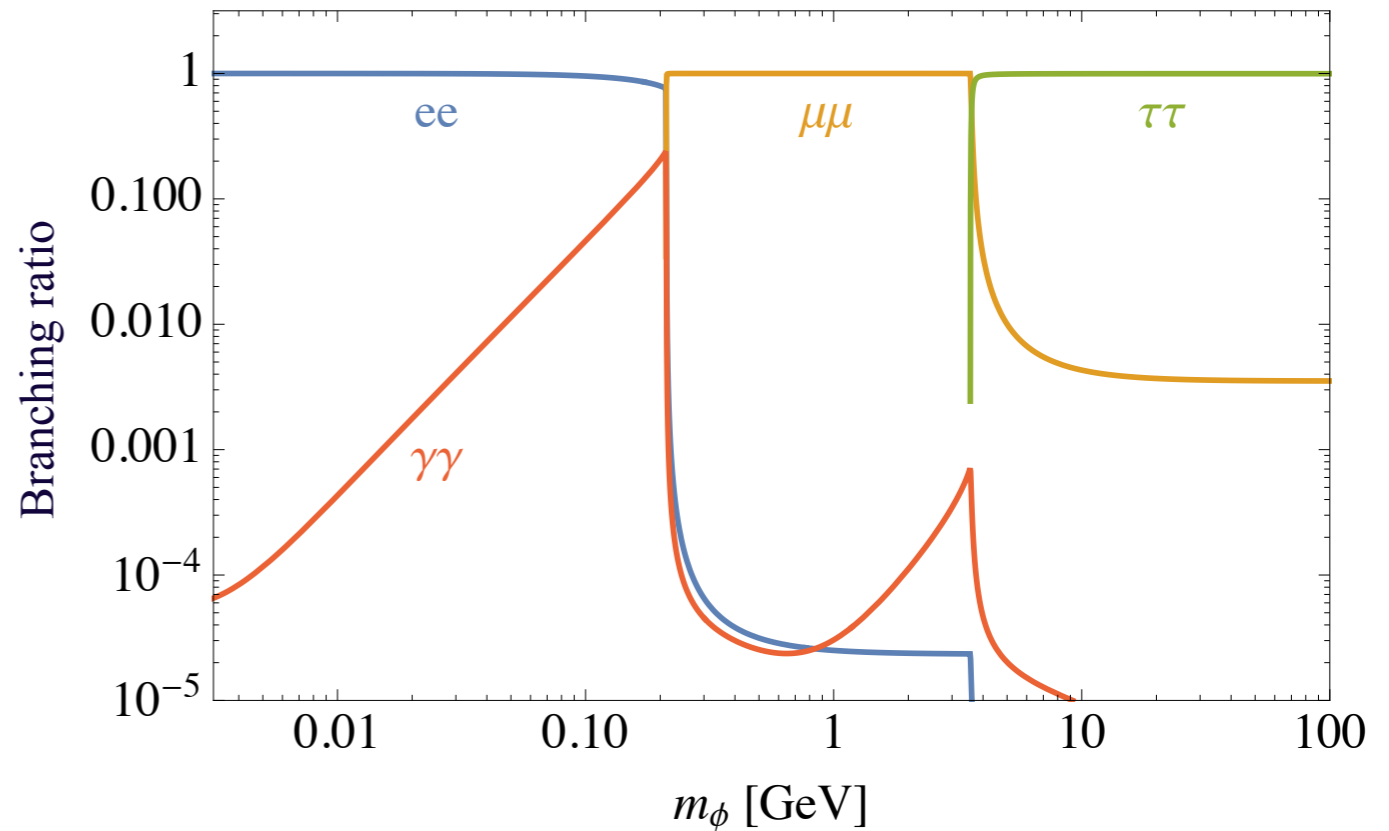
$$\mathcal{L} = -\xi \sum_{\ell=e,\mu,\tau} \frac{m_\ell}{v} \bar{\ell} \phi_L \ell$$

$\xi$  is the lepton flavor independent coupling constant,  $m_\ell$  is mass of the lepton the dark scalar couples with,  $v$  is the vacuum expectation value = 246 GeV

B. Batell, N. Lange, D. McKeen, M. Pospelov, and A. Ritz, "Muon anomalous magnetic moment through the leptonic higgs portal," Phys. Rev. D 95 (2017) 075003.

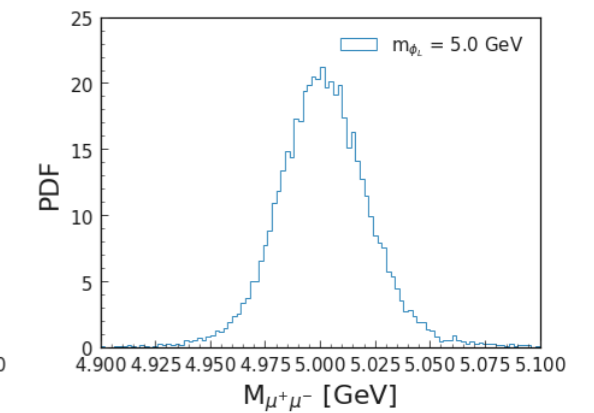
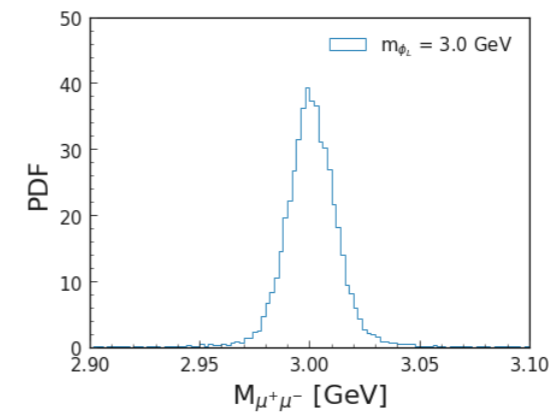
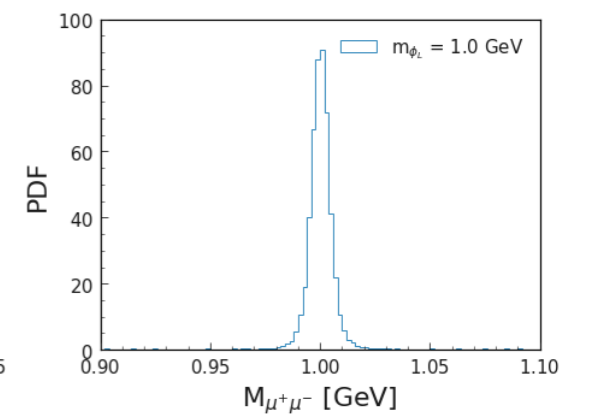
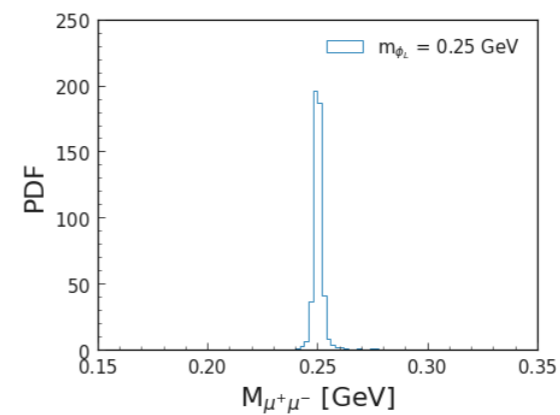
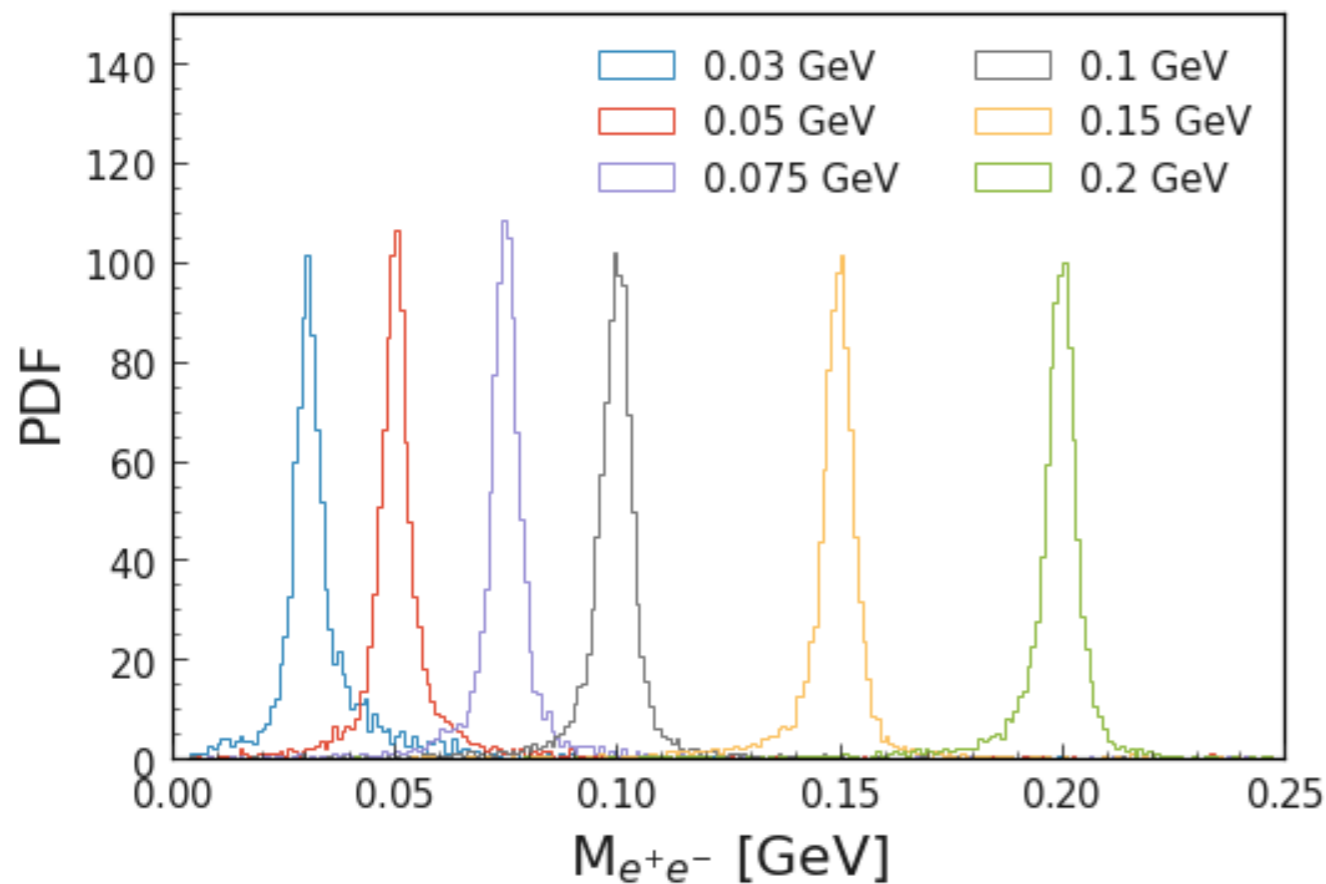
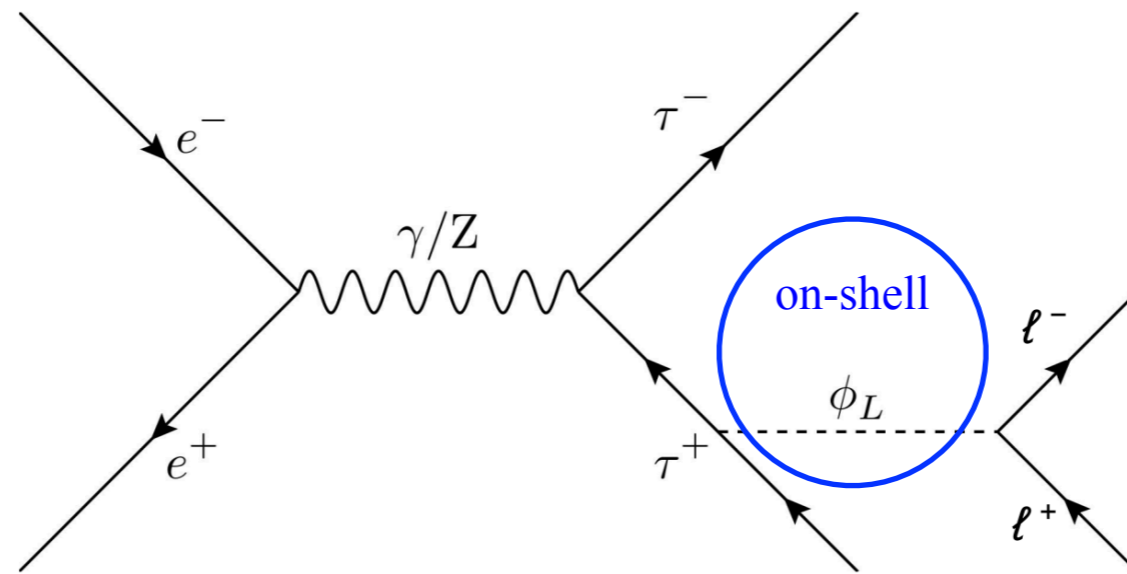
$$e^+e^- \rightarrow \tau^+\tau^-\phi_L; \phi_L \rightarrow e^+e^-/\mu^+\mu^-$$

- $\phi_L$  decays to a lepton pair:  
search for narrow peak in lepton pair invariant mass distribution.
  - $\phi_L \rightarrow e^+e^-$  for  $m_{\phi_L} < 2m_\mu$  and  
 $\phi_L \rightarrow \mu^+\mu^-$  for  $m_{\phi_L} > 2m_\mu$
- High production cross-section times branching ratio in the region  $40 \text{ MeV} < m_{\phi_L} < 6.5 \text{ GeV}$ .



- Comparison between our signal process:
  - $e^+e^- \rightarrow \tau^+\tau^-\phi_L; \phi_L \rightarrow \mu^+\mu^-$
 and complementary process:
  - $e^+e^- \rightarrow \mu^+\mu^-\phi_L; \phi_L \rightarrow \tau^+\tau^-$
 shows signal process has higher rate till 5.7 GeV.
- Our search has sensitivity to place competitive limits on  $\xi$  till  $m_{\phi_L} < 6.5 \text{ GeV}$ .

# Signal distribution of the discriminating variable

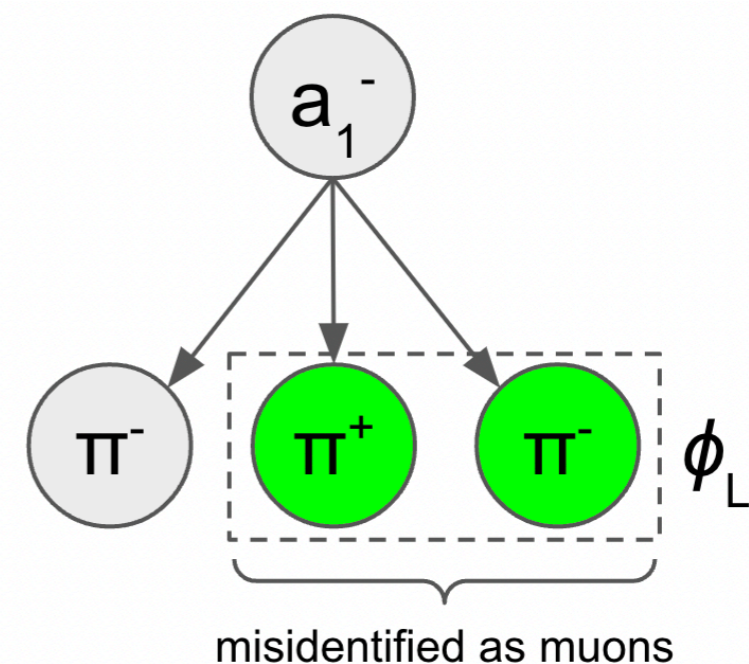
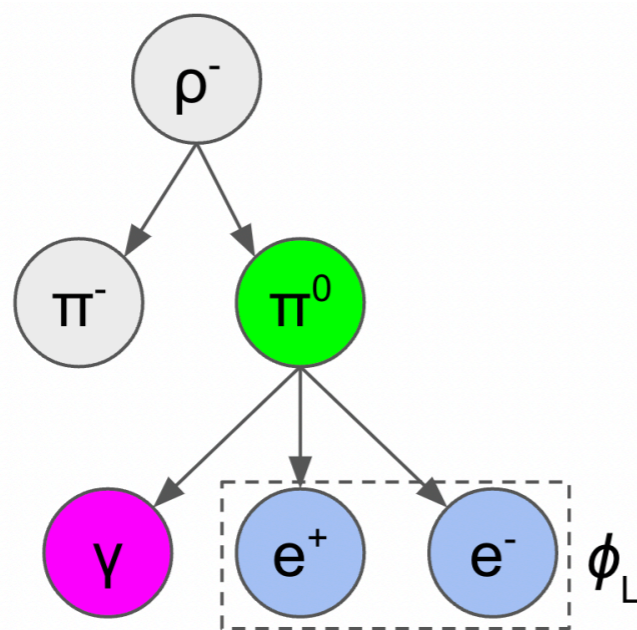


Resolution varies from 5 to 30 MeV, increasing at larger values of  $m_{\phi_L}$



# Search strategy

- Event reconstruction:
  - Require 4 track events with net charge 0.
  - At least two tracks are identified as  $\ell$ , for  $\phi_L \rightarrow \ell^+\ell^-$  channel ( $\ell = e$  or  $\mu$ ).
  - $\ell^+$  and  $\ell^-$  tracks are required to come from the same vertex.
- Backgrounds:
  - $\tau^- \rightarrow \rho^- \nu$ , for  $\phi_L \rightarrow e^+e^-$  channel.  $\rho^-$ -decay produces  $e^+$  and  $e^-$  as shown.
  - $\tau^- \rightarrow a_1^- \nu$ , for  $\phi_L \rightarrow \mu^+\mu^-$  channel.  $\pi^-$  from  $a_1^-$  decay is misidentified as  $\mu^-$ .
  - Some  $q\bar{q}$ ,  $\ell^+\ell^-$ ,  $\ell^+\ell^-\ell^+\ell^-$ ,  $\ell^+\ell^-h^+h^-$  backgrounds in both of the channels.
- Backgrounds have been suppressed using Boosted Decision Tree (BDT).
- Signal extraction:
  - Fit to  $\ell^+\ell^-$  invariant mass distribution.
  - Evaluate at each  $\phi_L$  mass point.

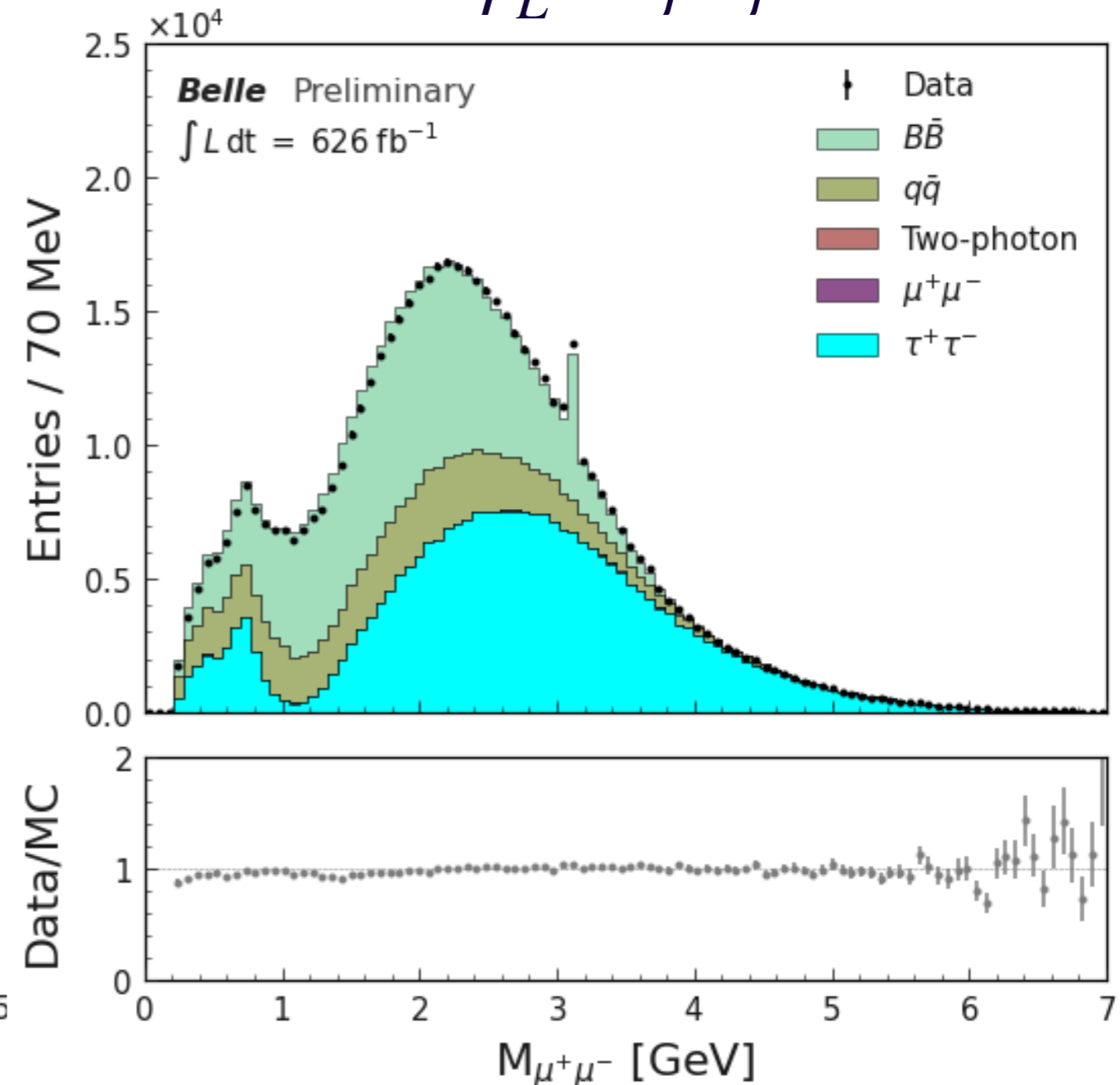
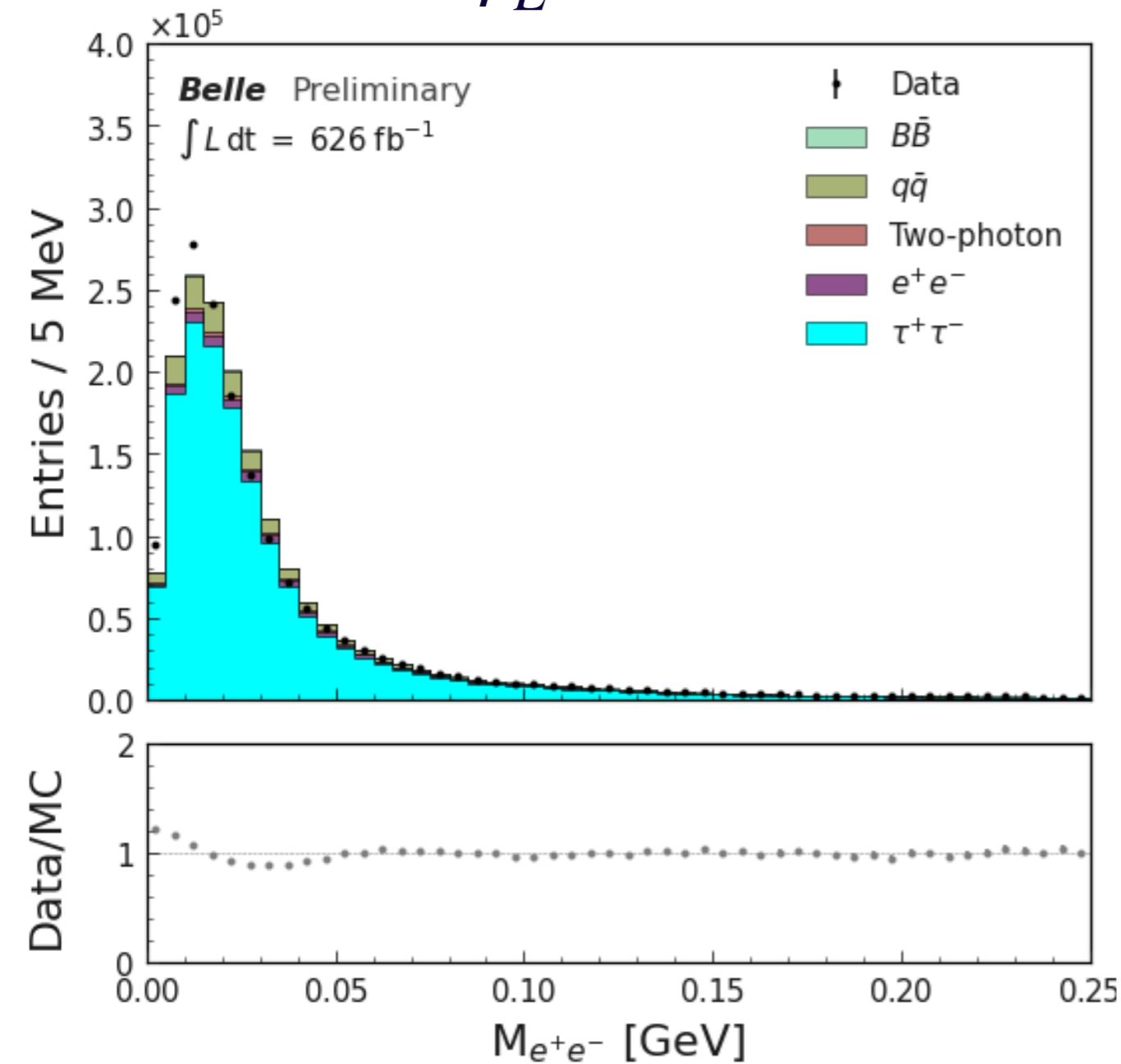


# Search strategy

Good agreement seen in data vs. Monte Carlo comparison in control regions:  $\text{BDT} < 0.5$

$$\phi_L \rightarrow e^+e^-$$

$$\phi_L \rightarrow \mu^+\mu^-$$

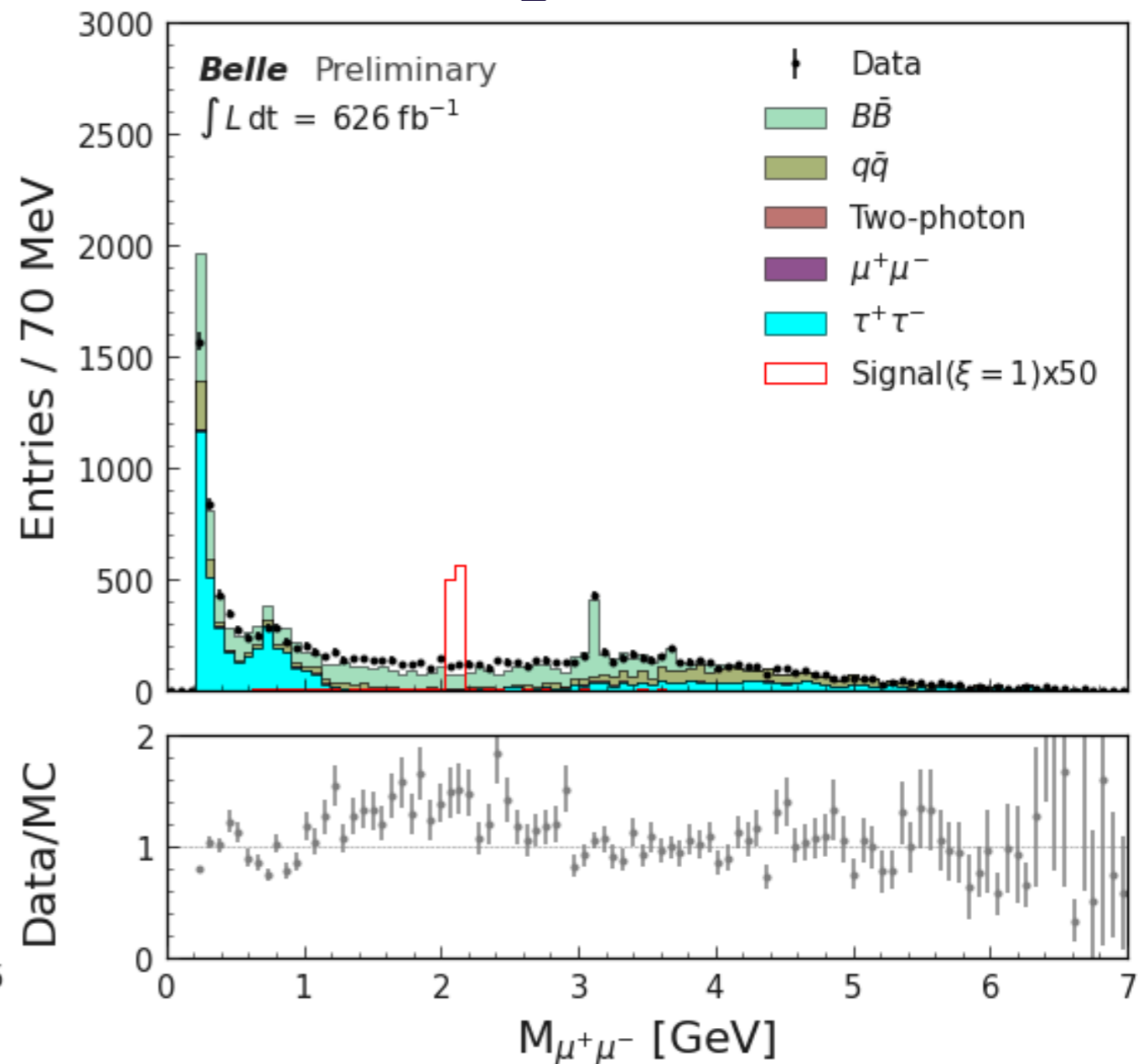
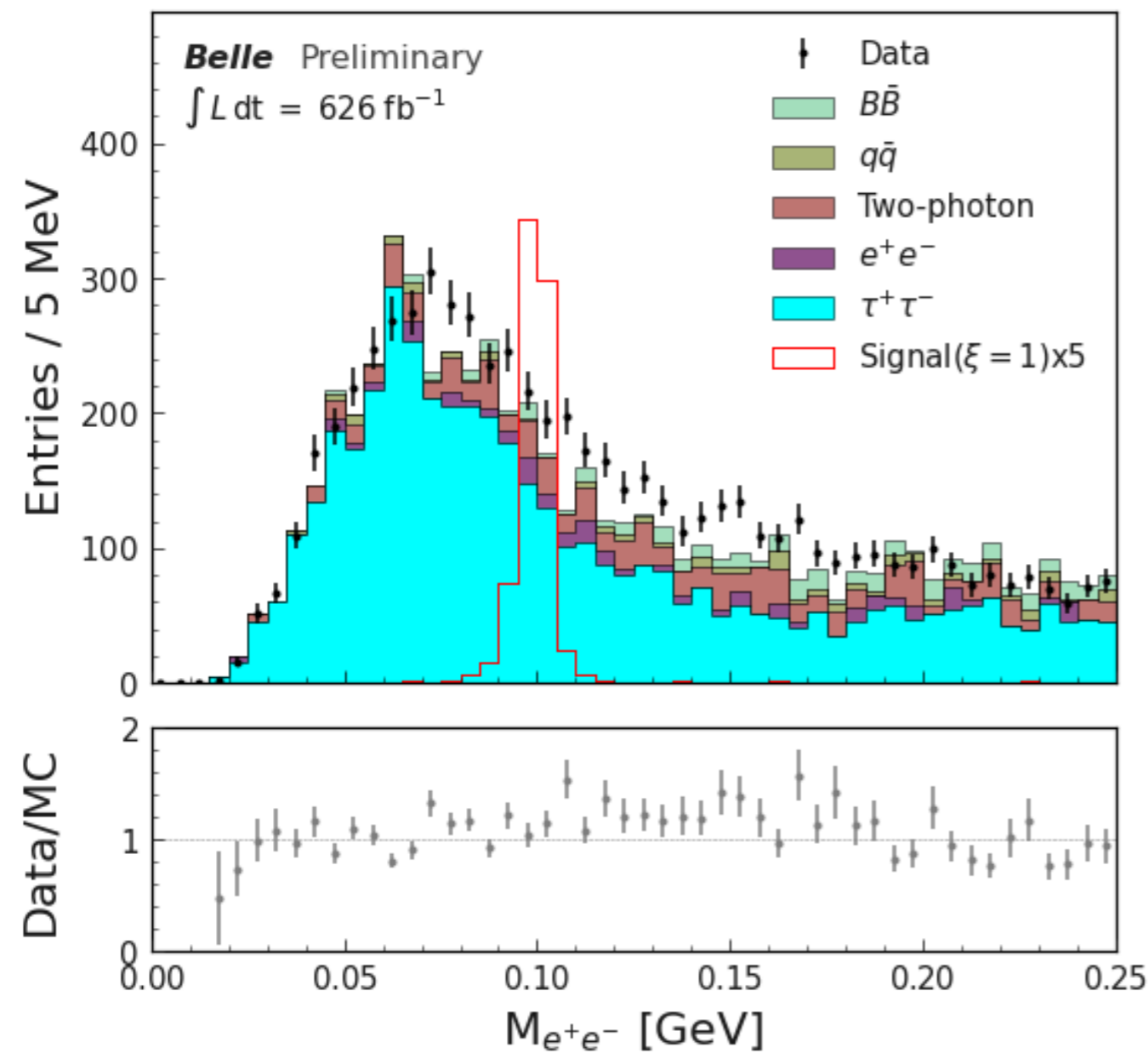


# Search strategy

Data vs. Monte Carlo comparison in signal regions:  
BDT > 0.95 (0.65) for  $\phi_L \rightarrow e^+e^-/\mu^+\mu^-$

$\phi_L \rightarrow e^+e^-$

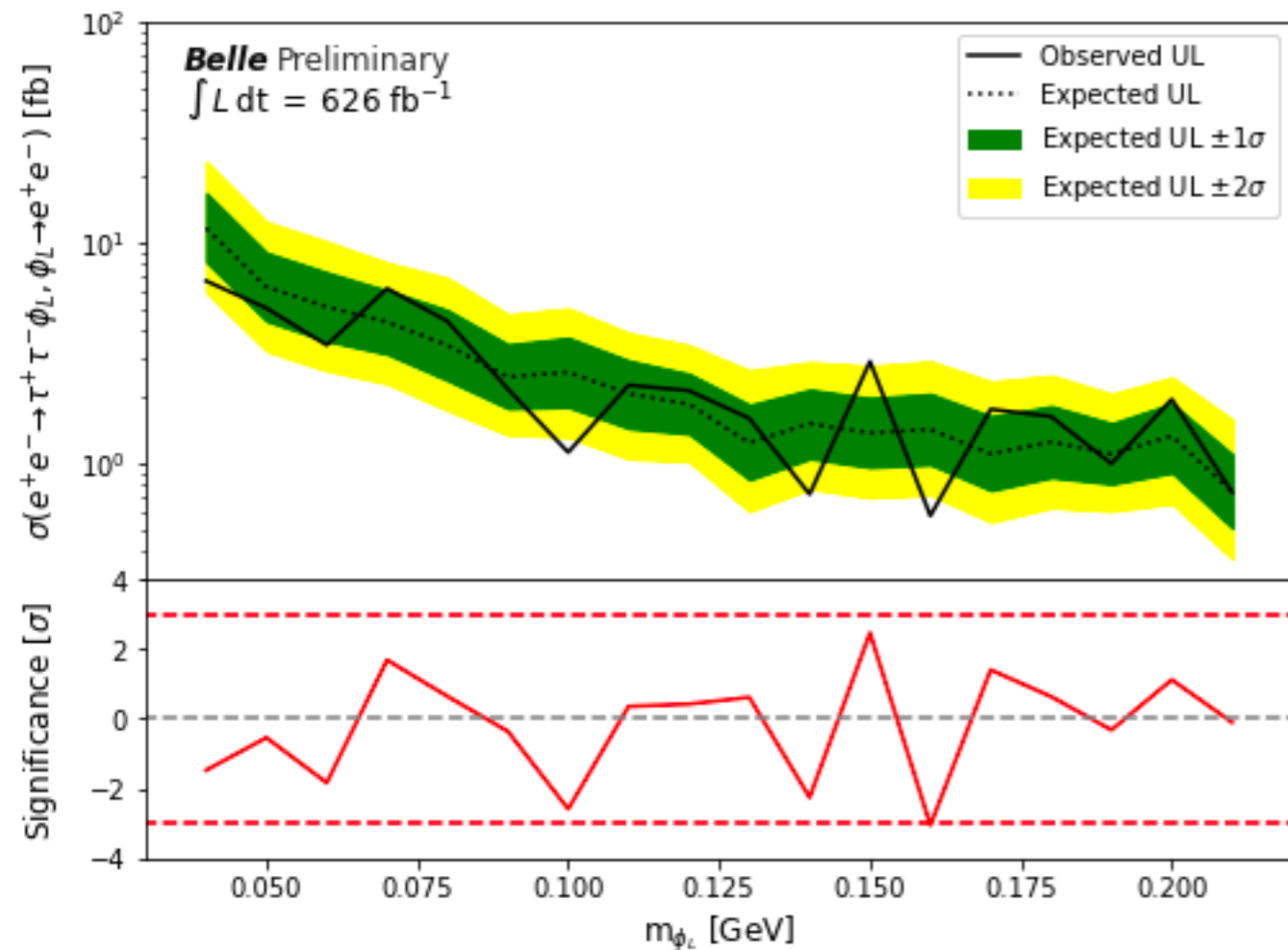
$\phi_L \rightarrow \mu^+\mu^-$



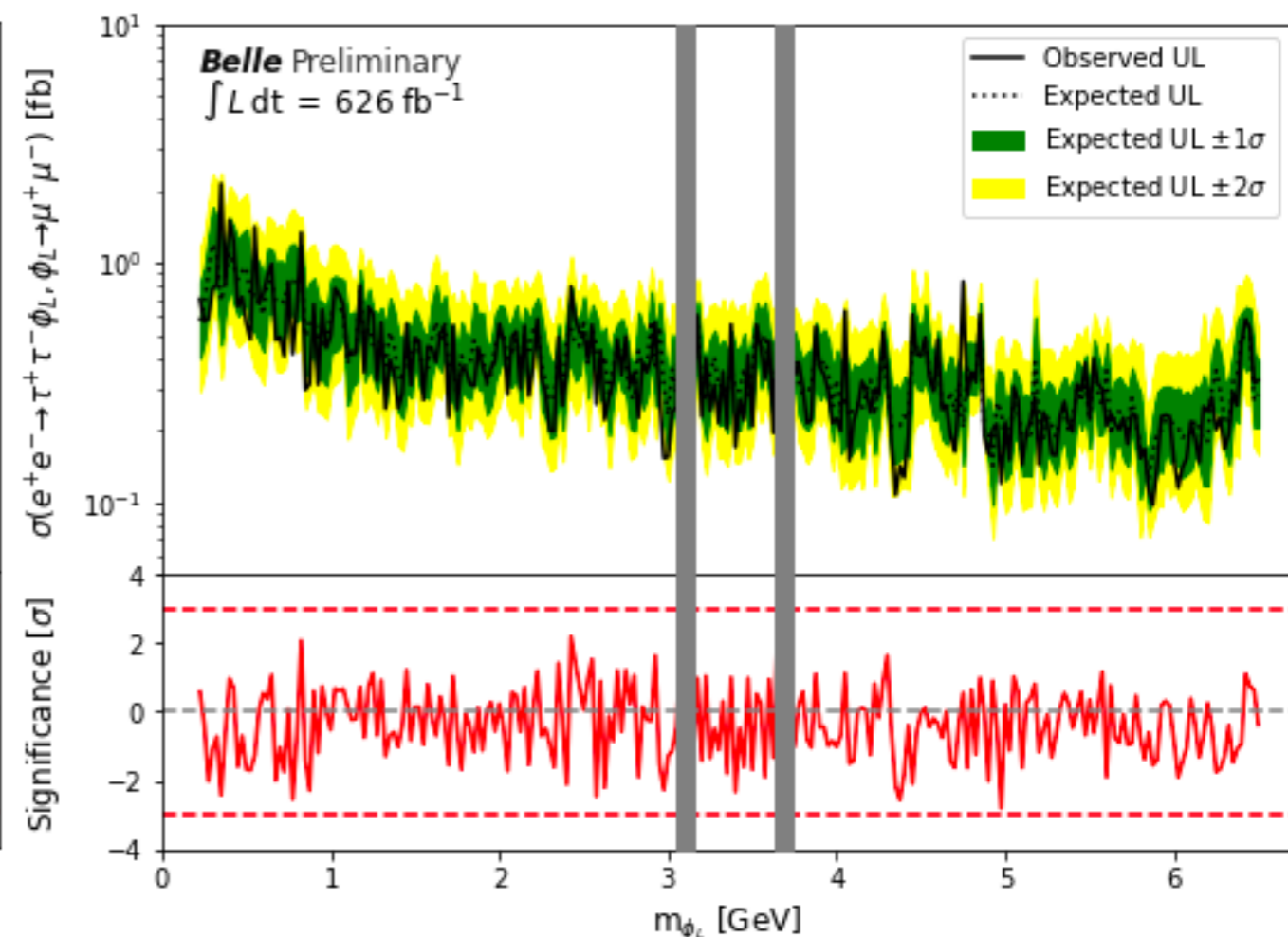
# Results

90% confidence level upper limits on the signal cross-section

$$\phi_L \rightarrow e^+e^-$$



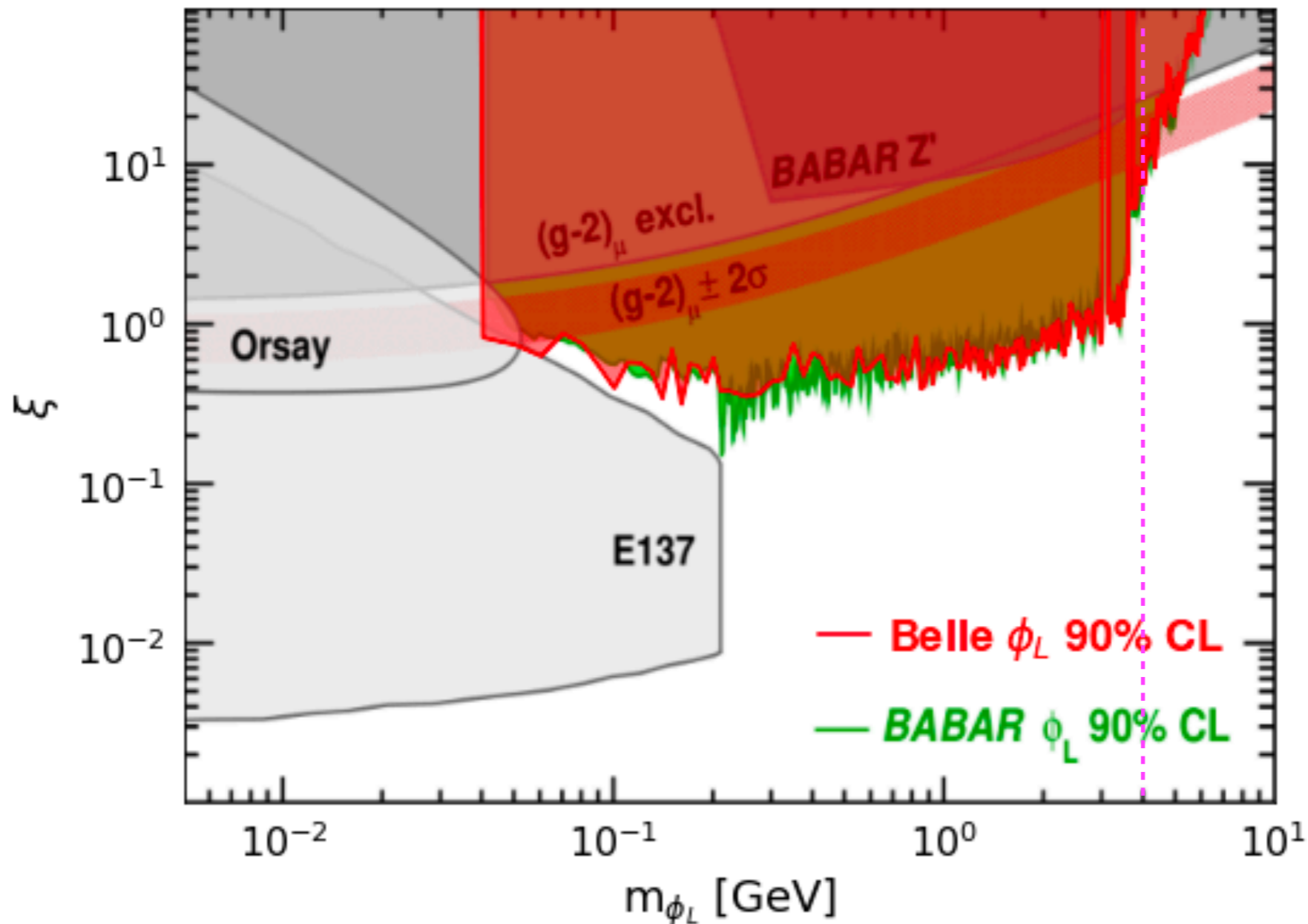
$$\phi_L \rightarrow \mu^+\mu^-$$



Significance  $< 3$  standard deviations for all scan points

# Results

90% confidence level upper limits on the coupling constant



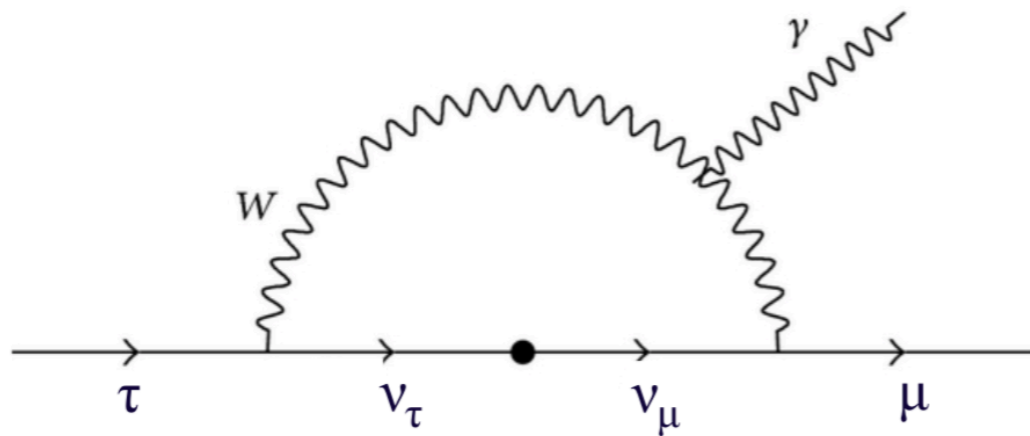
[BELLE-CONF-2201](#)

[arXiv:2207.07476 \[hep-ex\]](#)

No  $\phi_L$  can explain observed excess in  $(g-2)_\mu$  for  $m_{\phi_L} < 4$  GeV

# Charged Lepton flavor violation in $\tau$ decays

LFV is not forbidden by any continuous symmetry  
 $\Rightarrow$  most new physics (NP) models naturally includes LFV



$$\mathcal{B}(\tau^\pm \rightarrow \mu^\pm \gamma) \quad \text{Lee \& Shrock: Phys.Rev.D 16 (1977) 1444}$$

$$= \frac{3\alpha}{128\pi} \left( \frac{\Delta m_{23}^2}{M_W^2} \right)^2 \sin^2 2\theta_{\text{mix}} \mathcal{B}(\tau \rightarrow \mu \bar{\nu}_\mu \nu_\tau)$$

With  $\Delta \sim 10^{-3} \text{ eV}^2$ ,  $M_W \sim \mathcal{O}(10^{11}) \text{ eV}$   
 $\approx \mathcal{O}(10^{-54})$  ( $\theta_{\text{mix}} : \text{max}$ )

many orders below experimental sensitivity!

Any observation of LFV  $\Rightarrow$  unambiguous signature of NP

LFV in  $\tau$  sector is complementary to  $\mu$  sector in NP parameter space:  
 current limit on  $\mathcal{B}(\mu \rightarrow e \gamma) \sim 10^{-13}$  does not forbid  $\mathcal{B}(\tau \rightarrow \ell \gamma) \sim 10^{-8}$

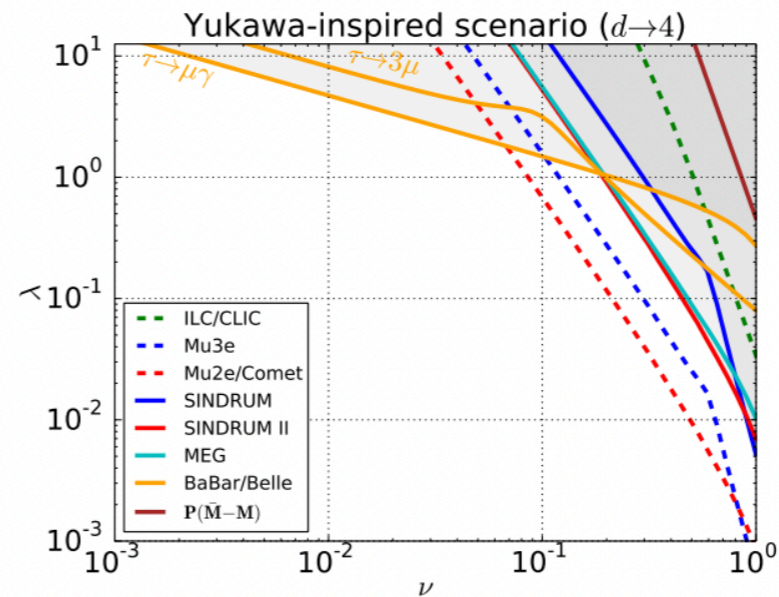
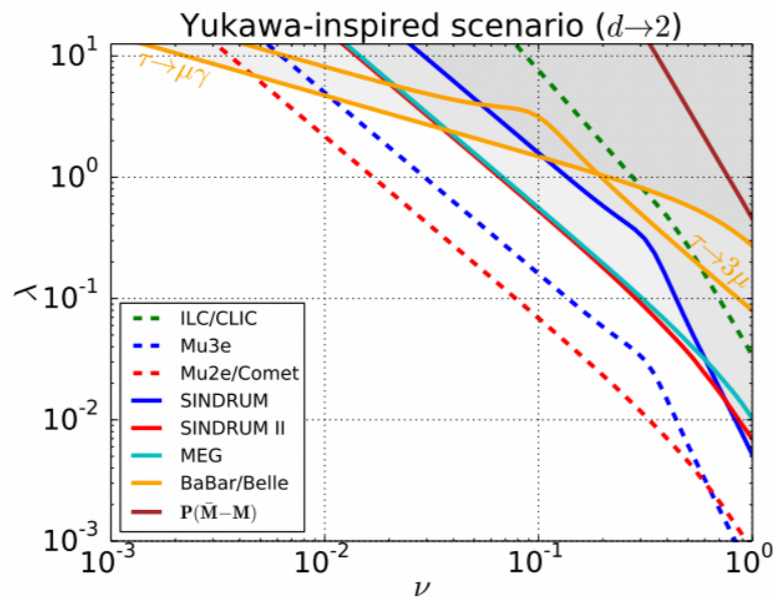
Leptonic MFV:	$\text{BR}(\mu \rightarrow e \gamma) / \text{BR}(\tau \rightarrow \mu \gamma) \sim s_{13}^2 \sim 10^{-2}$
GUT models:	$\text{BR}(\mu \rightarrow e \gamma) / \text{BR}(\tau \rightarrow \mu \gamma) \sim  V_{us} ^6 \sim 10^{-4}$

Vincenzo Cirigliano, Benjamin Grinstein, Gino Isidori, Mark B. Wise: [hep-ph/0507001](https://arxiv.org/abs/hep-ph/0507001) [hep-ph], [hep-ph/0608123](https://arxiv.org/abs/hep-ph/0608123) [hep-ph]  
 R. Barbieri, L. Hall, A. Strumia: [hep-ph/9501334](https://arxiv.org/abs/hep-ph/9501334) [hep-ph]

# New Physics expectations

- Mass dependent couplings enhance tau LFV w.r.t. lighter leptons

Low- and high-energy phenomenology of a doubly charged scalar  
 A. Crivellin et. al.  
 Phys. Rev. D 99, 035004  
 (2019)



$$\lambda_{ab} \sim (y_a^l y_b^l)^{-1}$$

$$\lambda_{ab} = \lambda \begin{pmatrix} \pm 1 & \nu^2 & \nu^3 \\ \nu^2 & \nu^4 & \nu^5 \\ \nu^3 & \nu^5 & \nu^6 \end{pmatrix}$$

- Some models predict LFV up to existing experimental bounds

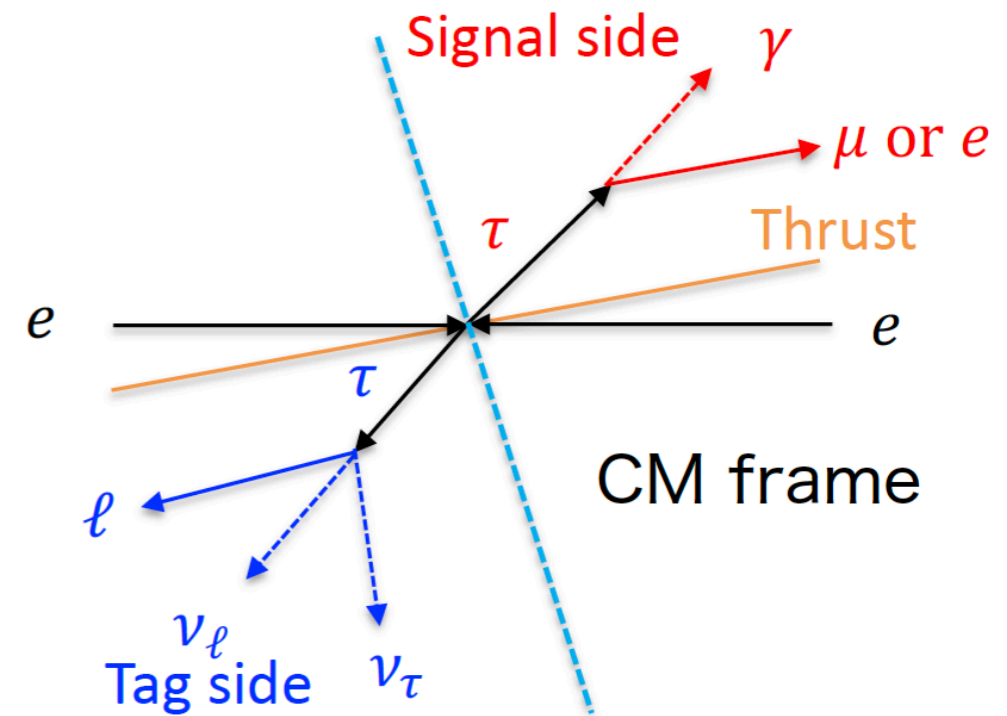
	$\mathcal{B}(\tau \rightarrow \ell \gamma)$
SUSY SO(10) (NPB649(2003)189, PRD68(2003)033012)	$10^{-8}$
SUSY Higgs (PLB549(2002)159, PLB566(2003)217)	$10^{-10}$
Non-Universal Z' (PLB547(2002)252)	$10^{-9}$
SM+Heavy Majorana $\nu_R$ (PRD66(2002)034008)	$10^{-9}$

- Normal (Inverted) hierarchy for slepton  $\Rightarrow \tau \rightarrow \mu \gamma$  ( $\tau \rightarrow e \gamma$ )  
 eg. SUSY models: non-diagonal slepton mass matrix  $\Rightarrow$  LFV

$$\tau^\pm \rightarrow \ell^\pm \gamma$$

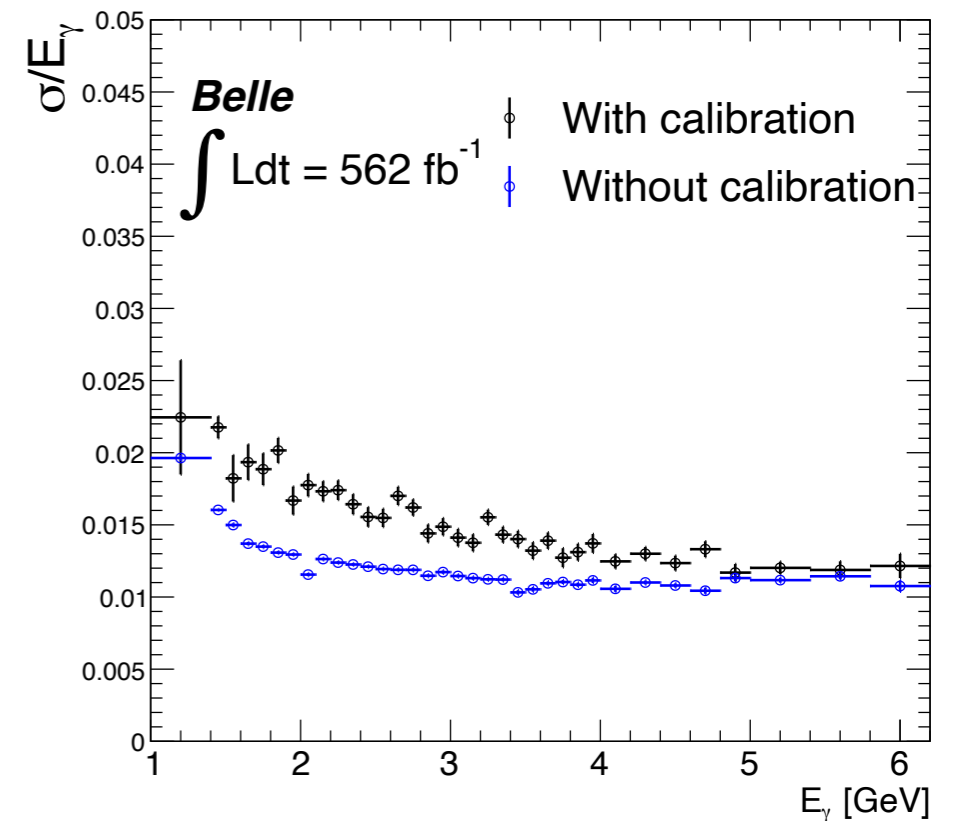
- Event reconstruction:

- ▶ Split event into hemispheres  $\perp$  to thrust axis ( $\hat{n}_T$ ) which maximizes  $\text{Thrust} = \max\left(\frac{\sum |\vec{p}_i| \cdot \hat{n}_T}{\sum |\vec{p}_i|}\right)$
- ▶ Require exactly 2 tracks: 1 in signal-side, 1 in tag-side
- ▶ Signal side:  $E_\gamma \in [0.1, 6]$  GeV identified in ECL



- Major improvement w.r.t previous analysis performed by the Belle Collaboration [Phys. Lett. B 666, 16 (2008)]:

- ▶ Photon energy calibration with  $e^+e^- \rightarrow \mu^+\mu^-\gamma$  events
- ▶ Calibrated energy cross-checked with test beam data  
H. Ikeda et al., Nucl.Instrum.Meth.A 441 (2000) 401





# Signal characteristics

Beam constraint mass:  $M_{bc} = \sqrt{(E_{\text{beam}}^{\text{CM}})^2 - |\vec{p}_{l\gamma}^{\text{CM}}|^2} \simeq m_\tau$

$$\Delta E / \sqrt{s} = (E_{l\gamma}^{\text{CM}} - \sqrt{s}/2) / \sqrt{s} \simeq 0$$

Signal PDF fitted to asymmetric Gaussian function: [JHEP 10 \(2021\) 019](#)

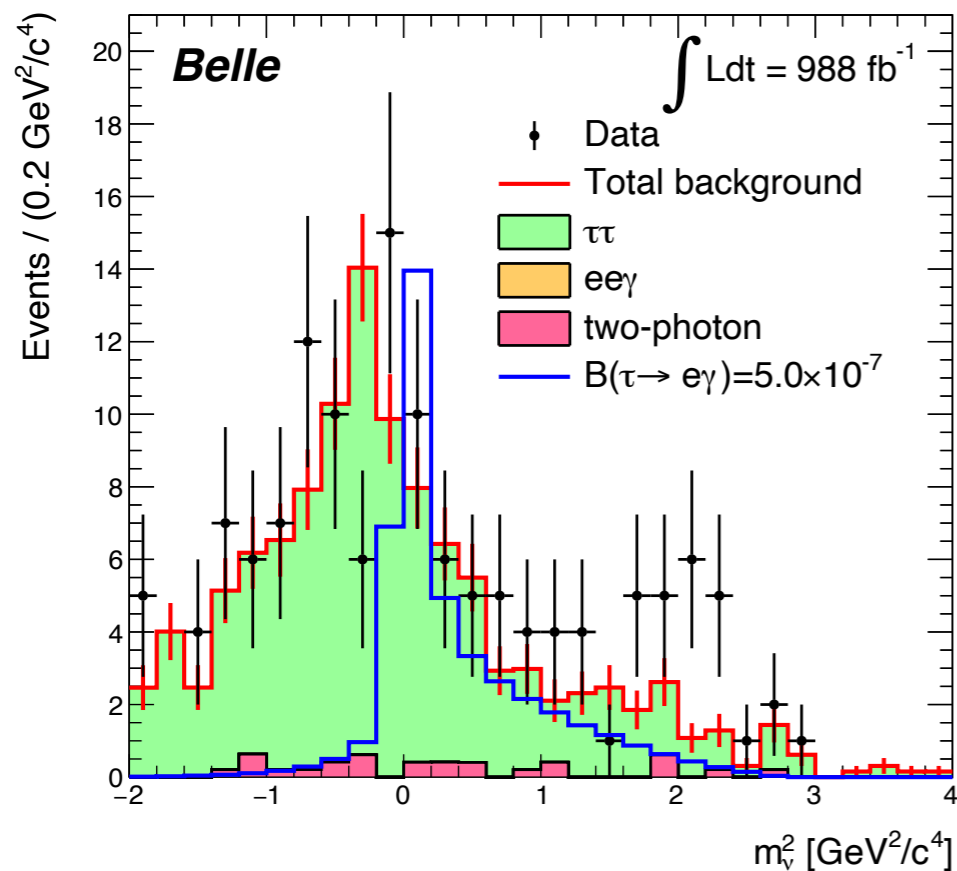
$\tau^\pm \rightarrow e^\pm \gamma$	Mean	Width (lower side)	Width (higher side)
$M_{bc}$	1.79 MeV/c <sup>2</sup>	(10.59 ± 0.19) MeV/c <sup>2</sup>	(11.55 ± 0.27) MeV/c <sup>2</sup>
$\Delta E / \sqrt{s}$	-1.0 x 10 <sup>-3</sup>	(4.4 ± 0.3) x 10 <sup>-3</sup>	(6.1 ± 0.7) x 10 <sup>-3</sup>

$\tau^\pm \rightarrow \mu^\pm \gamma$	Mean	Width (lower side)	Width (higher side)
$M_{bc}$	1.78 MeV/c <sup>2</sup>	(7.46 ± 0.23) MeV/c <sup>2</sup>	(11.08 ± 0.08) MeV/c <sup>2</sup>
$\Delta E / \sqrt{s}$	-0.6 x 10 <sup>-3</sup>	(4.2 ± 0.2) x 10 <sup>-3</sup>	(5.6 ± 0.4) x 10 <sup>-3</sup>

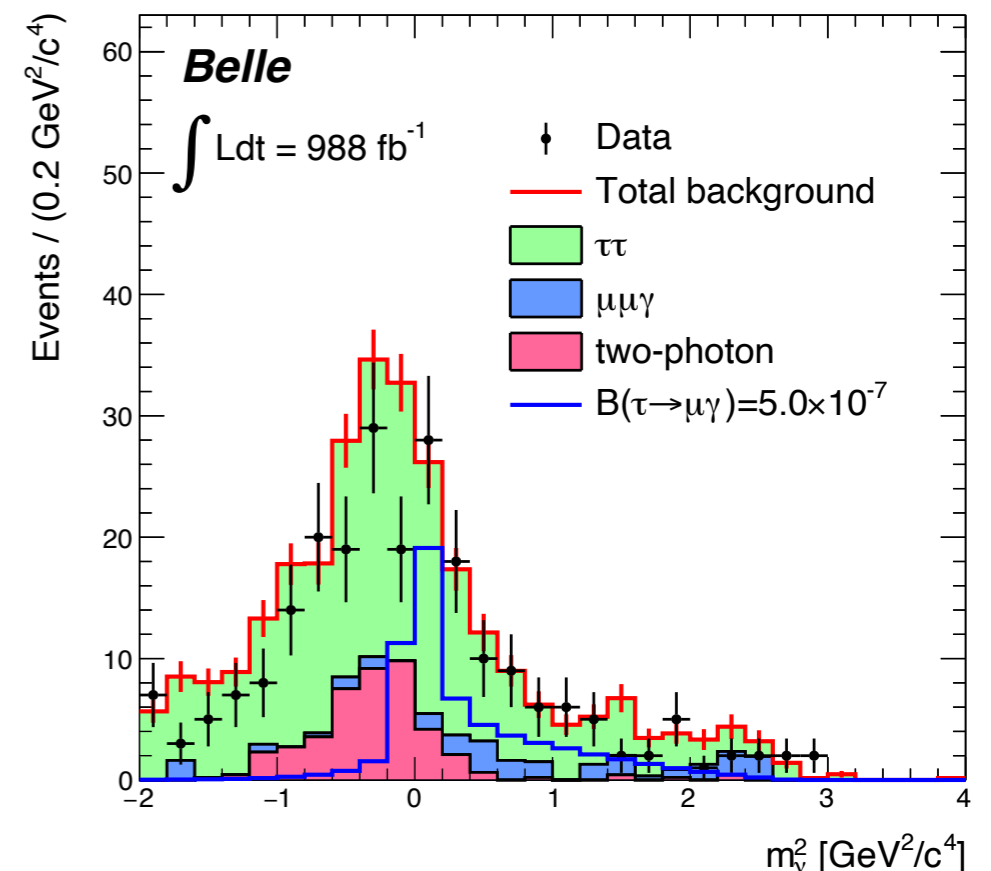
Beam constraint mass has about factor of two better resolution than invariant mass.

# Background rejection

- Dominant backgrounds:
  - ▶  $\tau^\pm \rightarrow \ell^\pm \nu \bar{\nu} + \text{ISR } \gamma$  or beam background
  - ▶  $e^+ e^- \rightarrow \ell^+ \ell^- + \text{ISR } \gamma$  or beam background

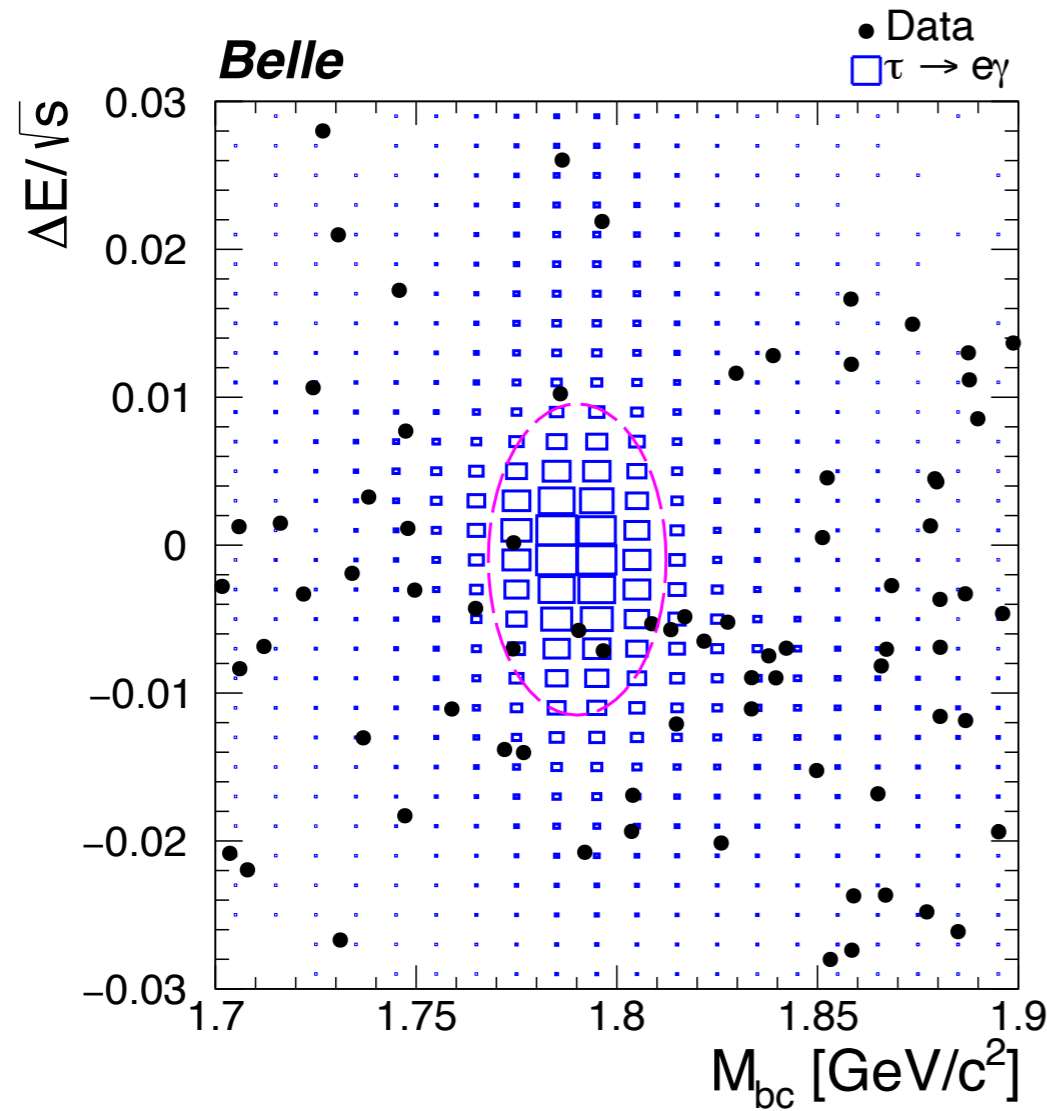


JHEP 10 (2021) 019

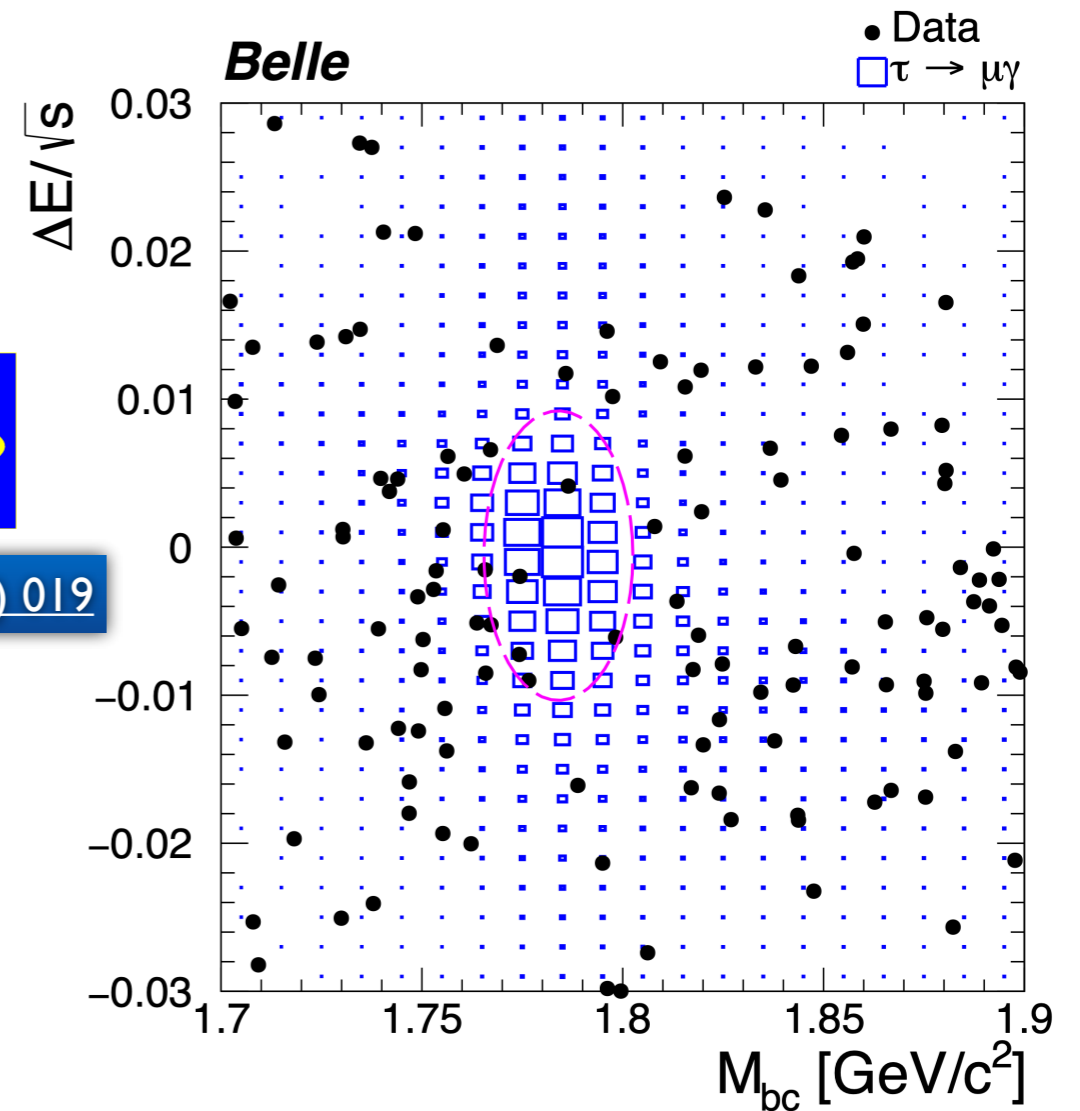


# of $\nu(s)$ in Signal-side	Signal: 0	$\tau^+ \tau^-$ : 1-2	Bhabha, di-muon, $q\bar{q}$ : 0
# of $\nu(s)$ in Tag-side	Signal: 1-2	$\tau^+ \tau^-$ : 1-2	Bhabha, di-muon, $q\bar{q}$ : 0

# Results



JHEP 10 (2021) 019



$B \times 10^{-8}$ at 90% CL	BaBar		Belle		Belle	
	$N_{\tau\tau} = 477 \times 10^6$		$N_{\tau\tau} = 480 \times 10^6$		$N_{\tau\tau} = 912 \times 10^6$	
	Exp	Obs	Exp	Obs	Exp	Obs
$B(\tau^\pm \rightarrow \mu^\pm \gamma)$	8.2	4.4	8.0	4.5	4.9	4.2
$B(\tau^\pm \rightarrow e^\pm \gamma)$	9.8	3.3	12	12	6.5	5.6

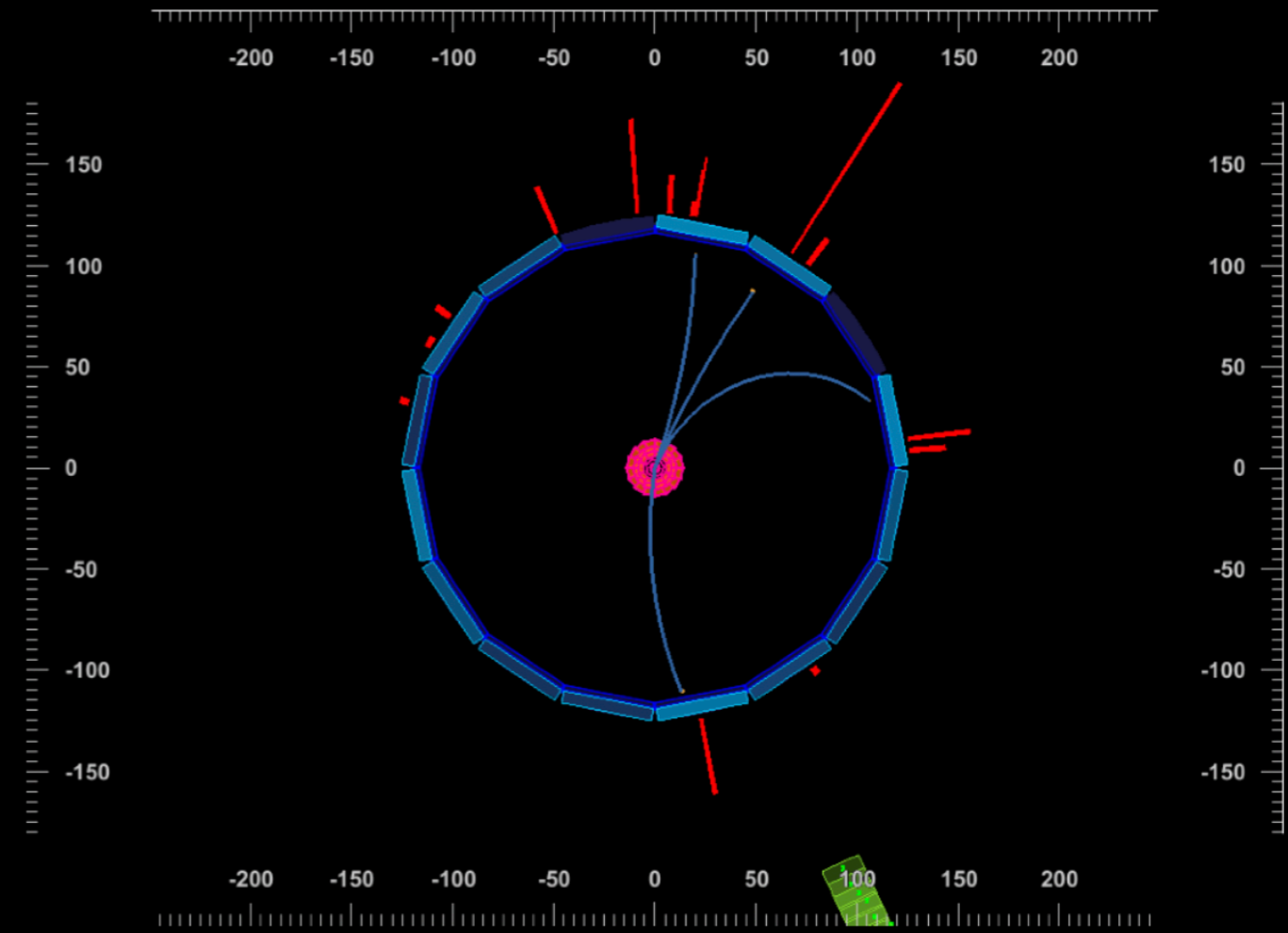
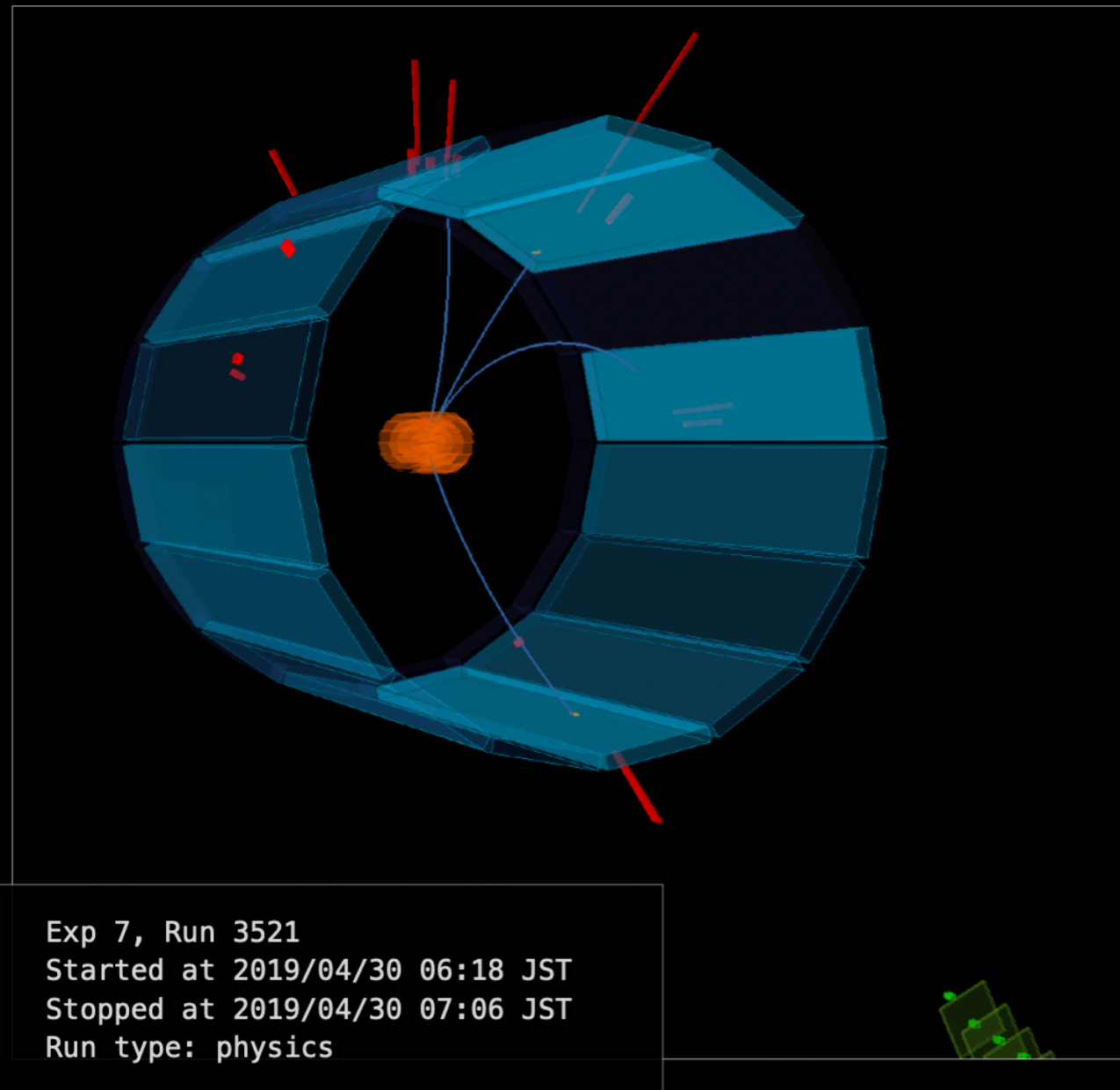
PRL 104 (2010) 021802

PLB 666 (2008) 16

JHEP 10 (2021) 019

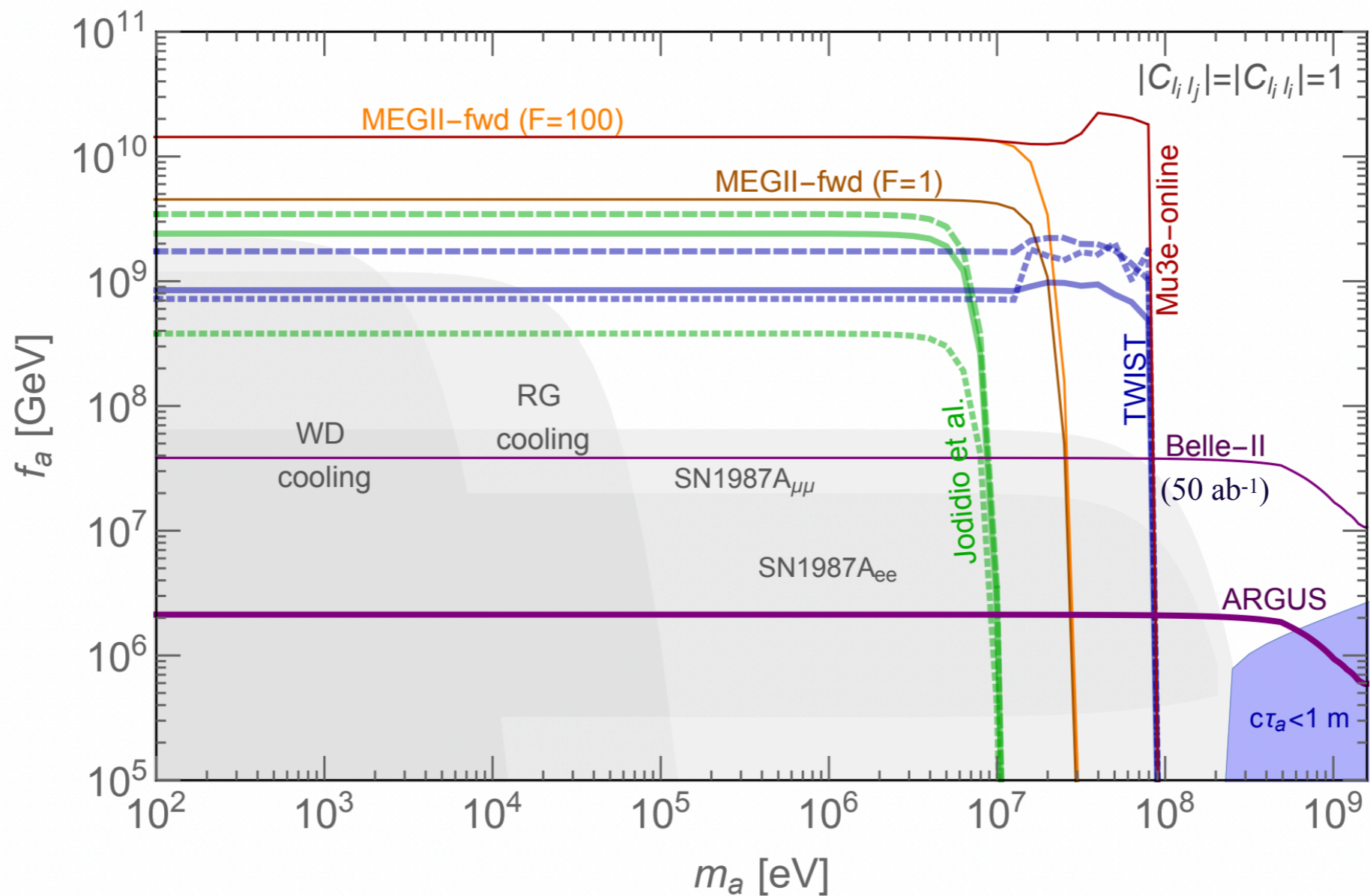
# Tau-pair event at Belle II

## 1-vs-3 topology



# $\tau \rightarrow \ell \alpha$ at Belle II

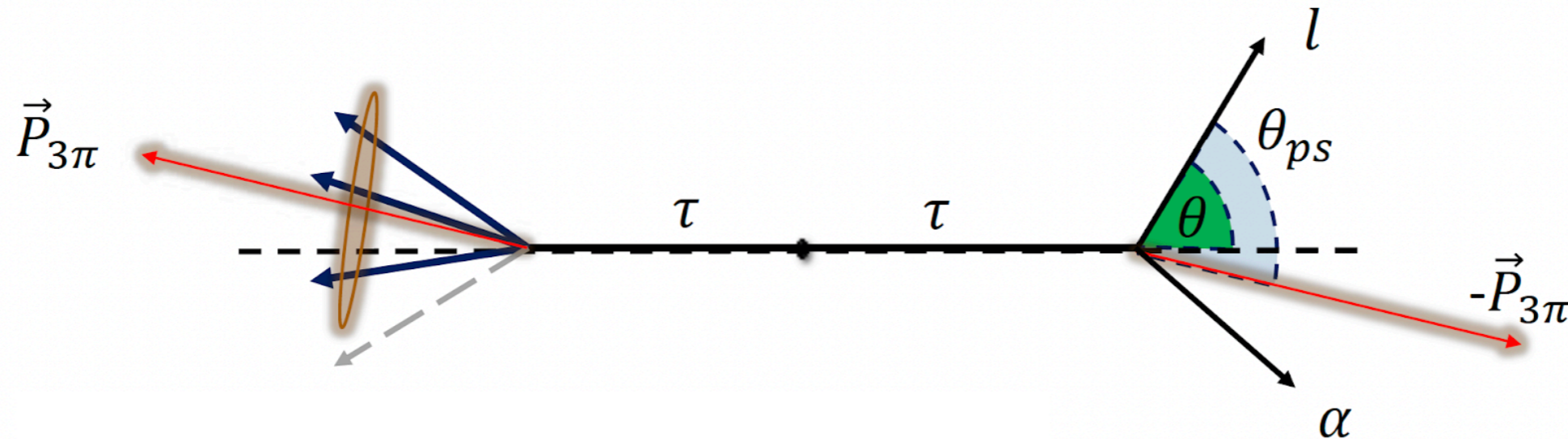
- LFV decay:  $\tau \rightarrow \ell \alpha$  (where  $\ell = e$  or  $\mu$ , and  $\alpha$  is an invisible boson)
- $\alpha$  can enter from new physics models, eg. light axion like particles (ALP),  $Z'$ , etc.



L. Calibbi, D. Redigolo, R. Ziegler, J. Zupan,  
 JHEP 09 (2021) 173 [arXiv:2006.04795](https://arxiv.org/abs/2006.04795) [hep-ph]

# $\tau \rightarrow \ell \alpha$ at Belle II

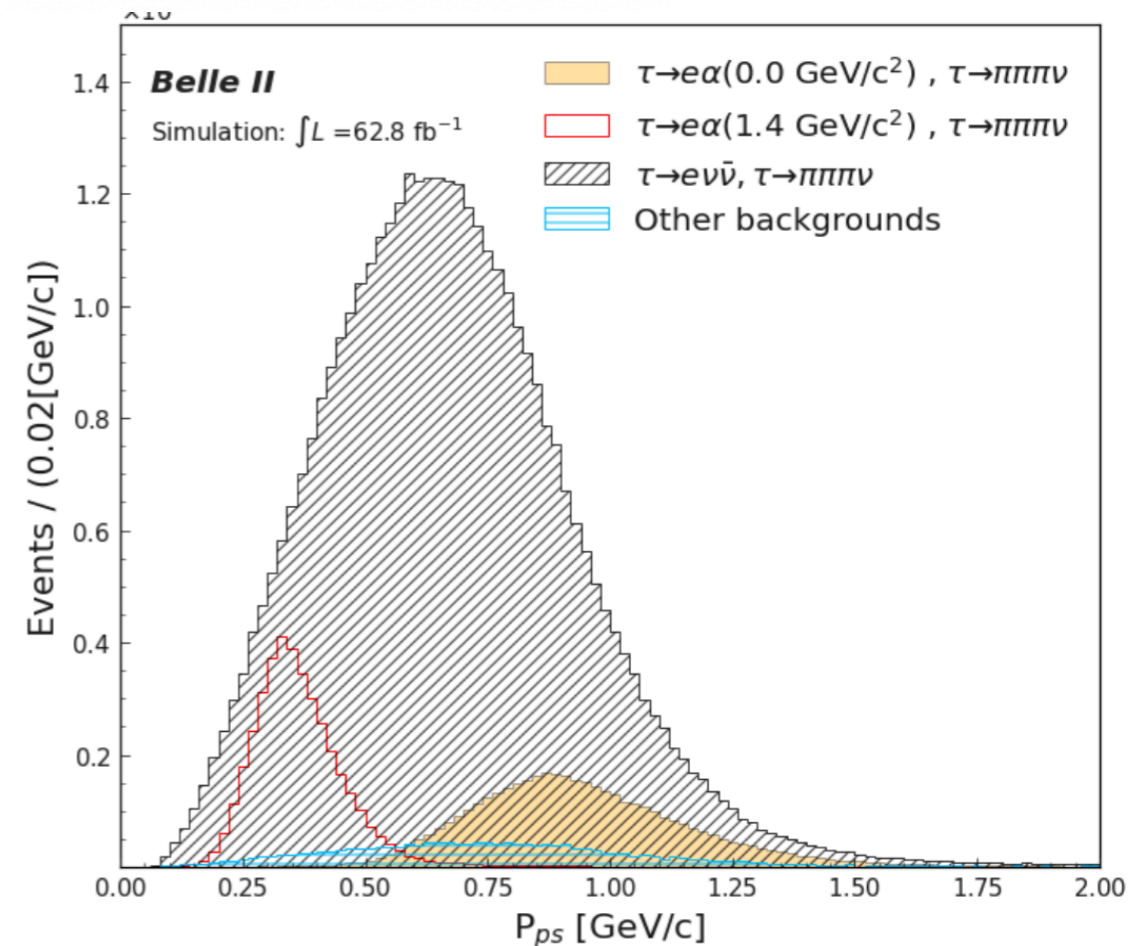
## Signature of the signal process



$\tau$  pseudo-rest frame

2-body  $\tau \rightarrow \ell \alpha$  decay will appear as a bump against the SM 3-body  $\tau \rightarrow \ell \nu \bar{\nu}$  background in the  $p_\ell$  distribution in the  $\tau$  pseudo-rest frame

$$\hat{p}_\tau \approx -\frac{\vec{P}_{tag}}{|\vec{P}_{tag}|}, \quad E_\tau \approx \sqrt{s}/2$$



# $\tau \rightarrow \ell \alpha$ at Belle II

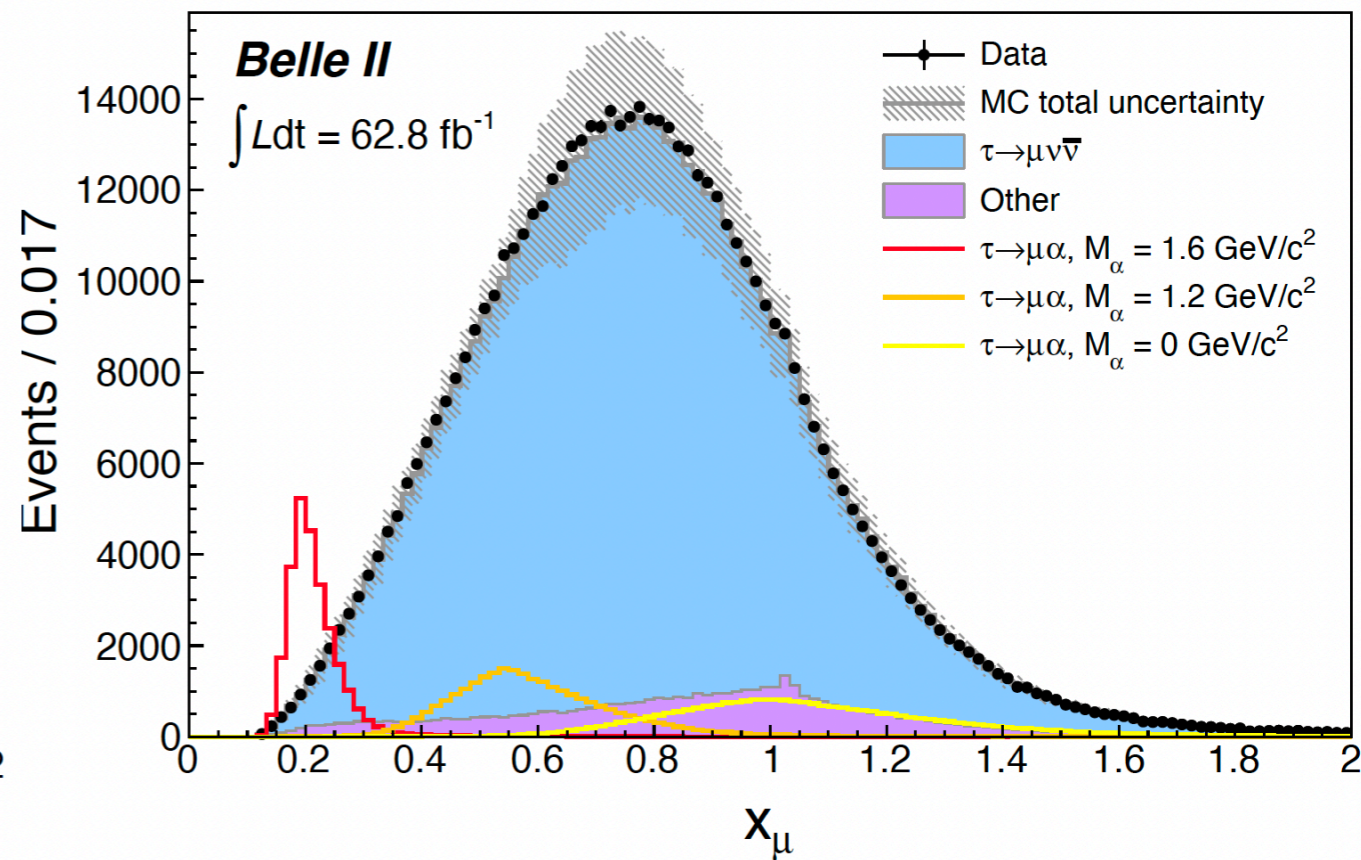
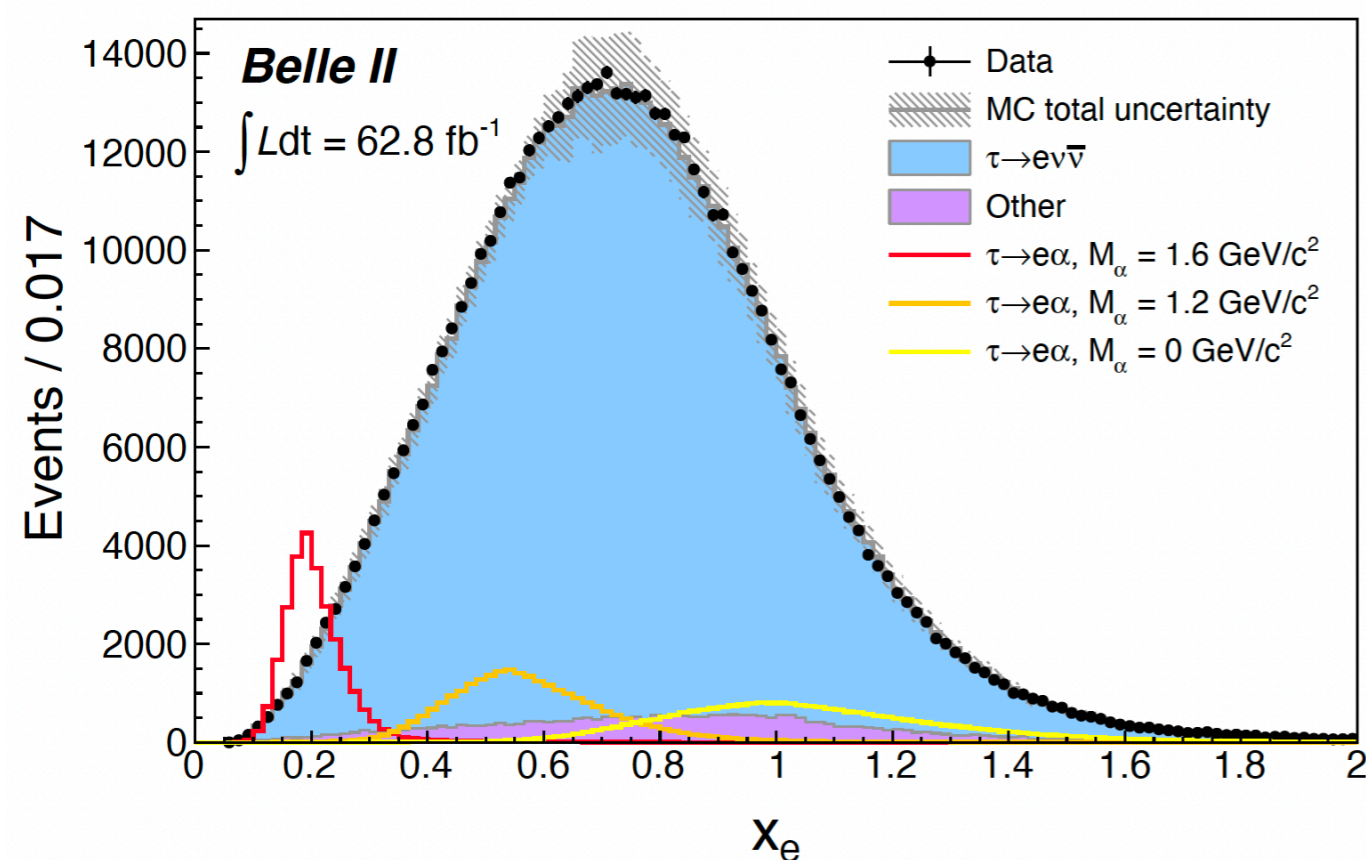
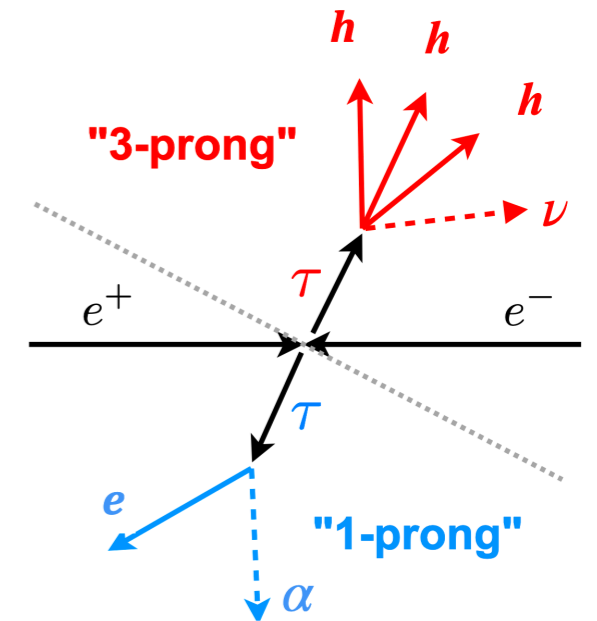
- **Event reconstruction:**

- ▶ Split event into hemispheres  $\perp$  to thrust axis ( $\hat{n}_T$ ) which maximizes  $\text{Thrust} = \max\left(\frac{\sum |\vec{p}_i| \cdot \hat{n}_T}{\sum |\vec{p}_i|}\right)$
- ▶ Require exactly 4 tracks: 1 in signal-side, 3 in tag-side
- ▶ Veto neutrals ( $\pi^0, \gamma$ ) to suppress hadronic background.

- **Backgrounds reduced by cuts:**

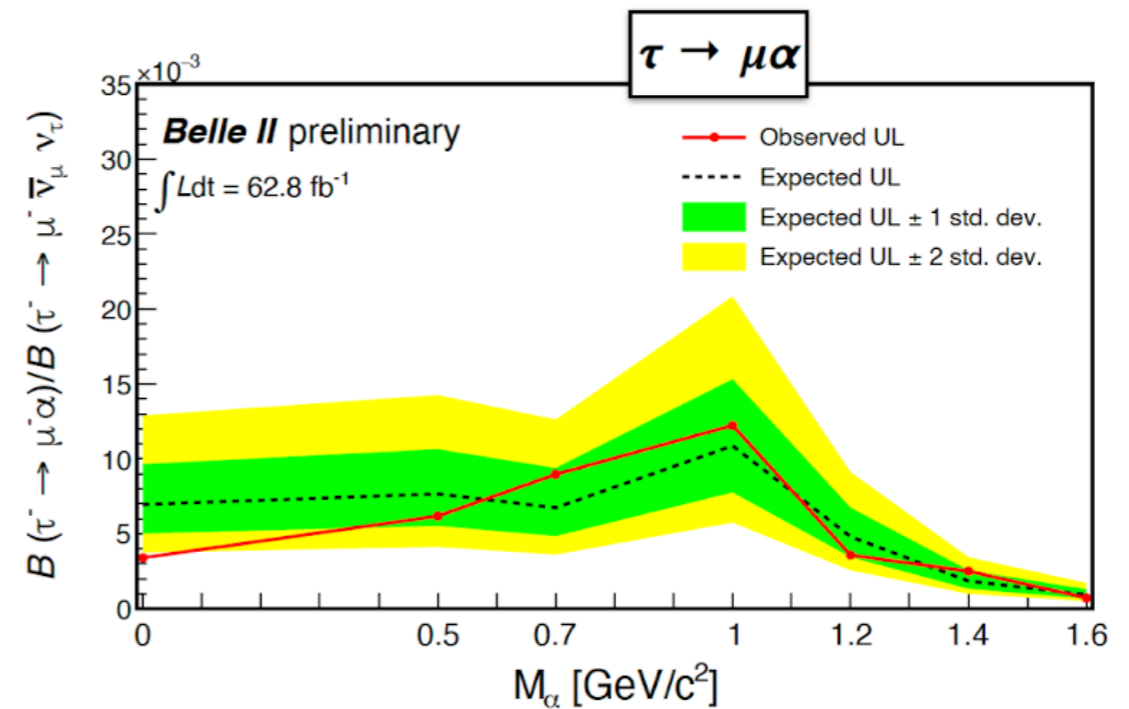
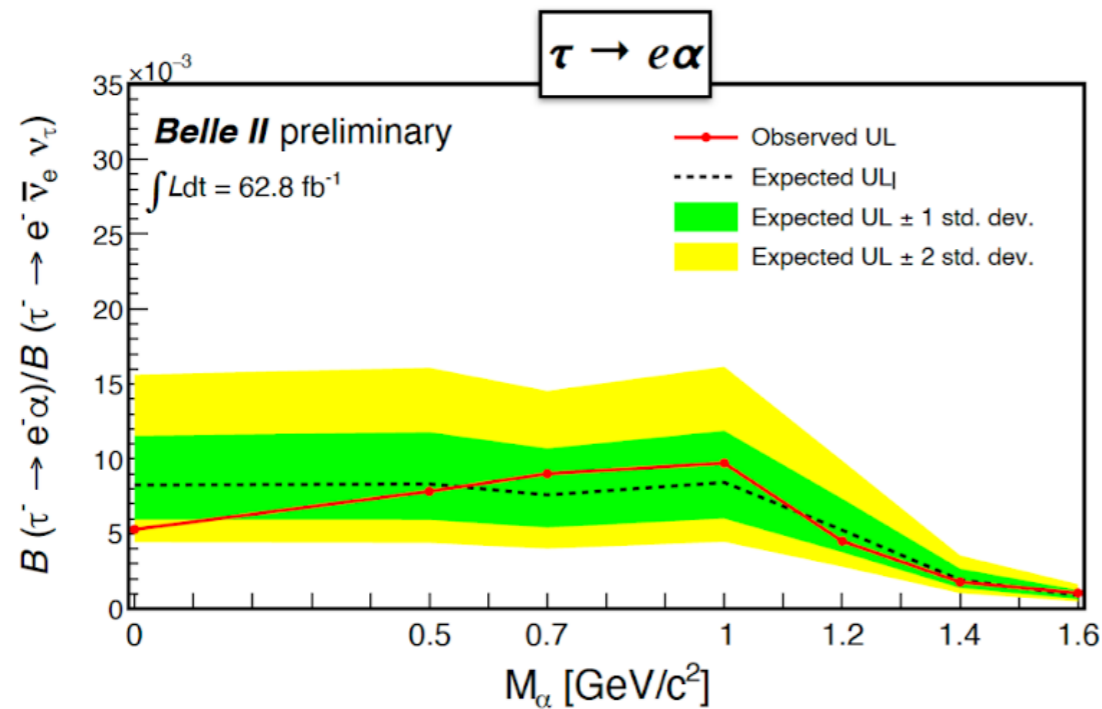
- ▶  $q\bar{q}, \ell^+\ell^-, \ell^+\ell^-\ell^+\ell^-, \ell^+\ell^-h^+h^-$  and  $\tau^+\tau^-$  with misidentified signal (e.g.  $\tau \rightarrow \pi\nu$ )

- **Data-MC agreement in the discriminating variable:  $x_\ell = 2E_\ell^{ps}/m_\tau$**

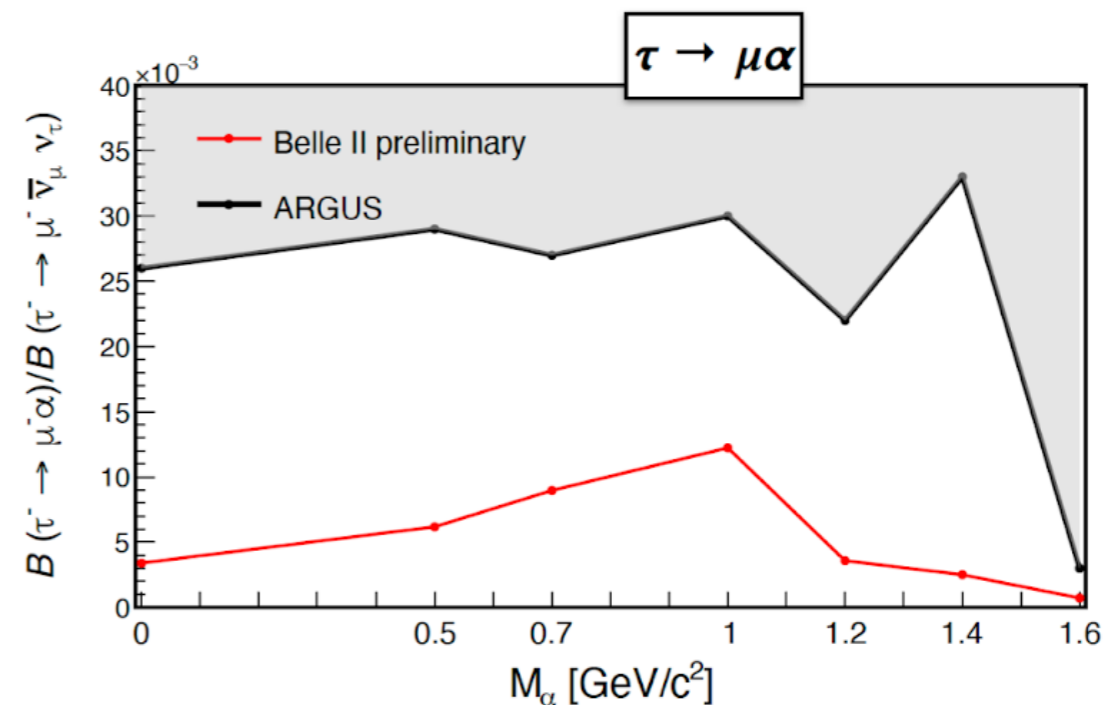
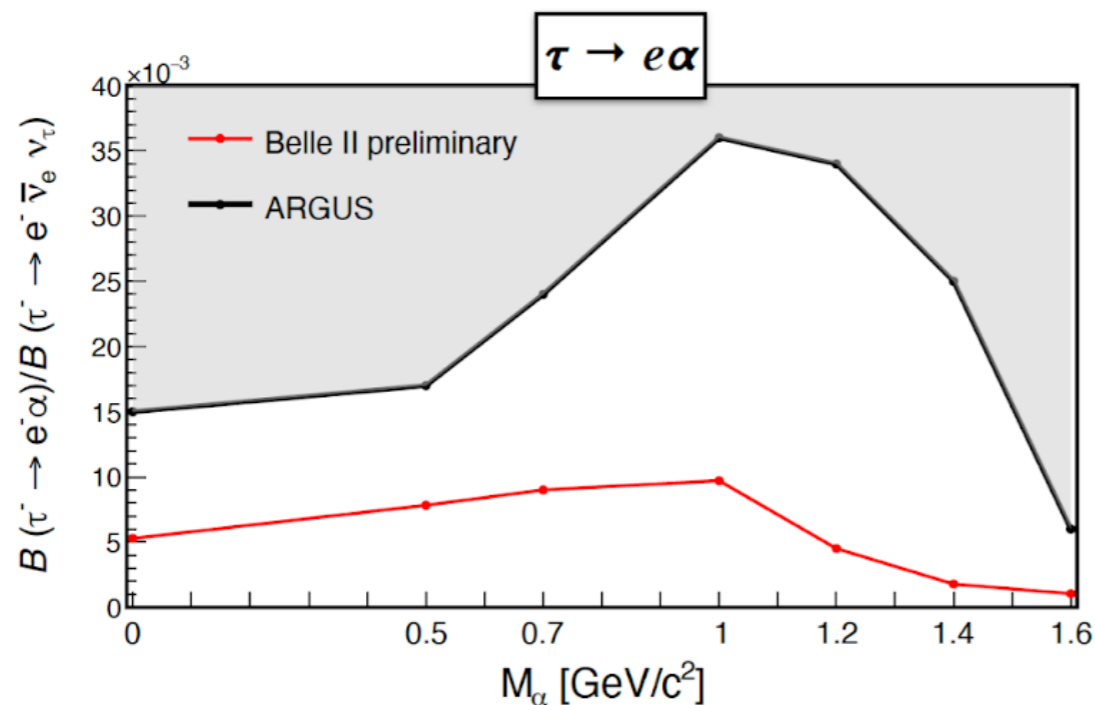


# $\tau \rightarrow \ell \alpha$ at Belle II

## 95% C.L. upper limits from Belle II (ICHEP'2022)



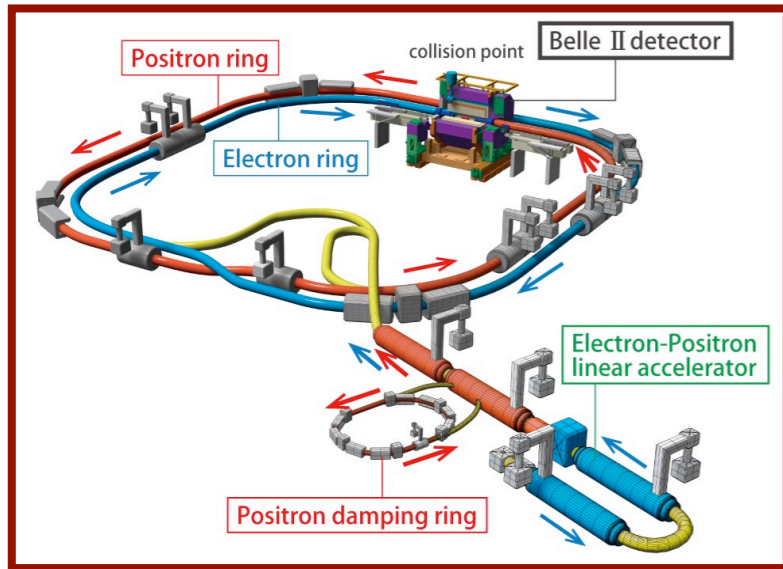
Comparison with previous limits from ARGUS (0.472 fb<sup>-1</sup>) [Z. Phys. C68 (1995) 25]



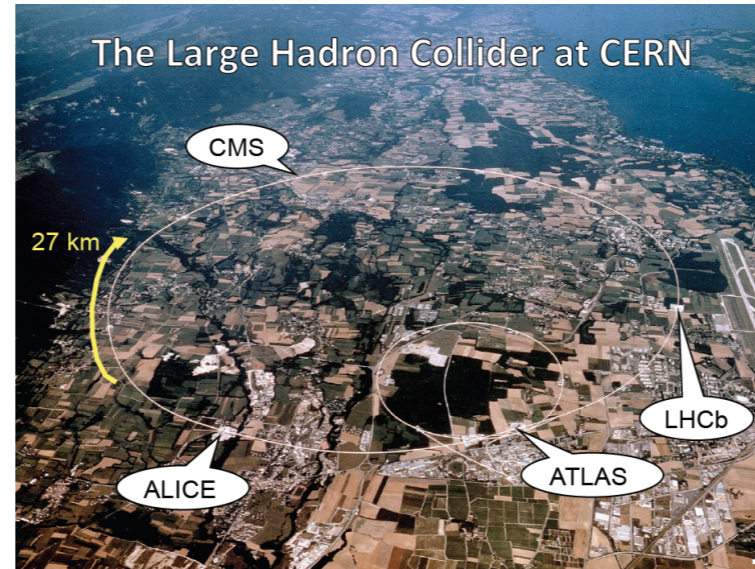


# Current and future experiments

**Belle II at SuperKEKB**



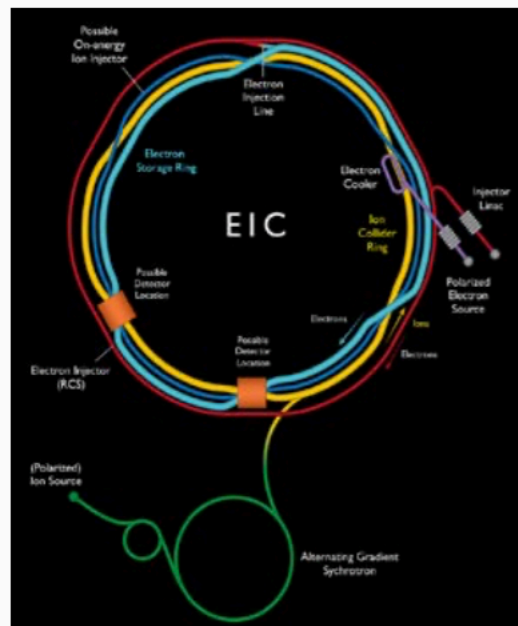
**ATLAS, CMS, LHCb at LHC**



**STCF proposal at China/Novosibirsk**



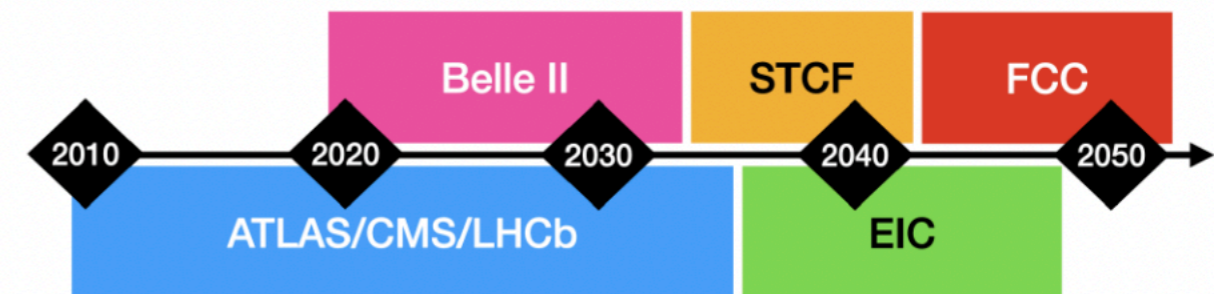
**EIC at Brookhaven**



**FCC-ee proposal – CERN**



**Tentative timeline**



[e-Print: 2203.14919 \[hep-ph\]](https://arxiv.org/abs/2203.14919)

# Estimates of experimental sensitivity in LFV searches

$$B_{UL}^{90} = N_{UL}^{90} / (N_{\tau} \times \epsilon)$$

- $\epsilon$ : high statistics signal MC simulated for different Data-taking periods

$\epsilon =$  Trigger . Reco . Topology . PID . Cuts . Signal-Box

90%    70%    70%    50%    50%    50%

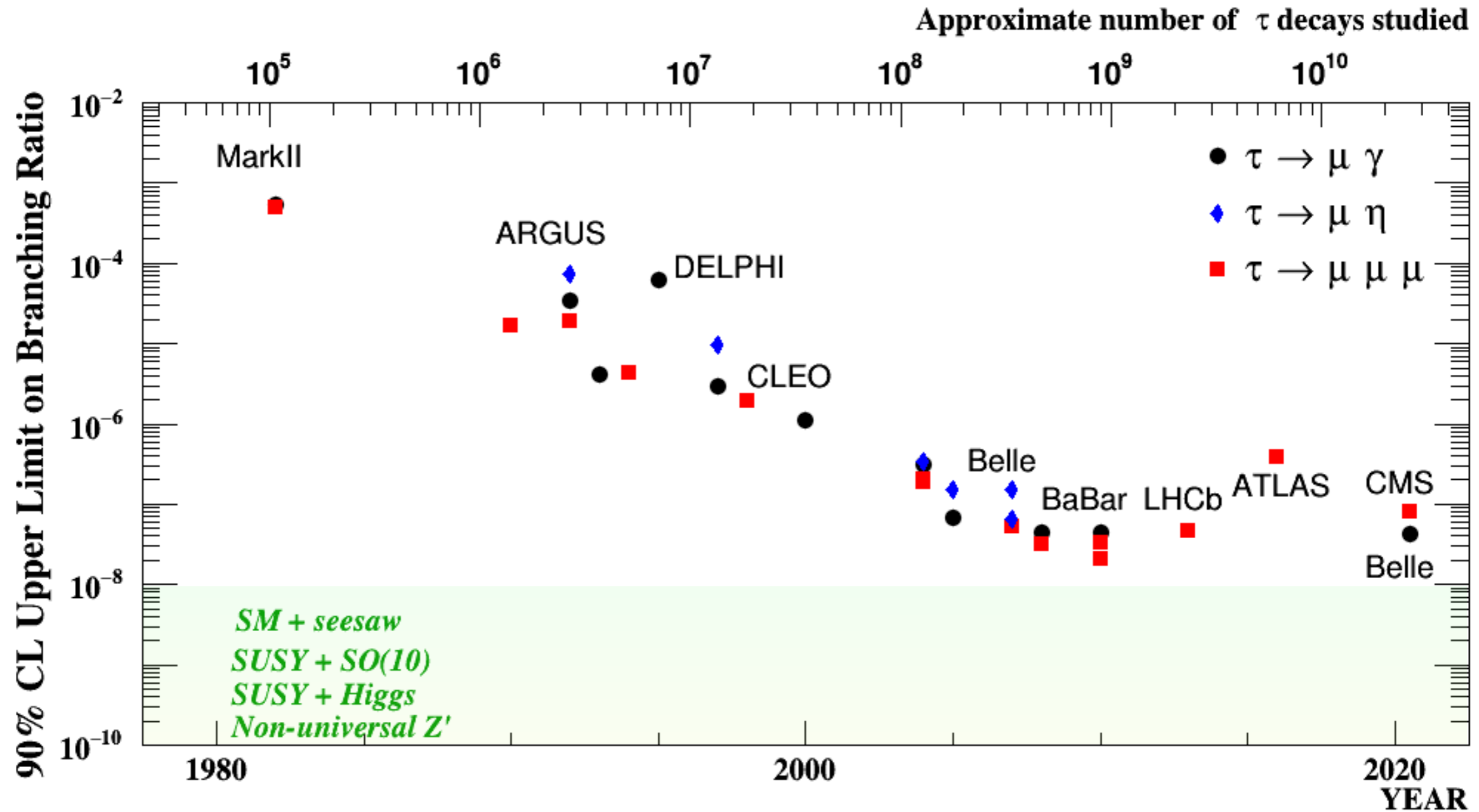
**Cumulative:**

90%    63%    44%    22%    11%    ~5%

	$\sqrt{s}$	Luminosity (L)	$N_{\tau} = 2L\sigma$
Belle II	10.58 GeV	50 ab <sup>-1</sup>	9.2 x10 <sup>10</sup>
HL-LHC	14 TeV	3 ab <sup>-1</sup>	$\mathcal{O}(10^{15})$
STCF	2-7 GeV	1 ab <sup>-1</sup>	7.0 x10 <sup>9</sup>
FCC-ee	91.2 GeV	150 ab <sup>-1</sup>	3.4 x 10 <sup>11</sup>

(Efficiency much lower)

# Current status of LFV $\tau$ decays $\sim 10^{-7}$



# $\tau \rightarrow \mu\mu\mu$ at Belle II

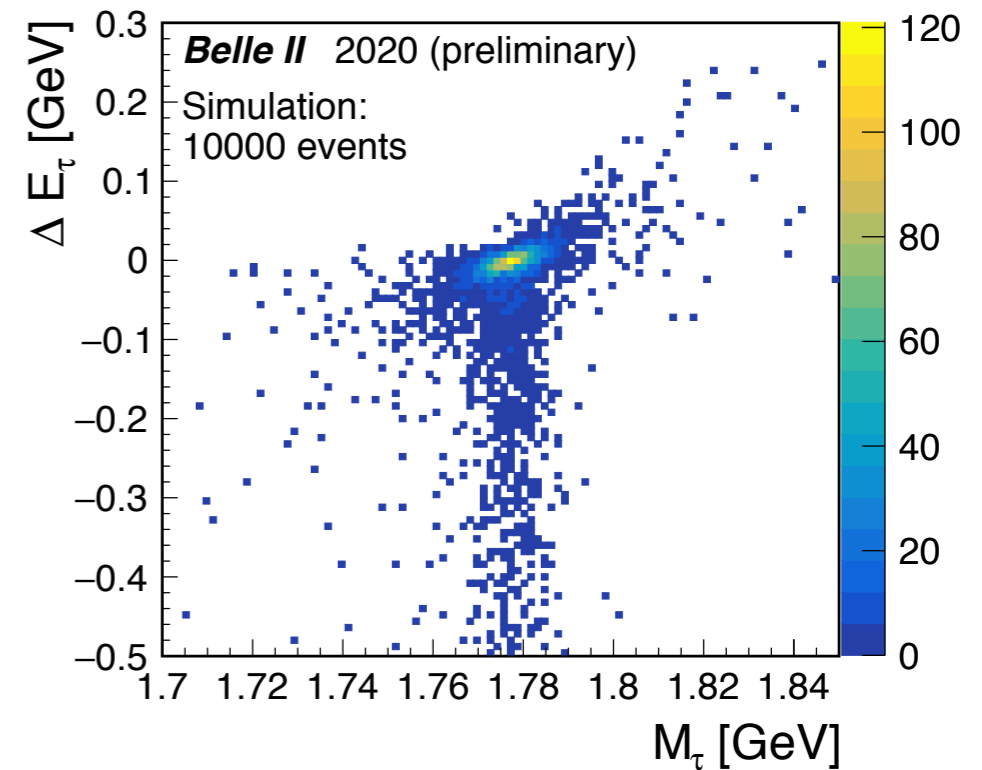
- Known initial conditions (beam energy constraint)
- Clean environment (fewer backgrounds)

Two independent variables:

$$M_\tau = \sqrt{E_{\mu\mu\mu}^2 - P_{\mu\mu\mu}^2}$$

$$\Delta E = E_{\mu\mu\mu}^{CMS} - E_{\text{beam}}^{CMS}$$

- ➔  $\Delta E$  close to 0 for signal
- ➔ Mass of tau daughters close to  $\tau$  mass



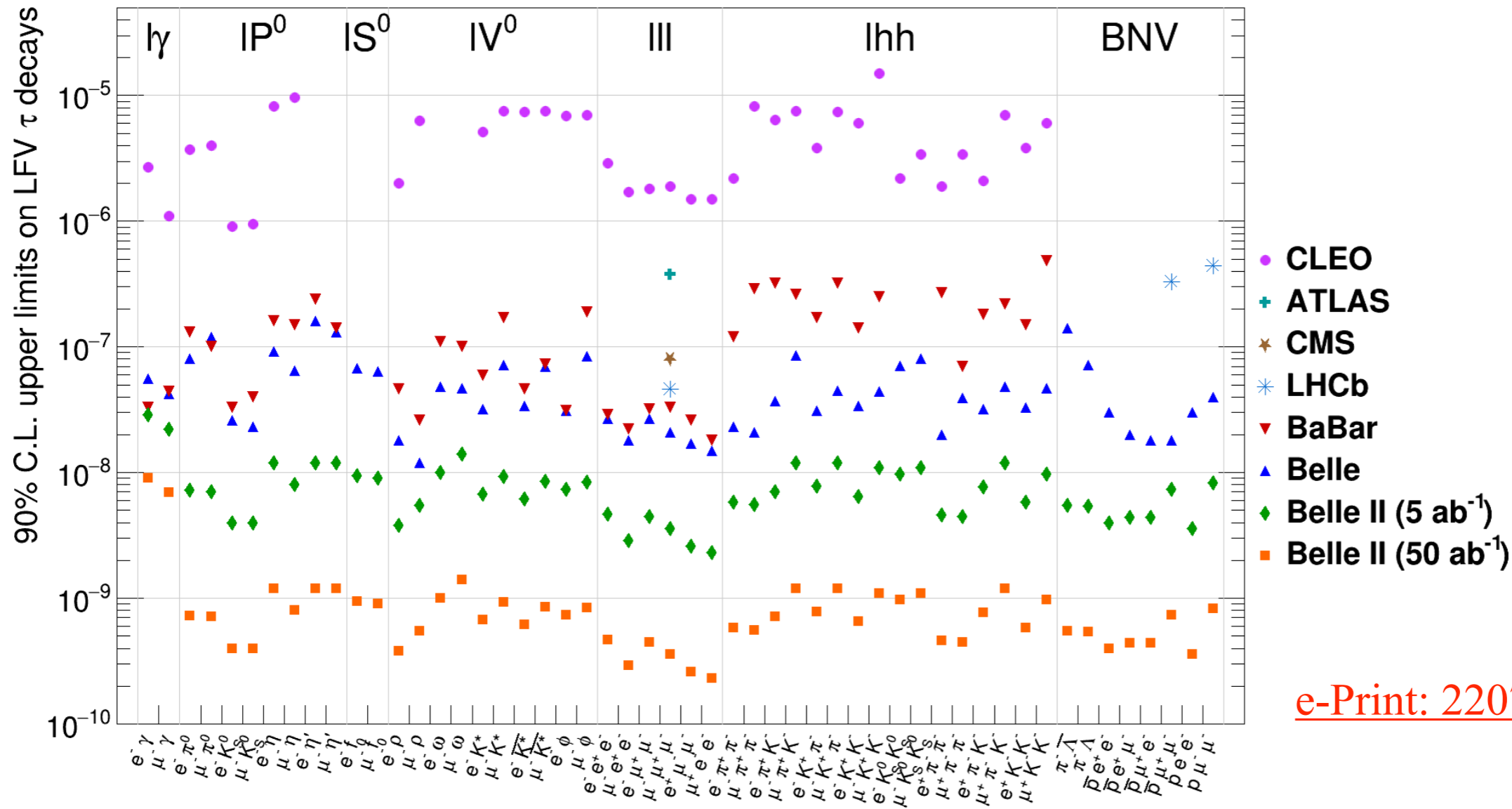
**Higher signal efficiency is foreseen at Belle II than at Belle or BaBar**

- higher trigger efficiencies
- improved vertexing detectors
- upgraded tracking /calorimetry
- momentum dependent particle identification optimizations

**Expected Belle II sensitivity:  $\mathcal{B}(\tau \rightarrow \mu\mu\mu) < 3.6 \times 10^{-10}$  with  $50 \text{ ab}^{-1}$**

# Projected limits at Belle II

	Background limited search	Background free search
$N_{UL}^{90}$	$\sqrt{\mathcal{L}}$	2.44 [Feldman – Cousins for $N_{obs} = 0$ ]
$B_{UL}^{90}$	$\propto 1/\sqrt{\mathcal{L}}$	$\propto 1/\mathcal{L}$



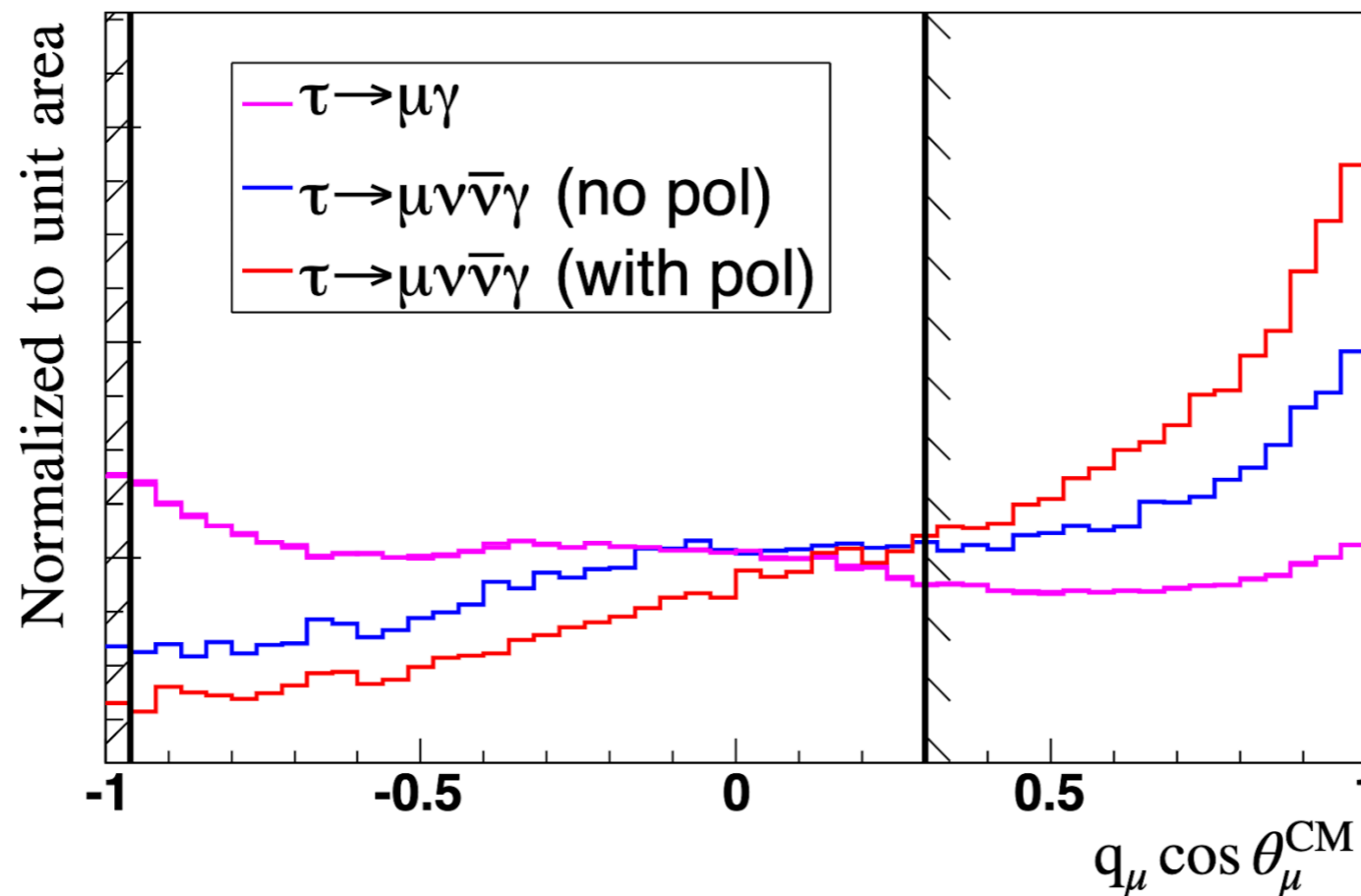
Projections

[e-Print: 2207.06307 \[hep-ex\]](https://arxiv.org/abs/2207.06307)

**Belle II to probe LFV in several channels  $\approx \mathcal{O}(10^{-10})$  to  $\mathcal{O}(10^{-9})$  with 50 ab<sup>-1</sup>**

# Beam polarization upgrade at SuperKEKB/Belle II

- Further improvements are expected with polarized beams
- With beam polarization, helicity distributions can suppress backgrounds
- Optimization study shows at least 10% improvement in  $\tau \rightarrow \ell \gamma$  sensitivity

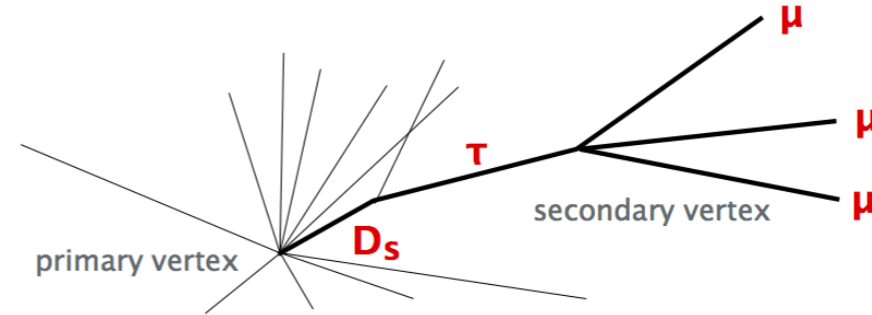


<https://arxiv.org/pdf/0810.1312.pdf>

Intriguing aspect of having the polarization is the possibility to determine the helicity structure of the LFV coupling in  $\tau \rightarrow \mu \mu \mu$  from Dalitz plots.

# $\tau \rightarrow \mu\mu\mu$ at LHCb

Using D decays ( $3\text{fb}^{-1}$  at 7/8 TeV)



$$\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-) = \frac{\mathcal{B}(D_s^- \rightarrow \phi(\mu^+ \mu^-) \pi^-)}{\mathcal{B}(D_s^- \rightarrow \tau^- \bar{\nu}_\tau)} \times f_\tau^{D_s} \times \frac{\epsilon_{\text{cal}}^{\text{R}}}{\epsilon_{\text{sig}}^{\text{R}}} \times \frac{\epsilon_{\text{cal}}^{\text{T}}}{\epsilon_{\text{sig}}^{\text{T}}} \times \frac{N_{\text{sig}}}{N_{\text{cal}}} \equiv \alpha N_{\text{sig}}$$

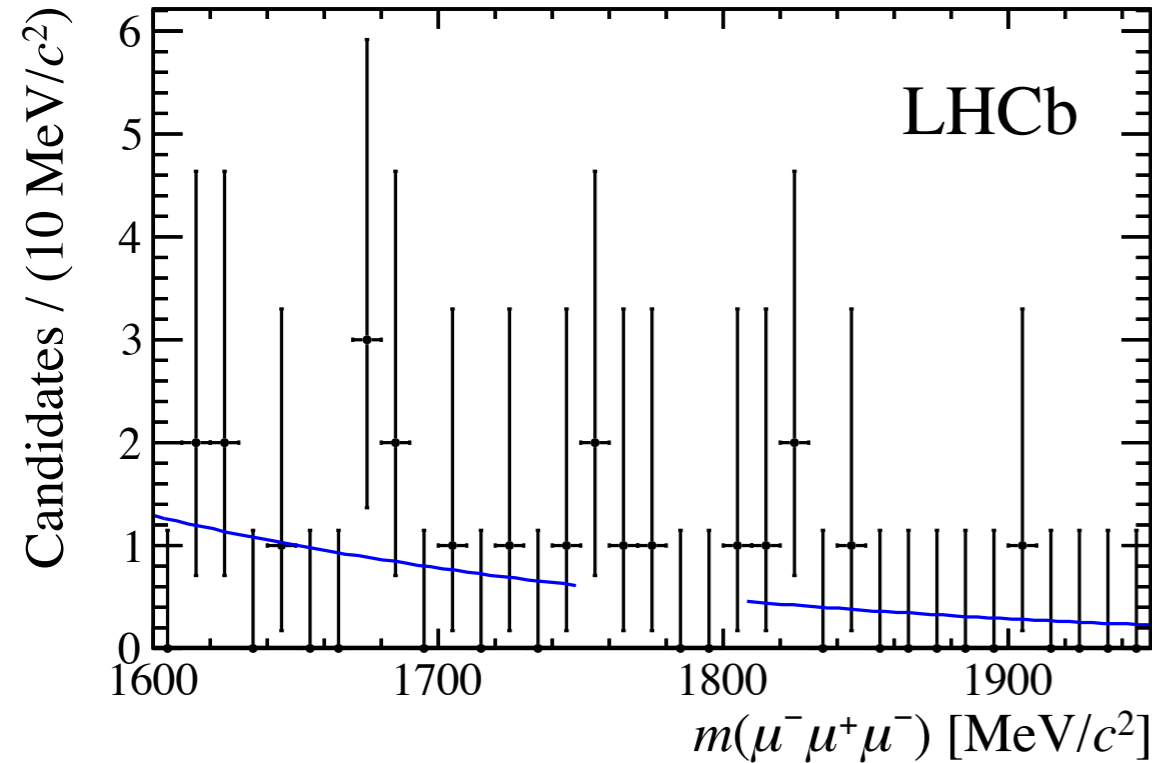
► LHCb limit on the  $\tau^- \rightarrow \mu^- \mu^+ \mu^-$  branching ratio

$$\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-) < 4.6 \times 10^{-8} \quad @ 90\% \text{ C.L.}$$

[JHEP 02 \(2015\) 121](#)

## LHCb-PUB-2018-009

The cross-section is five orders of magnitude larger than at Belle II. This compensates for the higher background levels and lower integrated luminosity. As pointed out in [76], during the HL-LHC era, the LHCb Upgrade II detector will allow to collect  $300 \text{fb}^{-1}$ . With this large data sample, LHCb will be able to probe the branching ratio down to  $O(10^{-9})$ , and either independently confirm any Belle II discovery or significantly improve the limit.



# $\tau \rightarrow \mu\mu\mu$ at ATLAS & CMS

- ▶ ATLAS limit on the  $\tau^- \rightarrow \mu^- \mu^+ \mu^-$  branching ratio

(20 fb<sup>-1</sup> at 8 TeV)

$$\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-) < 3.76 \times 10^{-7} \quad @ 90\% \text{ C.L.}$$

[Eur. Phys. J. C \(2016\) 76:232](#)

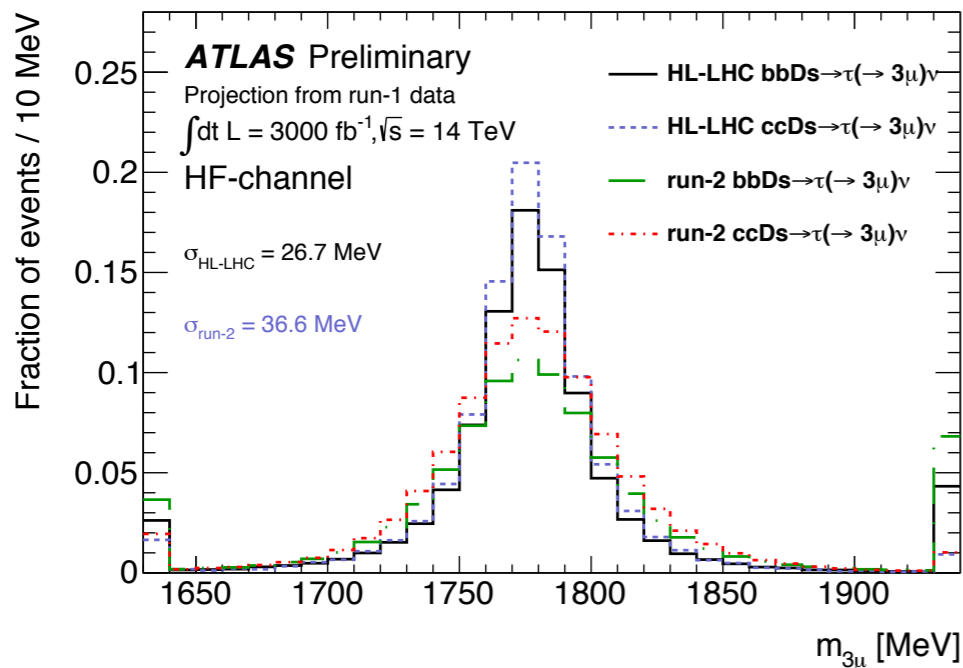
- ▶ CMS limit on the  $\tau^- \rightarrow \mu^- \mu^+ \mu^-$  branching ratio

(33 fb<sup>-1</sup> at 13 TeV)

$$\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-) < 8.0 \times 10^{-8} \quad @ 90\% \text{ C.L.}$$

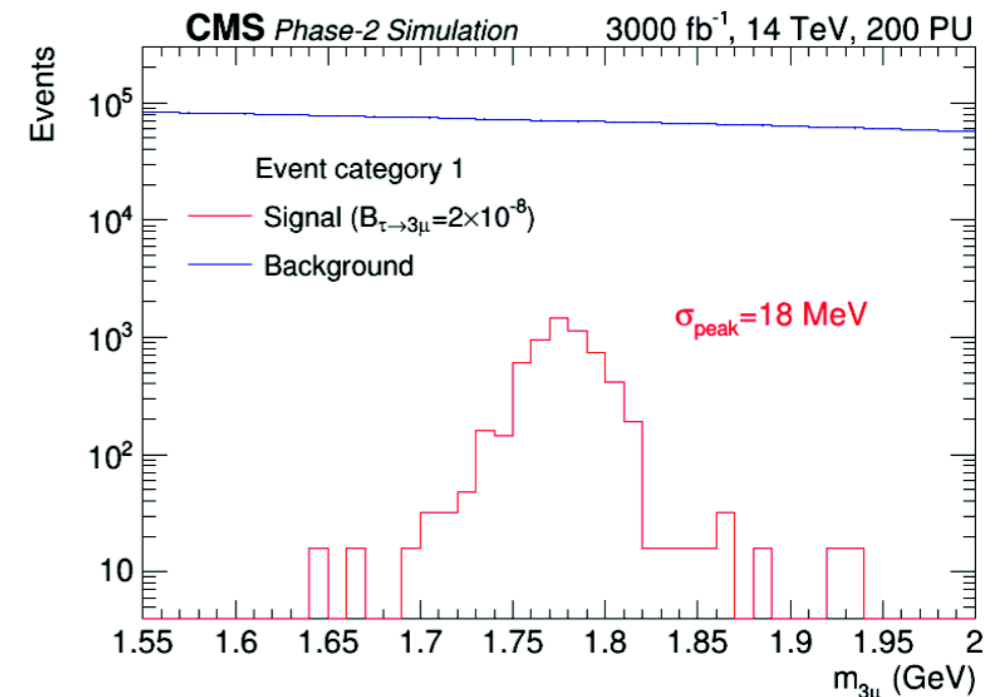
[JHEP 01 \(2021\) 163](#)

Future prospects using D & B decays (3 ab<sup>-1</sup> at 14 TeV) :



[ATL-PHYS-PUB-2018-032](#)

Scenario	$\mathcal{A} \times \epsilon$ [%]	$N_{\text{bkg}}^{\text{exp}}$	90% CL UL on BR( $\tau \rightarrow 3\mu$ ) [ $10^{-9}$ ]
High background	0.88	507.05	6.40
Medium background	0.88	152.12	2.31
Low background	0.88	50.71	1.03



[CMS-TDR-016](#)

	Category 1	Category 2
Number of background events	$2.4 \times 10^6$	$2.6 \times 10^6$
Number of signal events	4580	3640
Trimuon mass resolution	18 MeV	31 MeV
$\mathcal{B}(\tau \rightarrow 3\mu)$ limit per event category	$4.3 \times 10^{-9}$	$7.0 \times 10^{-9}$
$\mathcal{B}(\tau \rightarrow 3\mu)$ 90% C.L. limit	$3.7 \times 10^{-9}$	



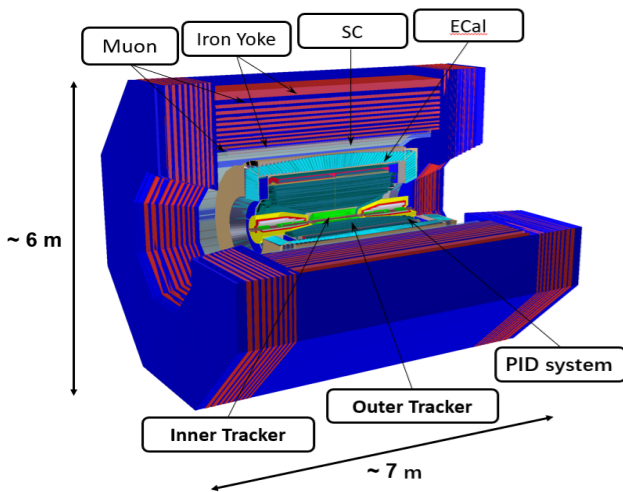
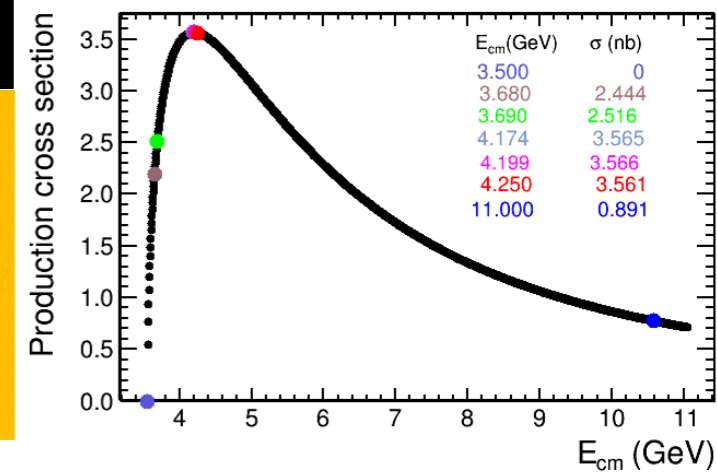
# Super Tau-Charm Facility

## “Physics Potential of a Super tau-Charm Facility” (RF/SNOWMASS21-RF7 RF1 STCF-013.pdf)

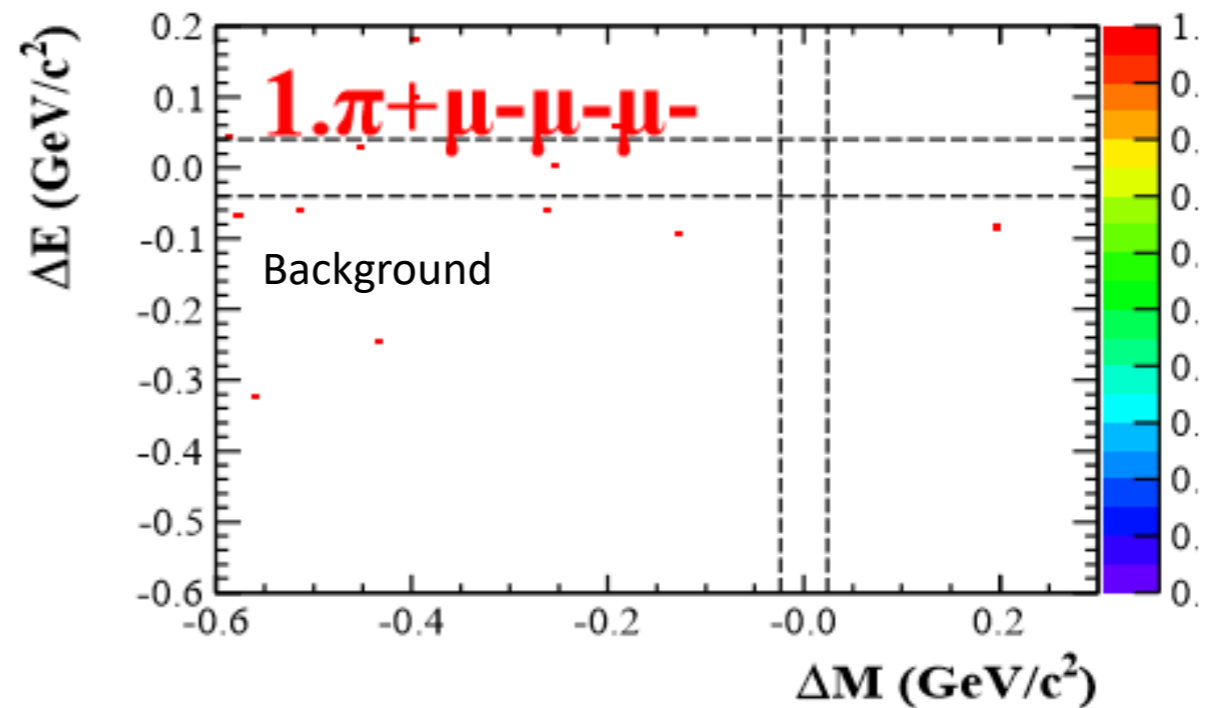
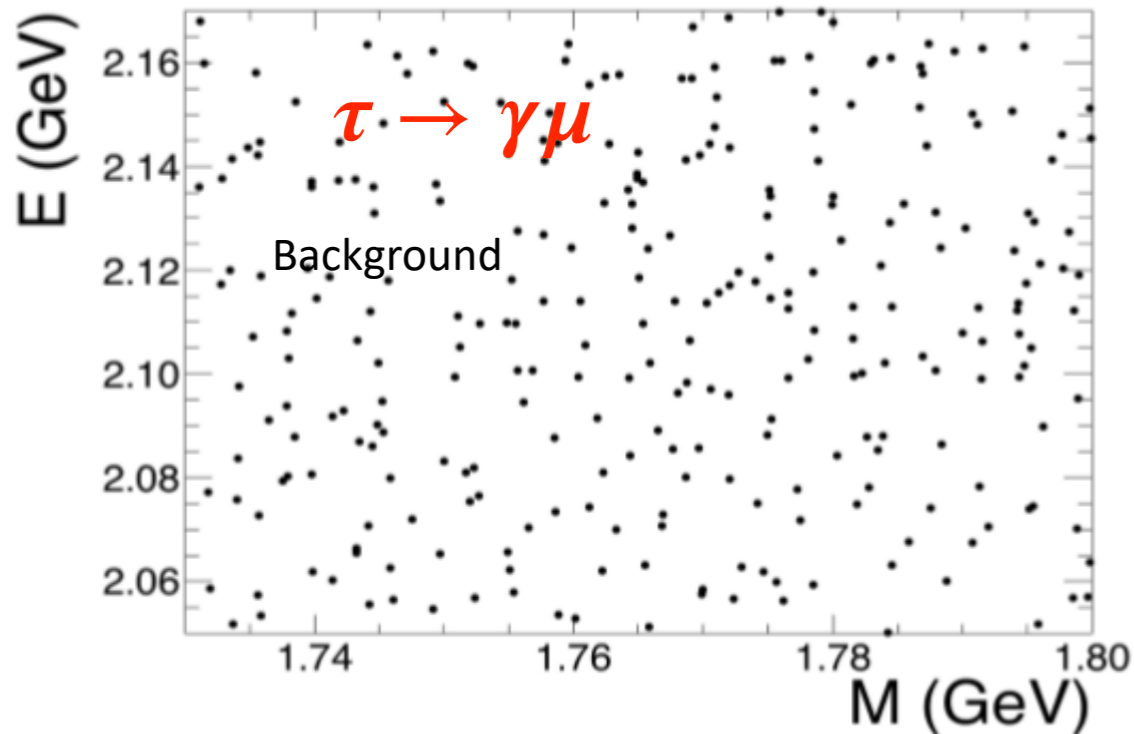
- Peaking luminosity  $> 0.5 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$  at 4 GeV
- Energy range  $E_{\text{cm}} = 2\text{-}7 \text{ GeV}$
- **Potential** to increase luminosity and realize beam polarization
- A nature extension and a viable option for China accelerator project in the post **BEPCII/BESIII** era

PoS CHARM2020 (2021), 007

Physics 49 (2020) 8, 513-524



At 4.26 GeV, number of tau pairs per year:  $N_{\tau\tau} \sim 1.0 \text{ ab}^{-1} \times 3.5 \text{ nb} = 3.5 \times 10^9$



> STCF with  $1 \text{ ab}^{-1}$ :

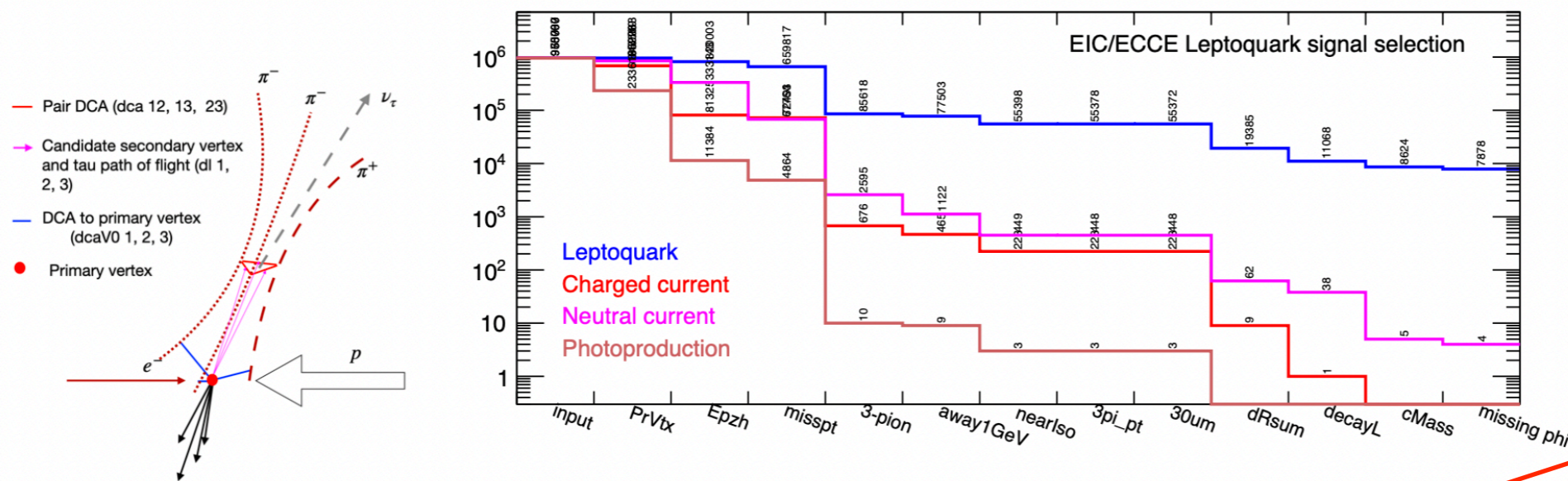
$$\mathcal{B}_{UL}^{90}(\tau \rightarrow \gamma\mu) < \frac{N_{UL}^{90}}{2\epsilon N_{\tau\tau}} \sim 1.2 \times 10^{-8}$$

> STCF with  $1 \text{ ab}^{-1}$ :

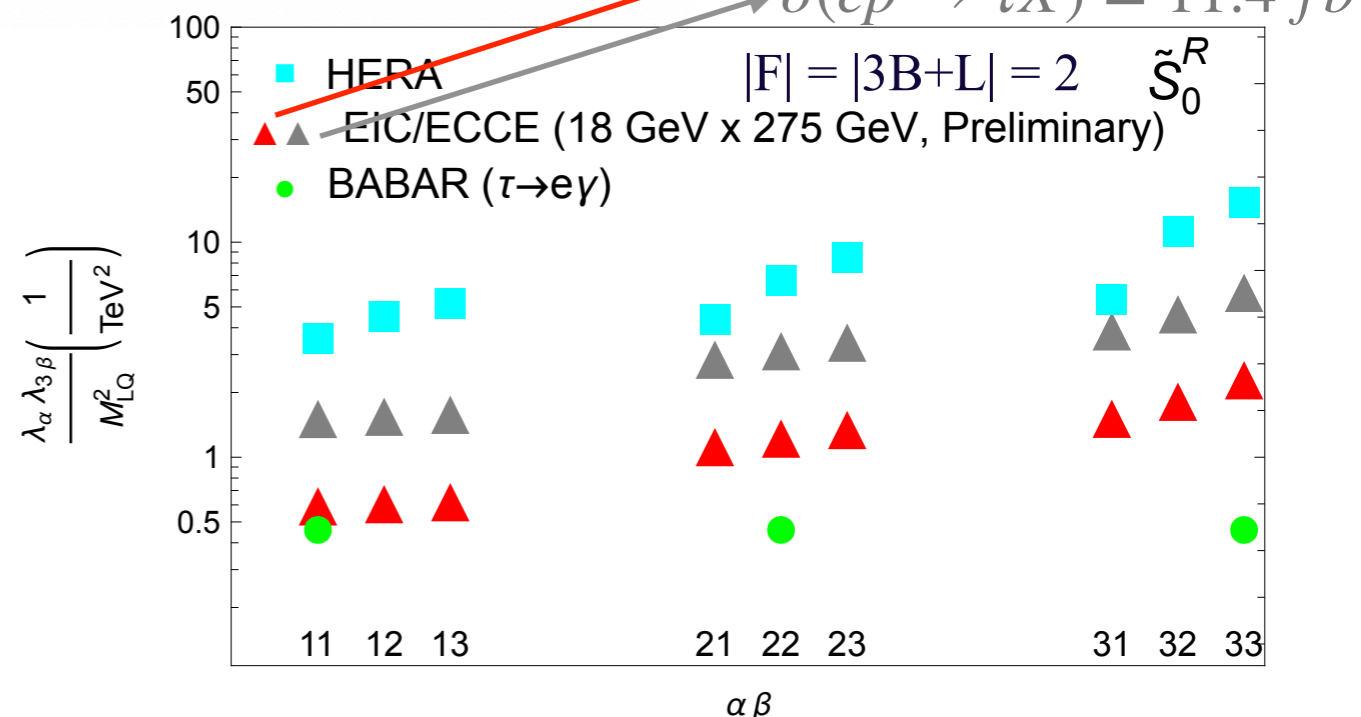
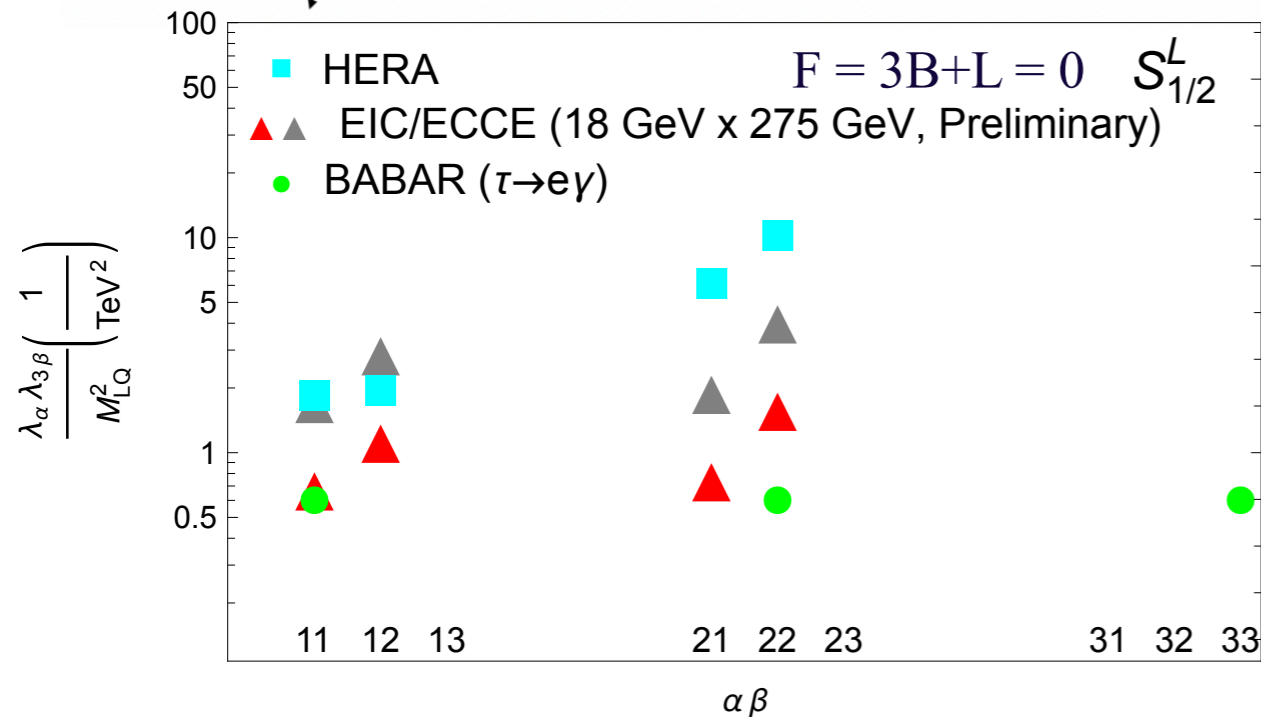
$$\mathcal{B}_{UL}^{90}(\tau \rightarrow \mu\mu\mu) < \frac{N_{UL}^{90}}{2\epsilon N_{\tau\tau}} \sim 1.4 \times 10^{-9}$$

# $e \rightarrow \tau$ transitions at EIC

Sensitivity study with  $100 \text{ fb}^{-1}$  of data to be collected at  $\sqrt{s} = 140 \text{ GeV}$  (18 GeV electron on 275 GeV protons)



e-Print: [2207.10261 \[hep-ph\]](https://arxiv.org/abs/2207.10261)

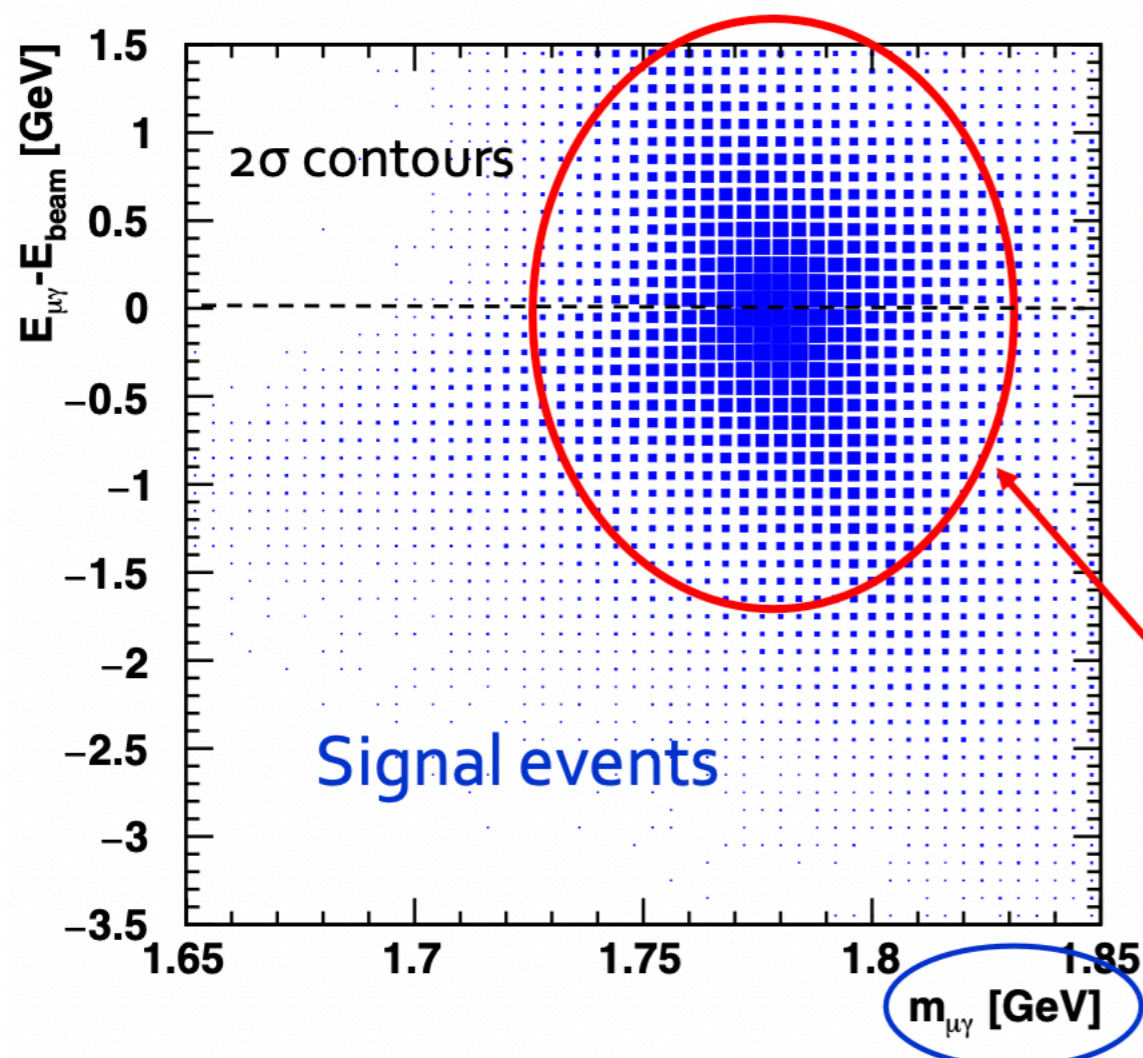


Expect to improve current sensitivity by an order of magnitude



$$\mathcal{B}(\tau \rightarrow \mu\gamma)$$

e-Print: [1811.09408 \[hep-ex\]](https://arxiv.org/abs/1811.09408)



- ◆ **Main background:** Radiative events (IRS+FSR),  $e^+e^- \rightarrow \tau^+\tau^-\gamma$ 
  - $\tau \rightarrow \mu\gamma$  decay faked by combination of  $\gamma$  from IRS/FSR and  $\mu$  from  $\tau \rightarrow \mu\nu\bar{\nu}$

Smear with assumed FCC-ee detector resolutions (ILC-like detector):

- Muon momentum [GeV]
 
$$\sigma(p_T)/p_T = 2 \times 10^{-5} \times p_T \oplus 1 \times 10^{-3}$$
- Photon ECAL energy [GeV]
 
$$\sigma(E)/E = 0.165/\sqrt{E} \oplus 0.010/E \oplus 0.011$$
- Photon ECAL spatial [mm]
 
$$\sigma(x) = \sigma(y) = (6/E \oplus 2) \text{ mm}$$

$$\sigma(m_{\gamma\mu}) = 26 \text{ MeV}; \quad \sigma(E_{\gamma\mu}) = 850 \text{ MeV}$$

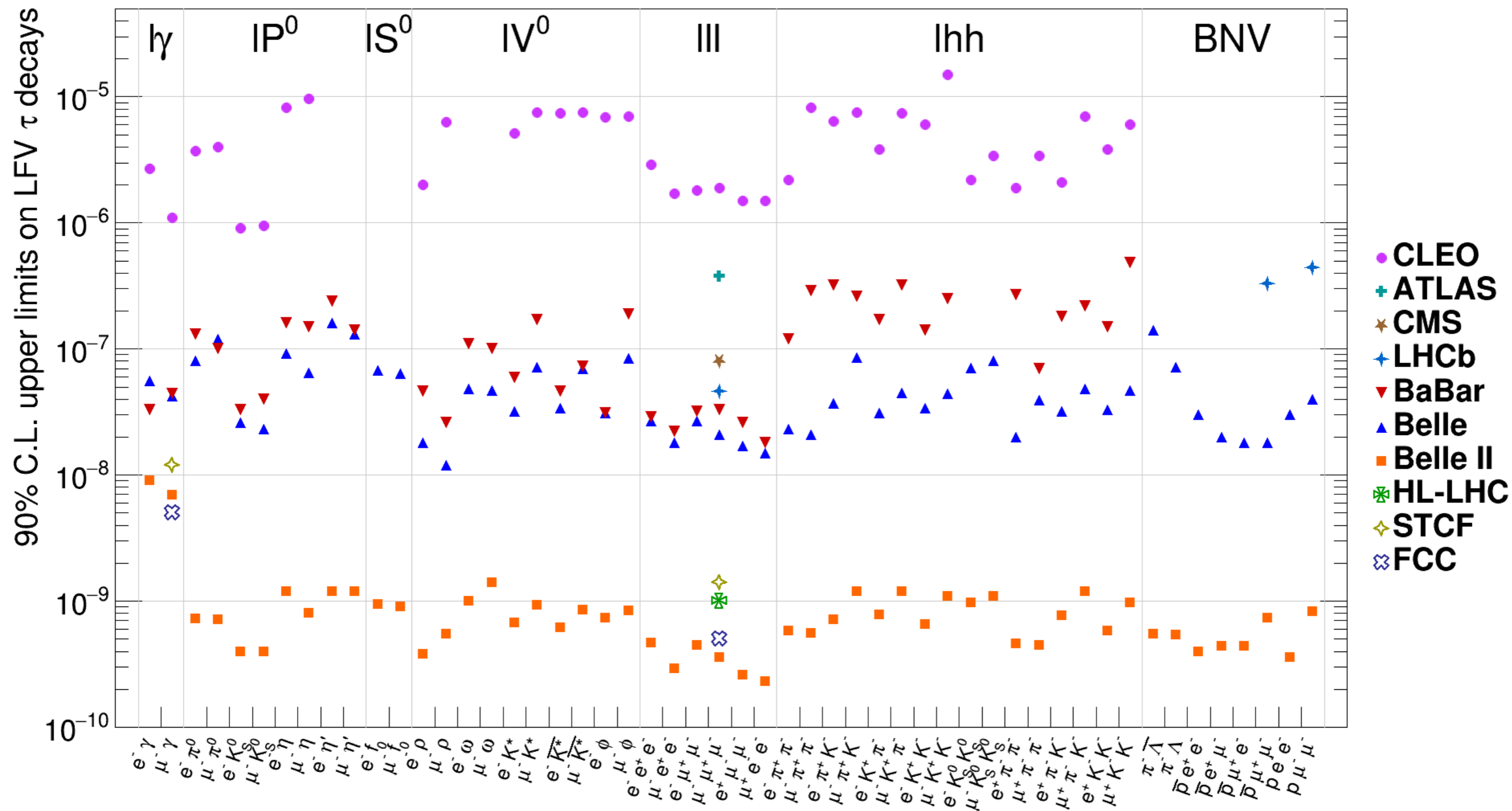
- From study (assuming 25% signal & background efficiency), projected BR sensitivity

$$2 \times 10^{-9}$$

$$\mathcal{B}(\tau \rightarrow \mu\mu\mu)$$

- Expect this search to have *very low* background, even with FCC-ee like statistics
- Should be able to have sensitivity down to BRs of  $\lesssim 10^{-10}$

# Summary of experimental prospects of $\tau$ decays



e-Print: [2203.14919 \[hep-ph\]](https://arxiv.org/abs/2203.14919)

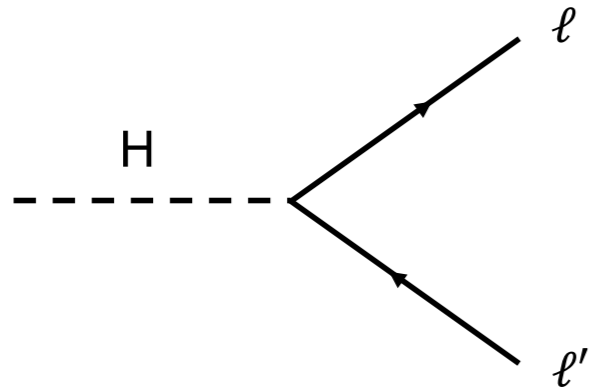
# Summary of transitions with $\tau$ in the final state

Channel	Upper limit	Experiment [Ref.]
$J/\psi \rightarrow e^\pm \tau^\mp$	$7.5 \times 10^{-8}$	BES III [108]
$J/\psi \rightarrow \mu^\pm \tau^\mp$	$2.0 \times 10^{-6}$	BES [109]
$B^0 \rightarrow e^\pm \tau^\mp$	$2.8 \times 10^{-5}$	BaBar [110]
$B^0 \rightarrow \mu^\pm \tau^\mp$	$2.2 \times 10^{-5}$	BaBar [110]
	$1.2 \times 10^{-5}$	LHCb [62]
$B^+ \rightarrow \pi^+ e^\pm \tau^\mp$	$7.5 \times 10^{-5}$	BaBar [111]
$B^+ \rightarrow \pi^+ \mu^\pm \tau^\mp$	$7.2 \times 10^{-5}$	BaBar [111]
$B^+ \rightarrow K^+ e^\pm \tau^\mp$	$3.0 \times 10^{-5}$	BaBar [111]
$B^+ \rightarrow K^+ \mu^\pm \tau^\mp$	$4.8 \times 10^{-5}$	BaBar [111]
$B^+ \rightarrow K^+ \mu^- \tau^+$	$3.9 \times 10^{-5}$	LHCb [63]
$B_s^0 \rightarrow \mu^\pm \tau^\mp$	$3.4 \times 10^{-5}$	LHCb [62]
$\Upsilon(1S) \rightarrow e^\pm \tau^\mp$	$2.7 \times 10^{-6}$	Belle [112]
$\Upsilon(1S) \rightarrow \mu^\pm \tau^\mp$	$2.7 \times 10^{-6}$	Belle [112]
$\Upsilon(2S) \rightarrow e^\pm \tau^\mp$	$3.2 \times 10^{-6}$	BaBar [113]
$\Upsilon(2S) \rightarrow \mu^\pm \tau^\mp$	$3.3 \times 10^{-6}$	BaBar [113]
$\Upsilon(3S) \rightarrow e^\pm \tau^\mp$	$4.2 \times 10^{-6}$	BaBar [113]
$\Upsilon(3S) \rightarrow \mu^\pm \tau^\mp$	$3.1 \times 10^{-6}$	BaBar [113]
$Z \rightarrow e^\pm \tau^\mp$	$5.0 \times 10^{-6}$ (*)	ATLAS [69]
$Z \rightarrow \mu^\pm \tau^\mp$	$6.5 \times 10^{-6}$ (*)	ATLAS [69]
$H \rightarrow e^\pm \tau^\mp$	0.47% (*)	ATLAS [65]
	0.22% (*)	CMS [66]
$H \rightarrow \mu^\pm \tau^\mp$	0.28% (*)	ATLAS [65]
	0.15% (*)	CMS [66]
	26% (*)	LHCb [64]

Table 2: Bounds on selected LFV decays with  $\tau$  in the final state are shown at 90% CL, except for limits on those decays marked with a (\*), which are quoted at 95% CL.

[e-Print: 2203.14919 \[hep-ph\]](https://arxiv.org/abs/2203.14919)

# LFV decays of Higgs Boson



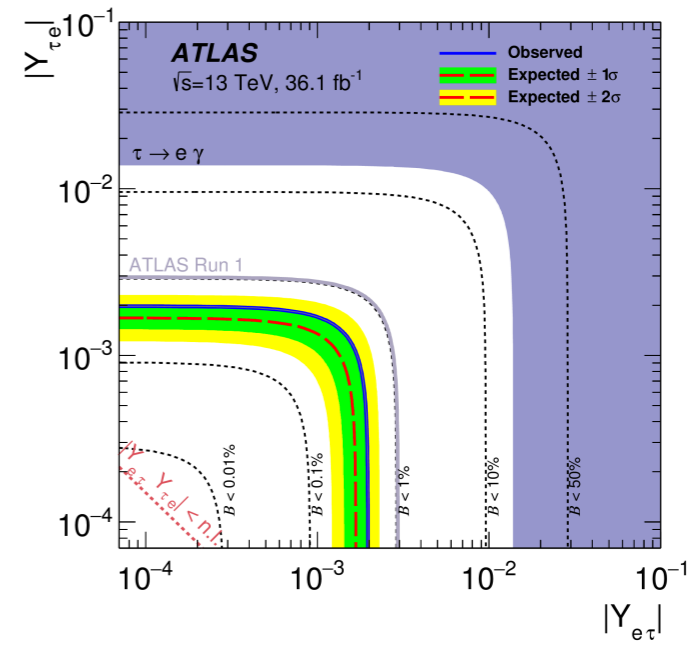
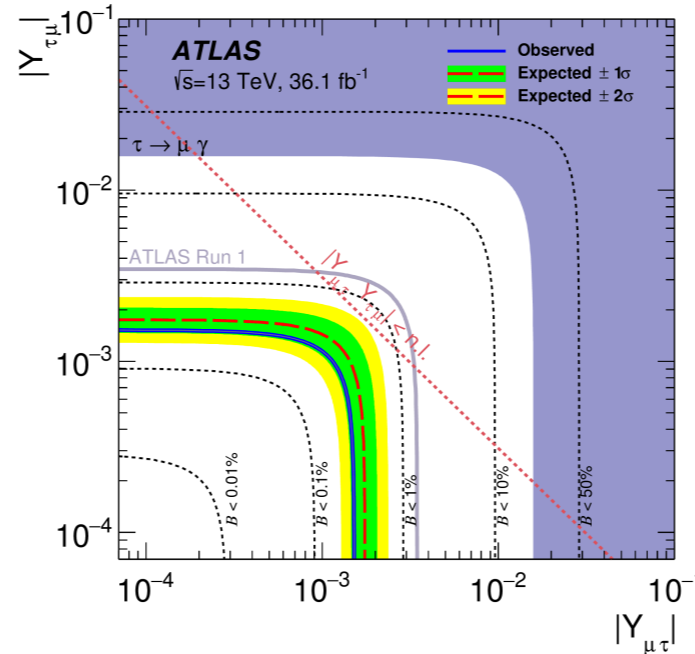
Yukawa off-diagonal terms

$$\mathcal{L}_Y = -m_i \bar{f}_L^i f_R^i - Y_{ij} (\bar{f}_L^i f_R^j) h + h.c. + \dots,$$

In the SM:  $Y_{ij} = (m_i/v)\delta_{ij}$

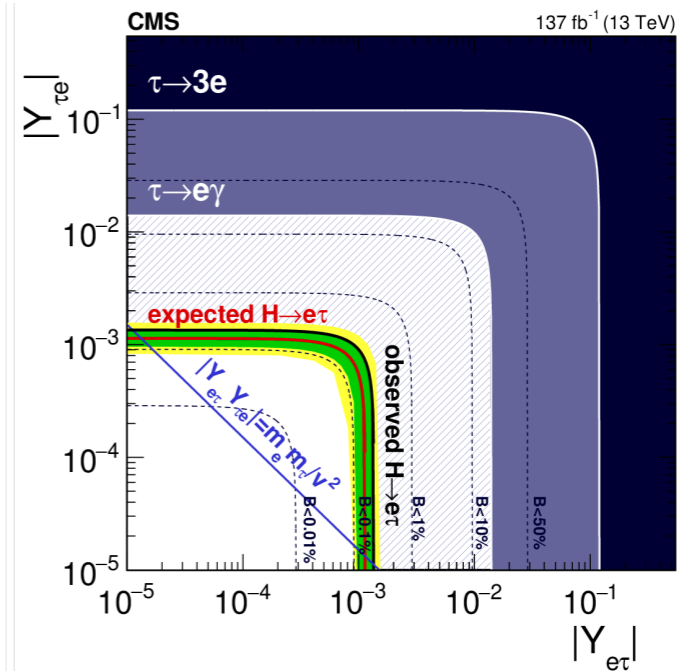
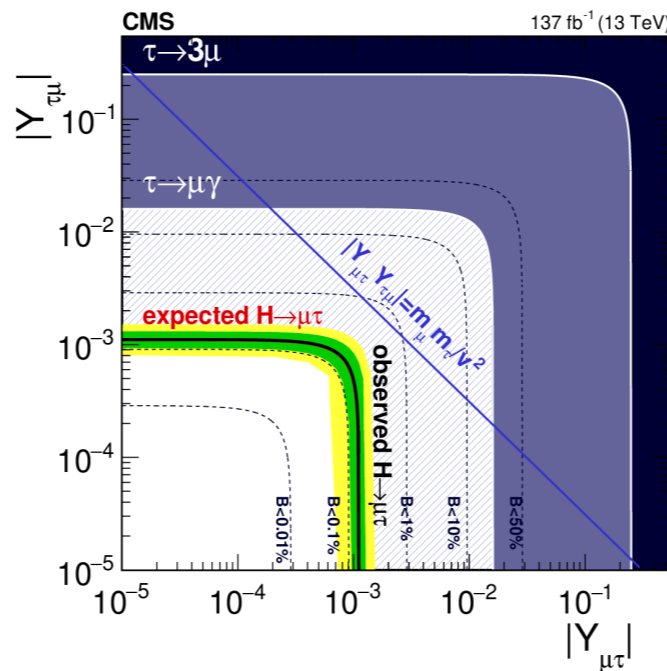
ATLAS

[Phys. Lett. B 800 \(2020\) 135069](#)



CMS

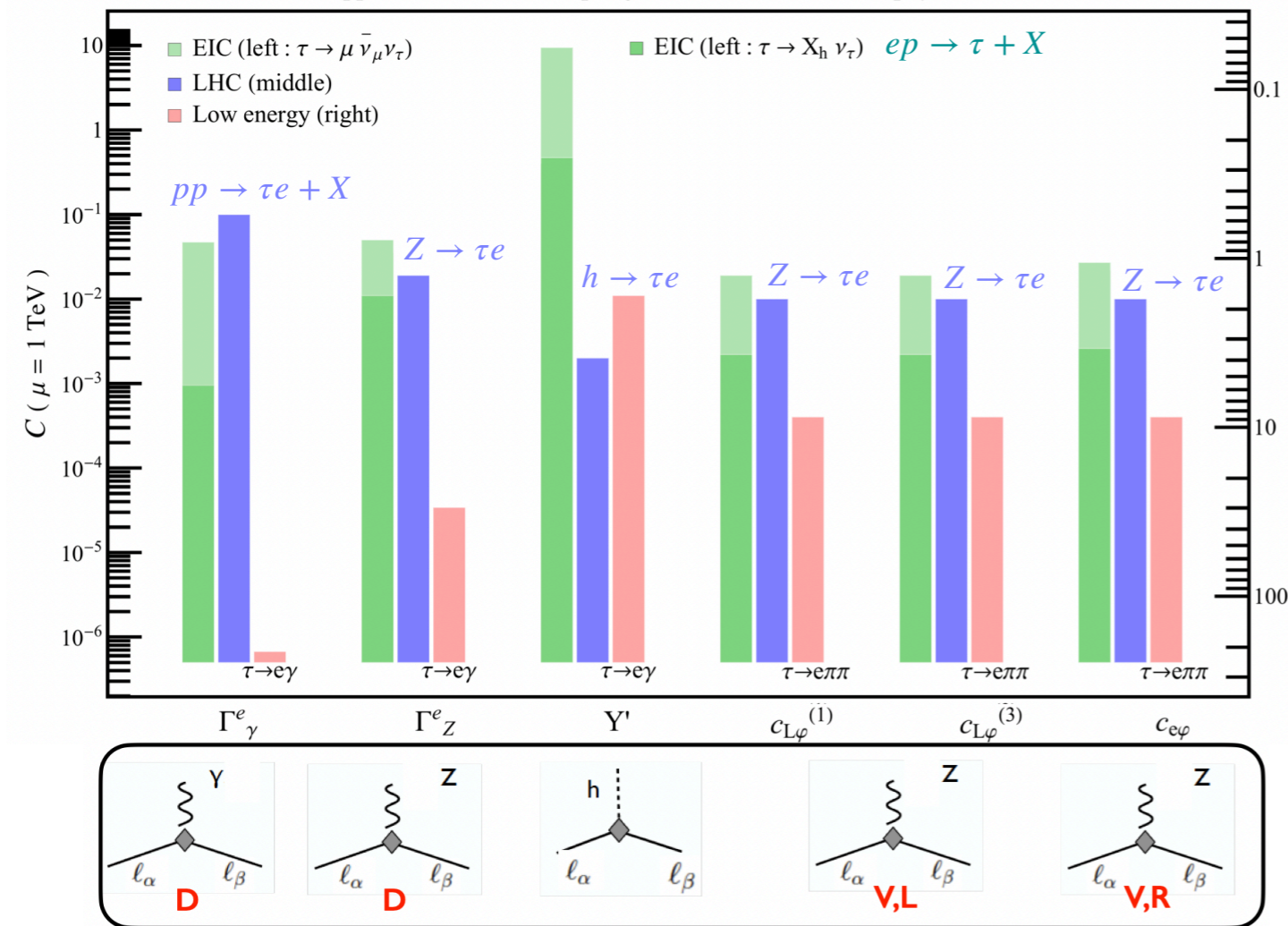
[Phys. Rev. D 104 \(2021\) 032013](#)



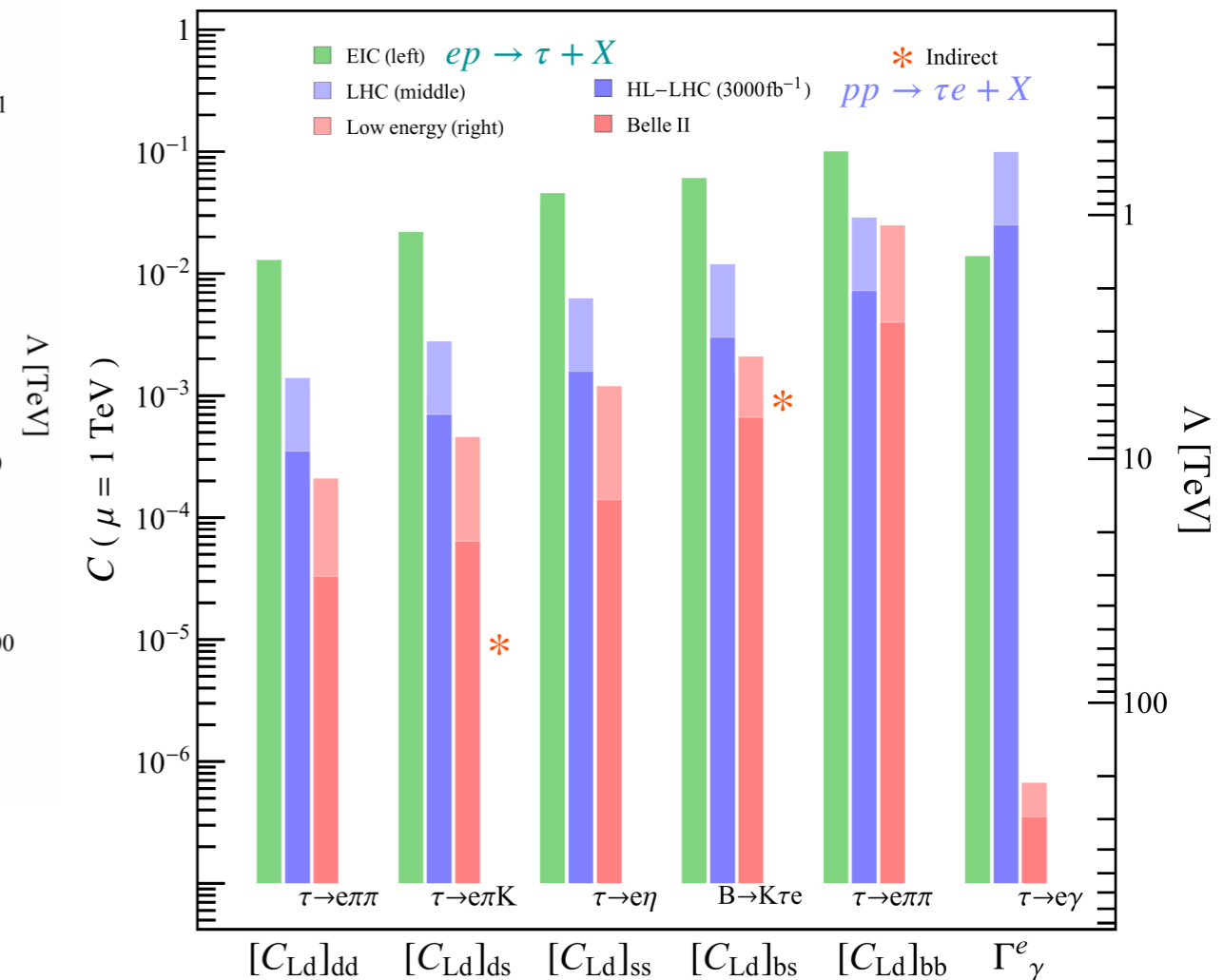
# Global fit: $\tau \rightarrow e$ decays and transitions with $\tau$ in the final state

Model-independent probes of new physics at scale ( $\Lambda$ ) encoded as Wilson coefficients ( $C_n$ ) via EFT approach. For certain operators, Higgs decay and LFV Drell-Yan compete, which are assumed to scale by factor of 4 at HL-LHC. For many other operators, bounds dominated by  $\tau$  and B-decays.

Upper limit on LFV coupling and lower limit on new physics scale



e-Print: 2102.06176 [hep-ph]

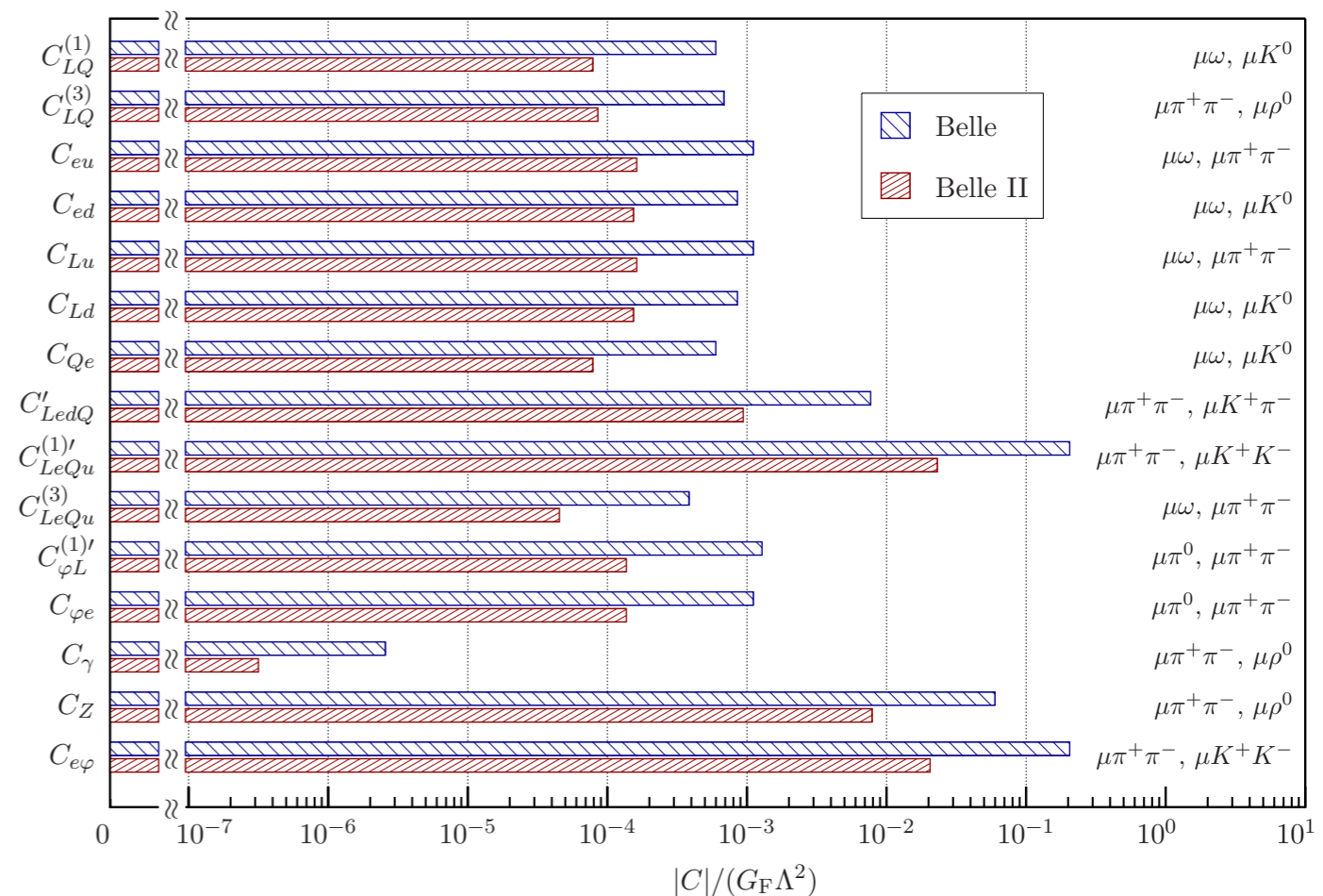


e-Print: 2203.14919 [hep-ph]

# Global fit: $\tau \rightarrow \mu$ decays and transitions with $\tau$ in the final state

Model-independent probes of new physics at scale ( $\Lambda$ ) encoded as Wilson coefficients ( $C_n$ ) via EFT approach.  
 For certain operators, Higgs decay and LFV Drell-Yan compete, which are assumed to scale by factor of 4 at HL-LHC.  
 For many other operators, bounds dominated by  $\tau$  and B-decays.

WC	Operator	WC	Operator
$C_{LQ}^{(1)}$	$(\bar{L}_p \gamma_\mu L_r) (\bar{Q}_s \gamma^\mu Q_t)$	$C_{e\varphi}$	$(\varphi^\dagger \varphi) (\bar{L}_p e_r \varphi)$
$C_{LQ}^{(3)}$	$(\bar{L}_p \gamma_\mu \sigma^I L_r) (\bar{Q}_s \gamma^\mu \sigma^I Q_t)$	$C_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (e_p \gamma^\mu e_r)$
$C_{eu}$	$(\bar{e}_p \gamma_\mu e_r) (\bar{u}_s \gamma^\mu u_t)$	$C_{\varphi L}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{L}_p \gamma^\mu L_r)$
$C_{ed}$	$(\bar{e}_p \gamma_\mu e_r) (\bar{d}_s \gamma^\mu d_t)$	$C_{\varphi L}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_{I\mu} \varphi) (\bar{L}_p \sigma_I \gamma^\mu L_r)$
$C_{Lu}$	$(\bar{L}_p \gamma_\mu L_r) (\bar{u}_s \gamma^\mu u_t)$	$C_{eW}$	$(\bar{L}_p \sigma^{\mu\nu} e_r) \sigma_I \varphi W_{\mu\nu}^I$
$C_{Ld}$	$(\bar{L}_p \gamma_\mu L_r) (\bar{d}_s \gamma^\mu d_t)$	$C_{eB}$	$(\bar{L}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$
$C_{Qe}$	$(\bar{Q}_p \gamma_\mu Q_r) (\bar{e}_s \gamma^\mu e_t)$		
$C_{LedQ}$	$(\bar{L}_p^j e_r) (\bar{d}_s Q_t^j)$		
$C_{LeQu}^{(1)}$	$(\bar{L}_p^j e_r) \varepsilon_{jk} (\bar{Q}_s^k u_t)$		
$C_{LeQu}^{(3)}$	$(\bar{L}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{Q}_s^k \sigma^{\mu\nu} u_t)$		



e-Print: [2203.14919 \[hep-ph\]](https://arxiv.org/abs/2203.14919)



# Summary

- ▶ Search for dark leptophilic scalar in  $e^+e^- \rightarrow \tau^+\tau^-\phi_L$ ;  $\phi_L \rightarrow e^+e^-/\mu^+\mu^-$ 
  - ▶ Performed using 626 fb<sup>-1</sup> of Belle data.
  - ▶ The analysis has been performed in a data-blinded manner: good understanding of the backgrounds.
  - ▶ Completely excludes the region favored by the  $(g-2)_\mu$  anomaly, till  $\phi_L$  mass of 4 GeV.



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- ▶ Search for LFV in  $\tau^\pm \rightarrow \ell^\pm\gamma$  decays
  - ▶ Performed using 988 fb<sup>-1</sup> of Belle data and improved analysis technique.
  - ▶ Most stringent limits for  $\tau \rightarrow \mu\gamma$  at 90% CL.

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- ▶ Search for LFV in  $\tau^\pm \rightarrow \ell^\pm\alpha$  decays
  - ▶ Performed using 62.8 fb<sup>-1</sup> of Belle II data.
  - ▶ Belle II can already set most stringent limits in the world.



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# Outlook

$\tau^- \rightarrow$	Observed Limits			Expected Limits		
	Experiment	Luminosity	UL (obs)	Experiment	Luminosity	UL (exp)
$\mu^- \gamma$	Belle [93]	988 fb <sup>-1</sup>	4.2 × 10 <sup>-8</sup>	Belle II [54]	50 ab <sup>-1</sup>	6.9 × 10 <sup>-9</sup>
	BaBar [83]	516 fb <sup>-1</sup>	4.4 × 10 <sup>-8</sup>	STCF [74]	1 ab <sup>-1</sup>	1.8 × 10 <sup>-8</sup>
				FCC-ee [87, 91]	150 ab <sup>-1</sup>	$\mathcal{O}(10^{-9})$
$\mu^- \mu^+ \mu^-$	Belle [102]	782 fb <sup>-1</sup>	2.1 × 10 <sup>-8</sup>	Belle II [54]	50 ab <sup>-1</sup>	3.6 × 10 <sup>-10</sup>
	BaBar [103]	468 fb <sup>-1</sup>	3.3 × 10 <sup>-8</sup>	LHCb [76]	300 fb <sup>-1</sup>	$\mathcal{O}(10^{-9})$
	LHCb [61]	3 fb <sup>-1</sup>	4.6 × 10 <sup>-8</sup>	CMS [77]	3 ab <sup>-1</sup>	3.7 × 10 <sup>-9</sup>
	CMS [67]	33 fb <sup>-1</sup>	8.0 × 10 <sup>-8</sup>	ATLAS [78]	3 ab <sup>-1</sup>	1.0 × 10 <sup>-9</sup>
	ATLAS [68]	20 fb <sup>-1</sup>	3.8 × 10 <sup>-7</sup>	STCF [74]	1 ab <sup>-1</sup>	1.4 × 10 <sup>-9</sup>
				FCC-ee [87, 91]	150 ab <sup>-1</sup>	$\mathcal{O}(10^{-10})$

- **Observation of LFV in the charged lepton sector would completely change our understanding of physics and herald a new period of discoveries in particle physics. Synergies between different experiments compliment discovery potential/confirmation.**
- **Now is a very interesting era in the searches for LFV in decays of the  $\tau$  lepton, as the current limits will improve by an order of magnitude down to a few parts in  $10^{-10}$  to  $10^{-9}$  at the Belle II experiment. Polarized beams can further improve the sensitivity.**
- **Similar sensitivities will be probed at ATLAS, CMS & LHCb with high luminosity upgrade.**
- **Proposed experiments at STCF, EIC & FCC-ee will continue searches for LFV in the tau sector, also with the possibility of beam polarization.**